



FC-HYPERMESH Matlab toolbox, User's Guide ^{*} under rhum-ubuntu-16-04-3lts computer

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Abstract

This object-oriented Matlab toolbox allows to mesh any d-orthotopes (hyperrectangle in dimension d) and their m-faces by simplices or orthotopes. It was created to show the implementation of the vectorized algorithms presented in [1]. The FC-HYPERMESH toolbox uses Matlab objects and is provided with meshes visualisation tools for dimension less than or equal to 3.

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^{*}Compiled with Matlab 2017a

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1 Introduction

The FC-HYPERMESH toolbox contains a simple class object `OrthMesh` which permits, in any dimension $d \geq 1$, to obtain a simplicial mesh or orthotope mesh with all their m -faces, $0 \leq m < d$. It is also possible with the method function `plotmesh` of the class object `OrthMesh` to represent a mesh or its m -faces for $d \leq 3$.

This toolbox was tested under

Windows 10.0.16299: with Matlab R2015b to R2017b (opengl hardware on NVIDIA Quadro K600 with nvidia-376 driver)

Mac OS X 10.12.6: with Matlab R2015b to R2017b (opengl hardware on Intel HD Graphics 3000 with 2.1 INTEL-10.2.37 driver)

Ubuntu 14.04.5 LTS: with Matlab R2015b to R2017b (opengl hardware on NVIDIA Quadro K1100M with nvidia-340 driver)

Ubuntu 16.04.3 LTS: with Matlab R2015b to R2017b (opengl hardware on NVIDIA GeForce GTX 1070 with nvidia-384 driver)

Ubuntu 17.10: with Matlab R2015b to R2017b (opengl hardware on NVIDIA GeForce GTX 1080 Ti with nvidia-384 driver)

In the following section, the class object `OrthMesh` is presented. Thereafter some warning statements on the memory used by these objects in high dimension are given. Finally computation times for orthotope meshes and simplicial meshes are given in dimension $d \in \llbracket 1, 5 \rrbracket$.

2 Installation

2.1 Installation automatic, all in one (recommended)

For this method, one just has to get/download the install file

`mfc_hypermesh_install.m`

or get it on the dedicated web page. Thereafter, it should be run under Matlab. This command downloads, extracts and configures the *fc-hypermesh* and the required *fc-tools* toolboxes in the current directory.

For example, to install this toolbox in `~/Matlab/toolboxes` directory, one has to copy the file `mfc_hypermesh_install.m` in the `~/Matlab/toolboxes` directory. Then in a Matlab terminal run the following commands

```
>> cd ~/Matlab/toolboxes
>> mfc_hypermesh_install
```

This is the output of the `mfc_hypermesh_install` command on a Linux computer:

```
1- Downloading and extracting the toolboxes
  -> <fc-tools>[0.0.20] ... OK
  -> <fc-hypermesh>[0.0.7] ... OK
2- Setting the <fc-hypermesh> toolbox
Write in ~/Matlab/toolboxes/fc-hypermesh-full/fc_hypermesh-0.0.7/
  configure_loc.m ...
  -> done
3- Using the <fc-hypermesh> toolbox
Under Matlab:
  addpath('~/Matlab/toolboxes/fc-hypermesh-full/fc_hypermesh-0.0.7')
  fc_hypermesh.init()

See ~/Matlab/toolboxes/mfc_hypermesh_set.m
```

The complete toolbox (i.e. with all the other needed toolboxes) is stored in the directory `~/Matlab/toolboxes/fc-hypermesh-full` and, for each Matlab session, one has to set the toolbox by:

```
>> addpath('~/Matlab/toolboxes/fc-hypermesh-full/mfc-hypermesh-0.0.7')
>> fc_hypermesh.init()
```

To **uninstall**, one just has to delete directory

`~/Matlab/toolboxes/fc-hypermesh-full`

2.2 Manual installation

This package uses the `fc_tools` toolbox. So one has to install it as explain in the dedicated web page.

