



Matlab toolbox, User's Guide* version 0.1.4

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Abstract

The experimental  Matlab toolbox contains some simplicial meshes given by their vertices array **q** and connectivity array **me**. These meshes can be easily used in other Matlab codes for debugging or testing purpose.

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*L^AT_EX manual, revision 0.1.4.a, compiled with Matlab 2022a, and toolboxes **fc-meshtools**[0.1.4], **fc-tools**[0.0.34], **fc-bench**[0.1.3], **fc-amat**[0.1.3]

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1 Introduction

A simplicial mesh is given by its vertices array **q** and its connectivity array **me**. For demonstration purpose, some simplicial meshes are given in this package and stored in the `+fc_meshtools/data` directory. They can be load by using the functions `fc_meshtools.simplicial.getMesh2D`, `fc_meshtools.simplicial.getMesh3D` or `fc_meshtools.simplicial.getMesh3Ds`. Here are the kind of simplicial meshes present in this toolbox:

- a triangular mesh in dimension 2, made with 2-simplices (ie. triangles),
- a tetrahedral mesh in dimension 3, made with 3-simplices (ie. tetrahedron),
- a triangular mesh in dimension 3 (surface mesh), made with 2-simplices,
- a line mesh in dimension 2 or 3 made with 1-simplices (ie. lines).

This toolbox was only tested on Ubuntu 22.04.1 with Matlab R2022a.

2 Installation

2.1 Installation automatic, all in one (recommanded)

For this method, one just have to get/download the install file

`mfc_meshtools_install.m`

or get it on the dedicated web page. Thereafter, one run it under Matlab. This command download, extract and configure the *fc-meshtools* and the required *fc-tools* toolbox in the current directory.

For example, to install this toolbox in `~/Matlab` directory, one have to copy the file `mfc_meshtools_install.m` in the `~/Matlab` directory. Then in a Matlab terminal run the following commands

```
>> cd ~/Matlab
>> mfc_meshtools_install
```

There is the output of the `mfc_mesh_install` command on a Linux computer:

```

Parts of the <fc-meshtools> Matlab toolbox.
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1- Downloading and extracting the toolboxes
2- Setting the <fc-meshtools> toolbox
Write in ~/Matlab/fc-meshtools-full/fc_meshtools-0.1.4/configure_loc.m
...
3- Using toolboxes :
->          fc-tools : 0.0.34
->          fc-bench : 0.1.3
->          fc-amat : 0.1.3
with        fc-meshtools : 0.1.4
*** Using instructions
To use the <fc-meshtools> toolbox:
addpath('~/Matlab/fc-meshtools-full/fc_meshtools-0.1.4')
fc_meshtools.init()

See ~/Matlab/mfc_meshtools_set.m

```

The complete toolbox (i.e. with all the other needed toolboxes) is stored in the directory `~/Matlab/fc-meshtools-full` and, for each Matlab session, one have to set the toolbox by:

```

>> addpath('~/Matlab/fc-meshtools-full/fc_meshtools-0.1.4')
>> fc_meshtools.init()

```

If it's the first time the `fc_meshtools.init()` function is used, then its output is

```

Try to use default parameters!
Use fc_tools.configure to configure.
Write in ~/Matlab/fc-meshtools-full/fc_tools-0.0.34/configure_loc.m ...
Try to use default parameters!
Use fc_bench.configure to configure.
Write in ~/Matlab/fc-meshtools-full/fc_bench-0.1.3/configure_loc.m ...
Try to use default parameters!
Use fc_amat.configure to configure.
Write in ~/Matlab/fc-meshtools-full/fc_amat-0.1.3/configure_loc.m ...
Using fc_meshtools[0.1.4] with fc_tools[0.0.34], fc_bench[0.1.3], fc_amat
[0.1.3].

```

Otherwise, the output of the `fc_meshtools.init()` function is

```

Using fc_meshtools[0.1.4] with fc_tools[0.0.34], fc_bench[0.1.3], fc_amat
[0.1.3].

```

For **uninstalling**, one just have to delete directory

`~/Matlab/fc-meshtools-full`

3 Simplicial meshes

The functions `fc_meshtools.simplicial.getMesh2D`, `gfc_meshtools.simplicial.getMesh3D` and `fc_meshtools.simplicial.getMesh3Ds` return a mesh vertices array **q**, a mesh elements connectivity array associated with the input argument *d* (simplex dimension) and the indices array `toGlobal`. The vertices array **q** is a *dim*-by-*n_q* array where *dim* is the space dimension (2 or 3) and *n_q* the number of vertices. The connectivity array **me** is a (*d* + 1)-by-*n_{me}* array where *n_{me}* is the number of mesh elements and $0 \leq d \leq \text{dim}$ is the simplicial dimension:

- $d = 0$: points,
- $d = 1$: lines,
- $d = 2$: triangle,
- $d = 3$: tetrahedron.

So we can use theses functions to obtain

- 3D mesh: `getMesh3D(3)` (*main* mesh), `getMesh3D(2)`, `getMesh3D(1)`, `getMesh3D(0)`,
- 3D surface mesh: `getMesh3Ds(2)` (*main* mesh), `getMesh3Ds(1)` , `getMesh3Ds(0)`,
- 2D mesh: `getMesh2D(2)` (*main* mesh), `getMesh2D(1)`, `getMesh2D(0)`.

