



FC-GRAPHICS4MESH Octave package, User's Guide *

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Abstract

This Octave package allows to display simplicial meshes or datas on simplicial meshes. A simplicial mesh must be given by two arrays : the vertices array and the connectivity array.

Contents

1	Introduction	2
2	Installation	2
2.1	Installation automatic, all in one	2
3	Mesh	3
4	PLOTMESH function	4
5	PLOT function	7
6	PLOTISO function	10
7	SLICEMESH function	14
8	SLICE function	15

*Compiled with Octave 4.2.1

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9	SLICEISO function	16
10	PLOTQUIVER function	19

1 Introduction

The **experimental** Octave package uses internal functions for displaying simplicial meshes or datas on simplicial meshes. Simplicial meshes could be:

- a triangular mesh in dimension 2, made with 2-simplices (ie. triangles),
- a tetrahedral mesh in dimension 3, made with 3-simplices (ie. tetrahedron),
- a triangular mesh in dimension 3 (surface mesh), made with 2-simplices,
- a line mesh in dimension 2 or 3 made with 1-simplices (ie. lines).

A simplicial mesh is given by its vertices array `q` and its connectivity array `me`. For demonstration purpose, some simplicial meshes are given in this package. They can be load by using the function `getMesh2D`, `getMesh3D` or `getMesh3Ds` of the `fc_graphics4mesh` package.

This package was tested under

Windows 10: with Octave 4.2.0 and 4.2.1

MacOS Sierra: with Octave 4.2.1 (install with homebrew)

Ubuntu 14.04.5 LTS: with Octave 4.2.1 and 4.2.0 (compiled from source)

Ubuntu 16.04 LTS: with Octave 4.2.1 and 4.2.0 (compiled from source)

It is not compatible with Octave 4.0.x and previous.

2 Installation

2.1 Installation automatic, all in one

For this method, one just have to get/download the install file

`ofc_graphics4mesh_install.m`

or get it on the dedicated web page. Thereafter, one run it under Octave. This command download, extract and configure the *fc-graphics4mesh* and the required *fc-tools* package in the current directory.

For example, to install this package in directory `~/Octave/packages`, in a terminal one can do:

```
# mkdir -p ~/Octave/packages
# cd ~/Octave/packages
# wget ...
    http://www.math.univ-paris13.fr/~cuvelier/software/codes/fc-graphics4mesh/0.0.1/ofc_graphics4mesh.in
```

Then in a Octave terminal run the following commands

```
>> cd ~/Octave/toolboxes
>> ofc_graphics4mesh_install
```

There is the output of the `ofc_graphics4mesh_install` command:

```
1- Downloading and extracting the packages
  -> <fc-tools>[0.0.18] ... OK
  -> <fc-graphics4mesh>[0.0.1] ... OK
2- Setting the <fc-graphics4mesh> package
Write in ...
  ~/Octave/packages/fc-graphics4mesh-full/fc_graphics4mesh-0.0.1/configure_loc.m ...
  ...
  -> done
3- Using the <fc-graphics4mesh> package
Under Octave:
  addpath('~/Octave/packages/./fc-graphics4mesh-full/fc_graphics4mesh-0.0.1')
  fc_graphics4mesh.init()

See ~/Octave/packages/ofc_graphics4mesh_set.m
```

The complete package (i.e. with all the other needed packages) is stored in the directory `~/Octave/packages/fc-graphics4mesh-full` and, for each Octave session, one have to set the package by:

```
>> ...
    addpath('~/Octave/packages/fc-graphics4mesh-full/ofc_graphics4mesh-0.0.4')
>> fc_graphics4mesh.init()
```

For **uninstalling**, one just have to delete directory `~/Octave/packages/fc-graphics4mesh-full`

3 Mesh

The functions `getMesh2D`, `getMesh3D` and `getMesh3Ds` return a mesh vertices array q , a mesh elements connectivity array associated with the input argument d (simplex dimension) and the indices array `toGlobal`. The vertices array q is a dim -by- n_q array where dim is the space dimension (2 or 3) and n_q the number of vertices. The connectivity array me is a $(d + 1)$ -by- n_{me} array where n_{me} is the number of mesh elements and $0 \leq d \leq dim$ is the simplicial dimension:

- $d = 0$: points,
- $d = 1$: lines,
- $d = 2$: triangle,
- $d = 3$: tetrahedron.