Thereafter, on the `fc_hypermesh` dedicated web page, one can found link to archives (*zip*, *7z* or *tar.gz* format)

- Downloads an archive and extracts it on a folder, for example `~/Matlab/toolboxes`. The toolbox path is `~/Matlab/toolboxes/mfc-hypermesh-0.0.7`
- Adds the toolbox path in Matlab with `addpath` command.
- Verifies that the `fc_tools` toolbox is in the Matlab path. Otherwise, adds it...

3 Using the fc-hypermesh toolbox

First of all, the main class object `OrthMesh` is presented. Thereafter some usage samples are given.

3.1 Class object `OrthMesh`

The aim of the class object `OrthMesh` is to efficiently create an object which contains a mesh of a d -orthotope and all its m -face meshes. An elementary mesh class object `EltMesh` is used to store only one mesh, the main mesh as well as any of the m -face meshes. This class `EltMesh` also simplifies (for me) the codes writing. Its fields are the following:

- d , space dimension
- m , kind of mesh ($m = d$ for the main mesh)
- type, 0 for simplicial mesh or 1 for orthotope mesh
- n_q , number of vertices
- q , vertices array of dimension d -by- n_q
- n_{me} , number of mesh elements
- me , connectivity array of dimension $(d + 1)$ -by- n_{me} for simplices elements or 2^d -by- n_{me} for orthotopes elements
- `toGlobal`, index array linking local array q to the one of the main mesh
- label, name/number of this elementary mesh
- color, color of this elementary mesh (for plotting purpose)

Let the d -orthotope defined by $[a_1, b_1] \times \dots \times [a_d, b_d]$. The class object `OrthMesh` corresponding to this d -orthotope contains the main mesh and all its m -face meshes, $0 \leq m < d$. Its Fields are the following

- d : space dimension
- type: string 'simplicial' or 'orthotope' mesh
- Mesh: main mesh as an `EltMesh` object
- Faces: list of arrays of `EltMesh` objects such that `Faces(1)` is an array of all the $(d - 1)$ -face meshes, `Faces(2)` is an array of all the $(d - 2)$ -face meshes, and so on
- box: a d -by-2 array such that $\text{box}(i, 1) = a_i$ and $\text{box}(i, 2) = b_i$.

Constructor

The `OrthMesh` constructor is :

$$Oh = \text{OrthMesh}(d, N)$$

where N is either a 1-by- d array/list such that $N[i-1]$ is the number of discretization for $[a_i, b_i]$ or either an integer if the the number of discretization is the same in all space directions.

Some options are proposed with the constructor:

$$Oh = \text{OrthMesh}(d, N, \text{Name}, \text{Value})$$

Options are defined with one or more Name,Value pair arguments. The Name argument could be the string

- 'box' : used to specify the d-orthotope $[a_1, b_1] \times \dots \times [a_d, b_d]$ by setting Value as an d-by-2 array such that $a_i = \text{Value}(i,1)$ and $b_i = \text{Value}(i,2)$.
- 'type' : used to select the kind of elements used for meshing. The default value is 'simplicial' and otherwise 'orthotope' can be used.

plotmesh method

The plotmesh() member function can be used to represent the mesh given by an OrthMesh object if the space dimension is less than or equal to 3. Some options are proposed with this function:

plotmesh(Name,Value)