For example,

- `[q3,me3,toGlobal3]=fc_meshtools.simplicial.getMesh3D(3)` return a 3-simplicial mesh (*main* mesh) in space dimension $dim = 3$,
- `[q2,me2,toGlobal2]=fc_meshtools.simplicial.getMesh3D(2)` return a 2-simplicial mesh in space dimension $dim = 3$.

The third output are indices of the vertices in the *main* mesh:
`q3(:,toGlobal2) == q2`

4 Functions

4.1 getMesh functions

Returns a vertices array `q`, a connectivity array `me` and an indices array `toGlobal`.

Description

```
[q,me,toGlobal]=fc_meshtools.simplicial.getMesh3D(d)
```

```
[q,me,toGlobal]=fc_meshtools.simplicial.getMesh3Ds(d)
```

```
[q,me,toGlobal]=fc_meshtools.simplicial.getMesh2D(d)
```

Returns a vertices array `q`, a connectivity array `me` and an indices array `toGlobal` depending on the value of the `d`. For a 3D mesh, $d \in \llbracket 0, 3 \rrbracket$, and for a 2D or 3Ds mesh, $d \in \llbracket 0, 2 \rrbracket$.

In Listing 2, some examples are provided.

Listing 1: : examples of `fc_meshtools.simplicial.getMesh3D` function usage

```
[q2, me2, toG2]=fc_meshtools.simplicial.getMesh3D(2);
[q3, me3, toG3]=fc_meshtools.simplicial.getMesh3D(3);
whos('q2','me2','toG2','q3','me3','toG3')
fprintf('Error: %5e\n', norm(q3(:, toG2) - q2, Inf))
```

Output

Name	Size	Bytes	Class	Attributes
me2	3x15074	361776	double	
me3	4x84302	2697664	double	
q2	3x7533	180792	double	
q3	3x17416	417984	double	
toG2	1x7533	60264	double	
toG3	1x17416	139328	double	

Error: 0.00000e+00

4.2 Volumes function

Syntaxe Returns all the element volumes of a mesh given by a vertices array `q` and a connectivity array `me`. One can refer to [1] for computationnal details.

Description

```
vols=fc_meshtools.simplicial.Volumes(q,me)
```

`vols(k)` is the volume of the `k`-th mesh element where its vertices are the columns of `q(:, me(:, k))`.

In Listing 2, some examples are provided.

Listing 2: : examples of `fc_meshtools.simplicial.Volumes` function usage

```
[q, me, toG]=fc_meshtools.simplicial.getMesh3D(2);
vols=fc_meshtools.simplicial.Volumes(q, me);
whos('q','me','toG','vols')
```

Output

Name	Size	Bytes	Class	Attributes
me	3x15074	361776	double	
q	3x7533	180792	double	
toG	1x7533	60264	double	
vols	1x15074	120592	double	

4.3 Gradient of barycentric coordinates

Syntaxe Returns all the gradients of barycentric coordinates of each element of a mesh given by a vertices array `q` and a connectivity array `me`. One can refer to [1] for computationnal details.

Description

```
G=fc_meshtools.simplicial.GradBaCo(q,me)
```

`G(k, i, :)` is the gradient of the `i`-th barycentric coordinate of the `k`-th mesh element.

In Listing 3, some examples are provided.

Listing 3: : examples of `fc_meshtools.simplicial.GradBaCo` function usage

```
[q,me,toG]=fc_meshtools.simplicial.getMesh3D(3);
G=fc_meshtools.simplicial.GradBaCo(q,me);
whos('q','me','toG','G')
```

Output

Name	Size	Bytes	Class	Attributes
G	84302x4x3	8092992	double	
me	4x84302	2697664	double	
q	3x17416	417984	double	
toG	1x17416	139328	double	

4 References

- [1] F. Cuvelier. Exact integration for products of power of barycentric coordinates over d -simplexes in R^n . <http://hal.archives-ouvertes.fr/hal-00931066v1>, June 2018. preprint.

Informations for git maintainers of the

 **Matlab toolbox**

git informations on the toolboxes used to build this manual

```
-----
name : fc-meshtools
tag : 0.1.4.a
commit : 57826462a8280dec5aa1eff0d424877097187b41
date : 2022-12-19
time : 08-27-27
status : 0
-----
name : fc-tools
tag : 0.0.34
commit : 34edf9393425222cdb72914e51e6465f50aa6760
date : 2022-12-21
time : 09-28-20
status : 0
-----
name : fc-bench
tag : 0.1.3
commit : 6c8969bb49b90c7cae34e70c88dd2f968766376b
date : 2022-12-17
time : 13-58-43
status : 0
-----
name : fc-amat
tag : 0.1.3
commit : 90dbaa2839188cf8e01629817e5f8ba1b7188052
date : 2022-12-19
time : 07-41-33
status : 0
-----
```

git informations on the L^AT_EX package used to build this manual

```
-----
name : fctools
tag :
commit : c9a33ce7b4dacf90f66e5e49856e69afadac0a3
date : 2022-12-17
time : 07:57:20
status : 1
-----
```

Using the remote configuration repository:

```
url      ssh://lagagit/MCS/Cuvelier/Matlab/fc-config
commit   1ddb965ef261410ecee4ce178be4ceb85939de04
```