So we can use theses functions to obtain

- 3D mesh: `getMesh3D(3)` (*main* mesh), `getMesh3D(2)`, `getMesh3D(1)`, `getMesh3D(0)`,
- 3D surface mesh: `getMesh3Ds(2)` (*main* mesh), `getMesh3Ds(1)`, `getMesh3Ds(0)`,
- 2D mesh: `getMesh2D(2)` (*main* mesh), `getMesh2D(1)`, `getMesh2D(0)`.

For example,

- `[q3,me3,toGlobal3]=fc_graphics4mesh.getMesh3D(3)` return a 3-simplicial mesh (main mesh) in space dimension $dim = 3$,
- `[q2,me2,toGlobal2]=fc_graphics4mesh.getMesh3D(2)` return a 2-simplicial mesh in space dimension $dim = 3$.

The third output are indices of the vertices in the *main* mesh:
`q3(:,toGlobal2) == q2`

4 **PLOTMESH** function

The function **PLOTMESH** displays a mesh given by

Syntaxe

```
fc_graphics4mesh.plotmesh(q,me)
fc_graphics4mesh.plotmesh(q,me,Name,Value,...)
```

Description

`plotmesh(q,me)` displays all the Th.d-dimensional simplices elements.

`plotmesh(q,me,Name,Value,...)` specifies function options using one or more Name,Value pair arguments. Options of first level are

- **'color'** : to specify the color of the displayed mesh elements. (default : 'blue'),
- **'cutPlan'** : (only for simplices in dimension 3) cut mesh by n plans given by n -by-4 array P where the equation of the i -th cut plan is given by

$$P(i,1)x + P(i,2)y + P(i,3)z + P(i,4) = 0.$$

The normal vector $P(i,1 : 3)$ pointed to the part of the mesh not displayed. default : `[]` (no cut).

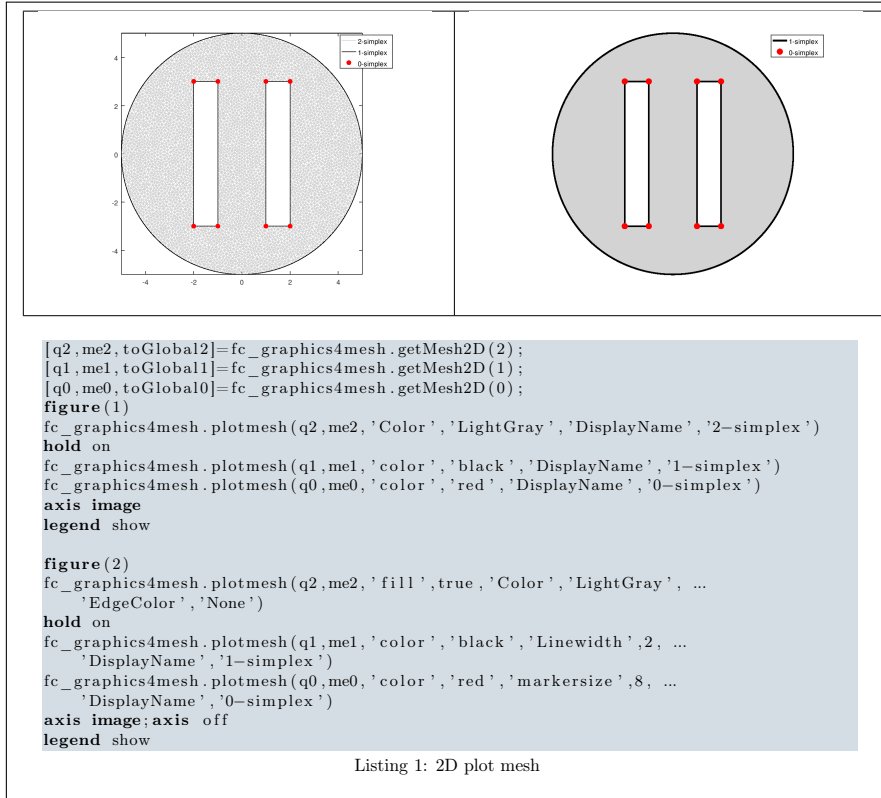
The options of second level depend on the type of elementaries mesh elements to represent.