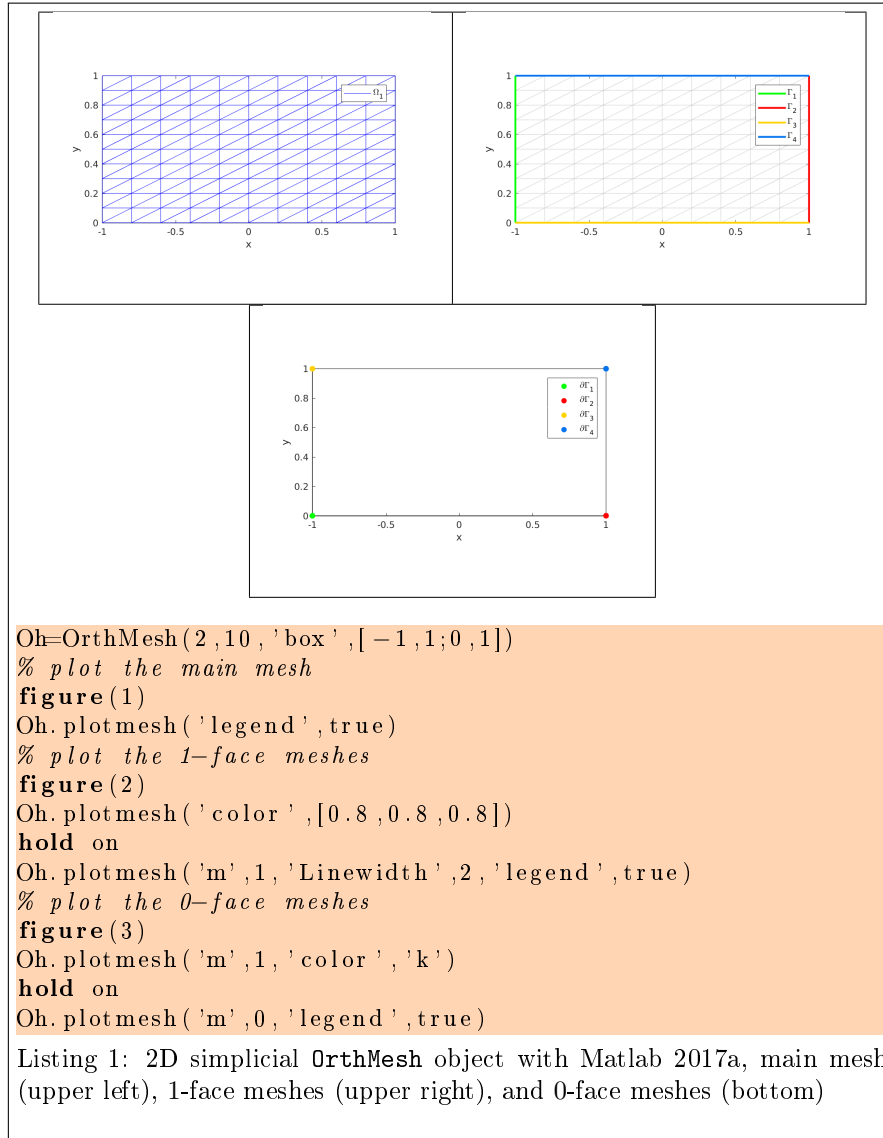
- 'legend_=_value' : if value is True, a legend is displayed. Default is False.
- m = value : plots all the m-faces of the mesh. Default m = d i.e. the main mesh. ($0 \leq m \leq d$)
- ...

3.2 2d-orthotope meshing by simplices

In Listing 15, an OrthMesh object is built under Matlab by using command

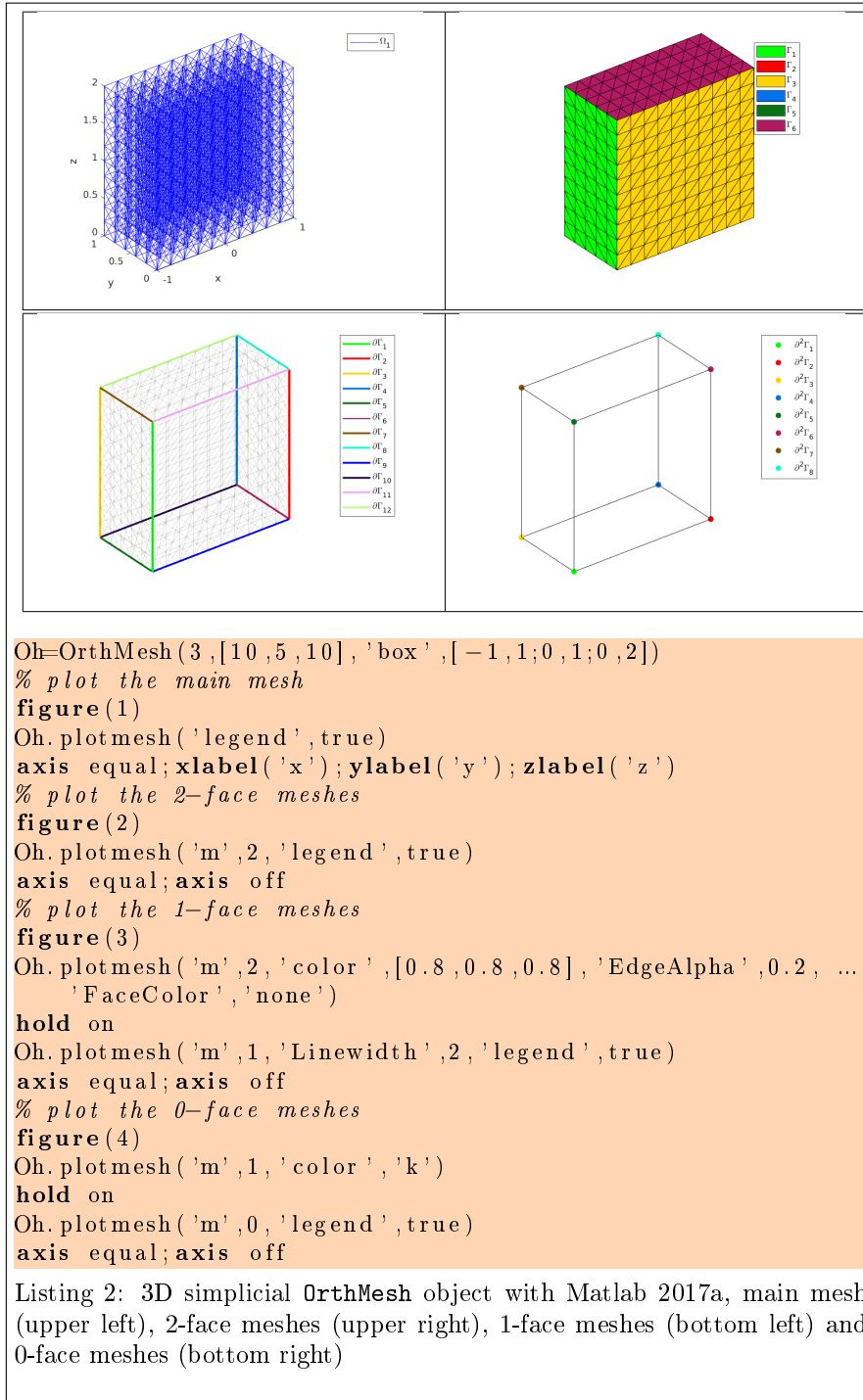
```
Oh=OrthMesh(2,10,'box',[-1,1;0,1])
```

So the Oh object is the tessellations of the orthotope $[-1, 1] \times [0, 1]$ with simplicial elements. In each direction $10 + 1 (= 11!)$ points are taken. So we have 11^2 vertices in this mesh. The main mesh and all the m -face meshes of the resulting object are plotted by using plotmesh method.