One can use any option of the following functions according to the type of d -simplex to be represented.

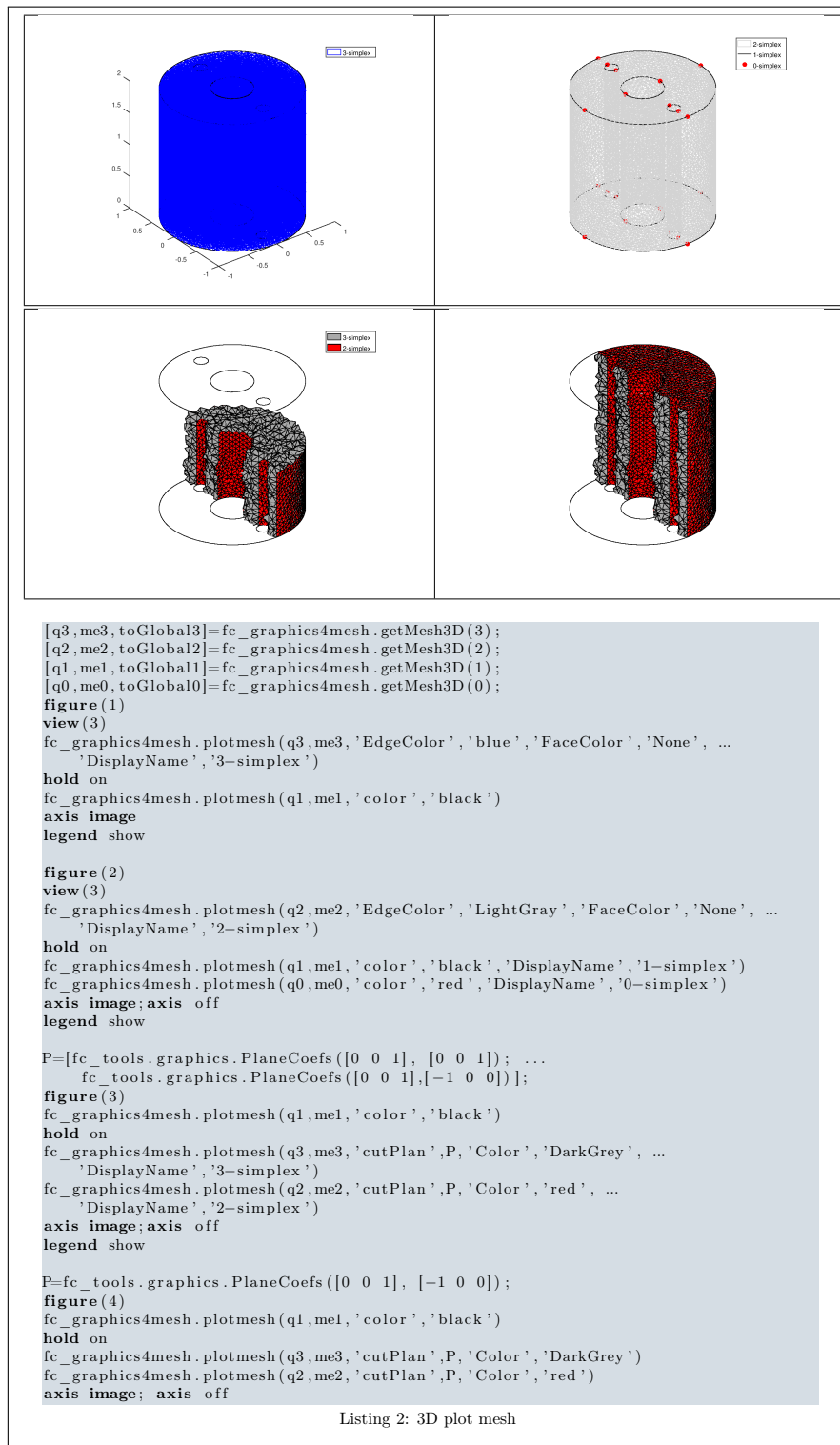
- In dimension 3,
 - if $d == 3$, **patch** function is used,
 - if $d == 2$, **trimesh** function is used,
 - if $d == 1$, **plot3** function is used,
 - if $d == 0$, **plot3** function is used,
- In dimension 2,
 - if $d == 2$, **trimesh** or **patch** function is used,
 - if $d == 1$, **plot** function is used,