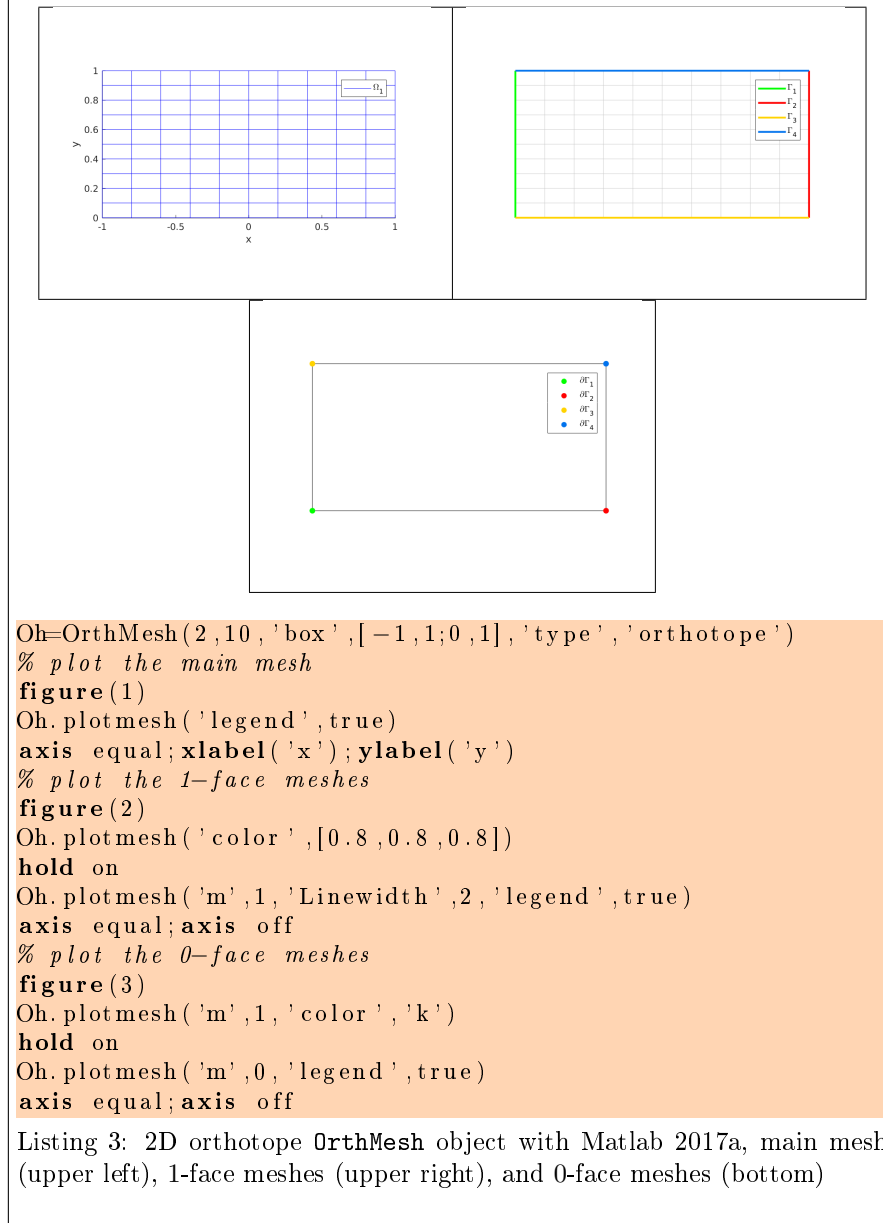
3.3 3d-orthotope meshing by simplices

In Listing 22, an `OrthMesh` object is built under Matlab for the orthotope $[-1,1] \times [0,1] \times [0,2]$ with simplicial elements and $\mathbf{N} = (10,5,10)$. The main mesh and all the m -face meshes of the resulting object are plotted.



3.4 2d-orthotope meshing by orthotopes

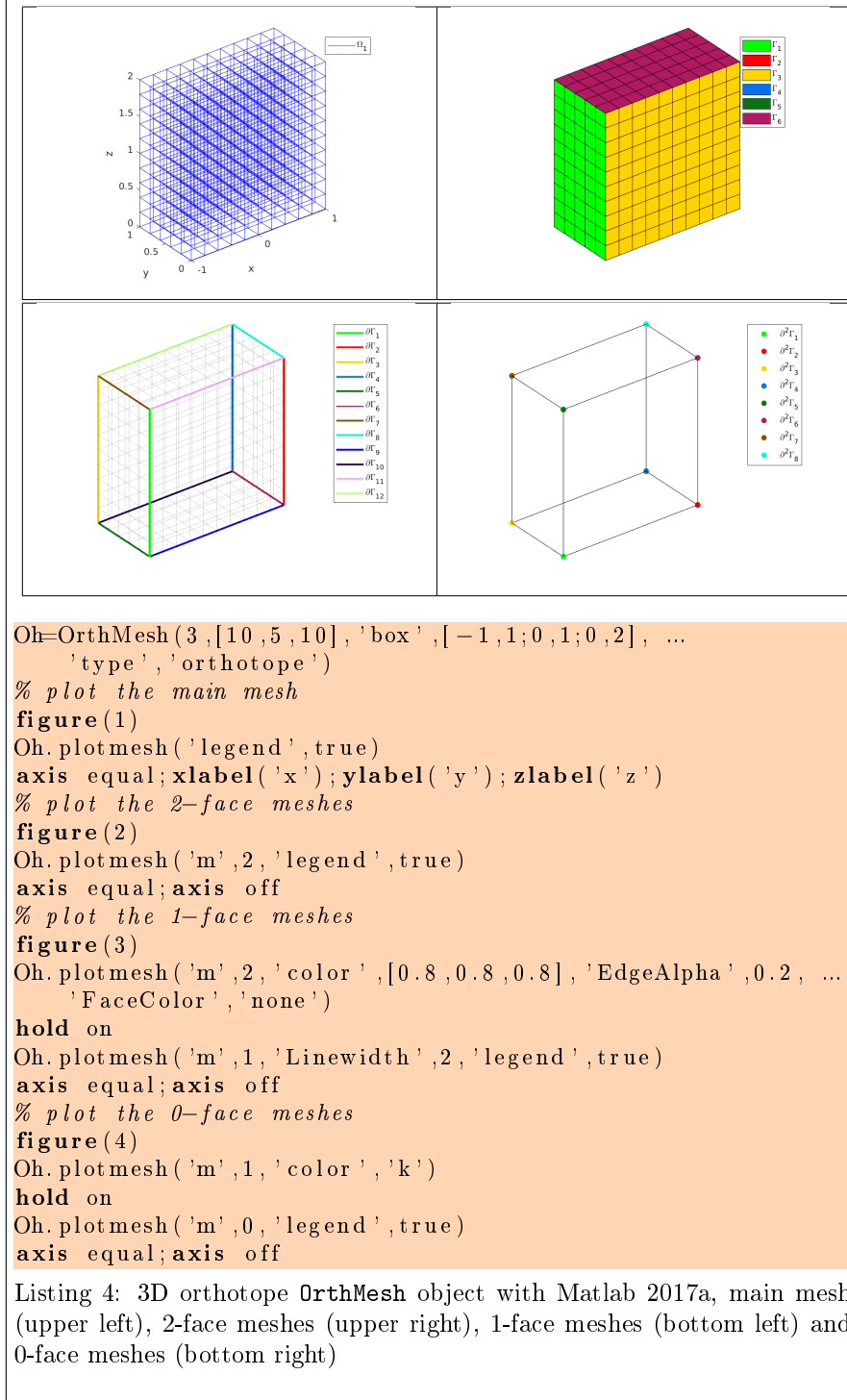
In Listing 22, an `OrthMesh` object is built under Matlab for the orthotope $[-1, 1] \times [0, 1] \times [0, 2]$ with orthotope elements and $\mathbf{N} = (10, 5, 10)$. The main mesh and all the m -face meshes of the resulting object are plotted.



3.5 3d-orthotope meshing by orthotopes

In Listing 22, an `OrthMesh` object is built under Matlab for the orthotope $[-1, 1] \times [0, 1] \times [0, 2]$ with orthotope elements and $\mathbf{N} = (10, 5, 10)$. The main

mesh and all the m -face meshes of the resulting object are plotted.

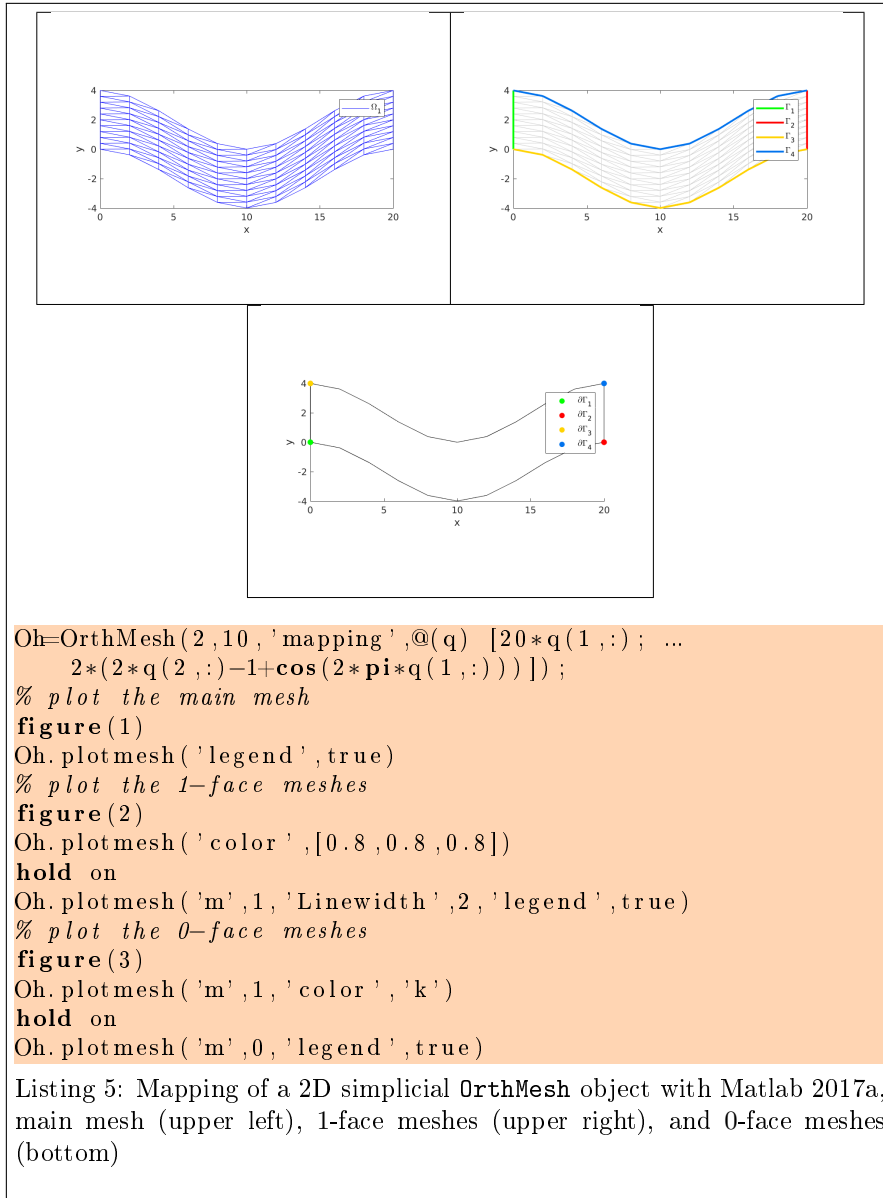


3.6 Mapping of a 2d-orthotope meshing by simplices

For example, the following 2D geometrical transformation allows to deform the reference unit hypercube.

$$[0, 1] \times [0, 1] \longrightarrow \mathbb{R}^2$$

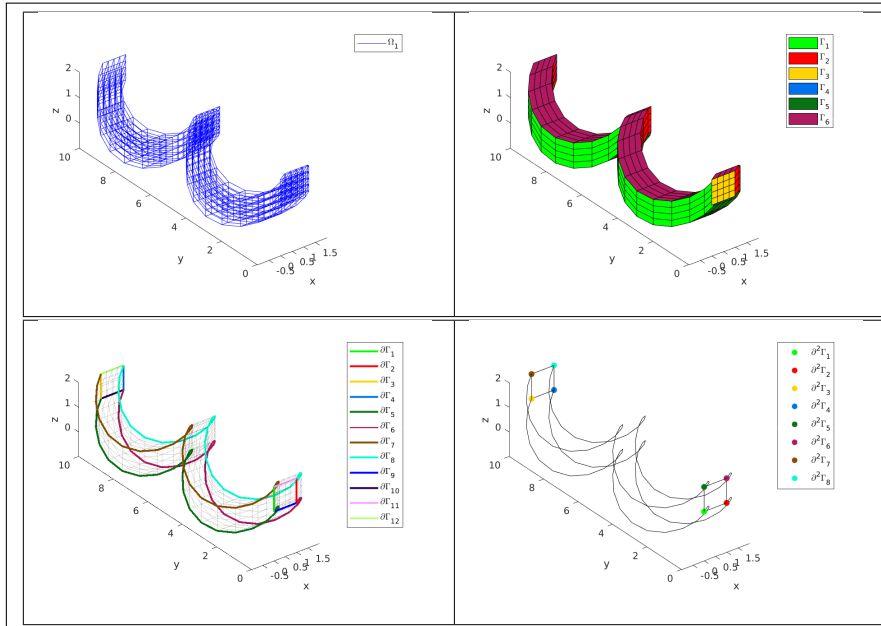
$$\begin{pmatrix} x \\ y \end{pmatrix} \longrightarrow F(x, y) = \begin{pmatrix} 20x \\ 2(2y - 1 + \cos(2\pi x)) \end{pmatrix}$$



3.7 3d-orthotope meshing by orthotopes

For example, the following 3D geometrical transformation allows to deform the reference unit hypercube.

$$\begin{aligned} [0, 1] \times [0, 1] \times [0, 1] &\longrightarrow \mathbb{R}^3 \\ \begin{pmatrix} x \\ y \\ z \end{pmatrix} &\longrightarrow F(x, y, z) = \begin{pmatrix} x + \sin(4\pi y) \\ 10y \\ z + \cos(4\pi y) \end{pmatrix} \end{aligned}$$



```

Map=@(q) [q(1,:)+ sin(4*pi*q(2,:)); 10*q(2,:); ...
          q(3,:)+cos(4*pi*q(2,:))];
Oh=OrthMesh(3,[4,25,4], 'mapping',Map, 'type', 'orthotope');
% plot the main mesh
figure(1)
Oh.plotmesh()
legend('show')
% plot the 2-face meshes
figure(2)
Oh.plotmesh('m',2)
legend('show')
% plot the 1-face meshes
figure(3)
Oh.plotmesh('m',2, 'color',[0.8,0.8,0.8], 'EdgeAlpha',0.2, ...
           'FaceColor','none')
hold on
Oh.plotmesh('m',1, 'Linewidth',2, 'legend',true)
% plot the 0-face meshes
figure(4)
Oh.plotmesh('m',1, 'color','k')
hold on
Oh.plotmesh('m',0, 'legend',true)

```

Listing 6: Mapping of a 3D orthotope `OrthMesh` object with Matlab 2017a, main mesh (upper left), 2-face meshes (upper right), 1-face meshes (bottom left) and 0-face meshes (bottom right)