- if $d == 0$, **plot** function is used,
- In dimension 1,
 - if $d == 1$, **line** function is used,
 - if $d == 0$, **plot** function is used,

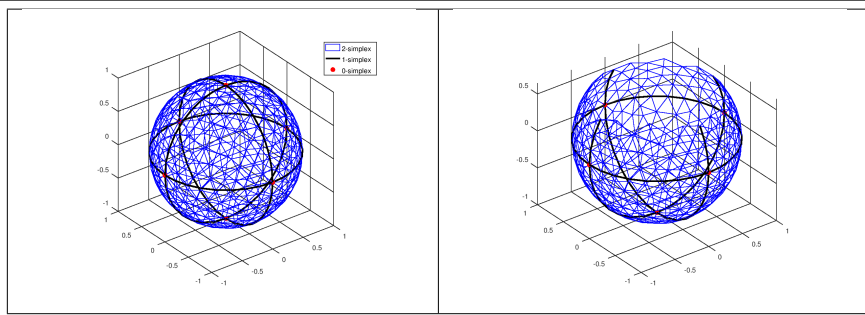
2D example



3D example



3D surface example



```
[q2,me2,toGlobal2]=fc_graphics4mesh.getMesh3Ds(2);
[q1,me1,toGlobal1]=fc_graphics4mesh.getMesh3Ds(1);
[q0,me0,toGlobal0]=fc_graphics4mesh.getMesh3Ds(0);
figure(1)
view(3)
fc_graphics4mesh.plotmesh(q2,me2,'EdgeColor','blue','FaceColor','None',...
    'DisplayName','2-simplex')
hold on
fc_graphics4mesh.plotmesh(q1,me1,'color','black',...
    'Linewidth',2,'DisplayName','1-simplex')
fc_graphics4mesh.plotmesh(q0,me0,'color','red','DisplayName','0-simplex')
axis image
legend show
P=fc_tools.graphics.PlaneCoefs([0 0 1/2], [0 0 1]);
figure(2)
fc_graphics4mesh.plotmesh(q2,me2,'EdgeColor','blue','FaceColor','None','cutPlan',P)
hold on
fc_graphics4mesh.plotmesh(q1,me1,'color','black','Linewidth',2,'cutPlan',P)
fc_graphics4mesh.plotmesh(q0,me0,'color','red','cutPlan',P)
axis image
```

Listing 3: 3D surface mesh : plot function

5 PLOT function

The function **PLOT** displays data on a mesh given by its vertices array q and its connectivity array me .

Syntax

```
fc_graphics4mesh.plot(q,me,u)
fc_graphics4mesh.plot(q,me,u,Name,Value,...)
```

Description

plot(q,me,u) displays data u on a simplicial mesh. The data u can be an handle function or an array.

plot($q,me,u,Name,Value,...$) specifies function options using one or more $Name,Value$ pair arguments. Options of first level are

- **'cutPlan'** : (only for simplices in dimension 3) cut mesh by n plans given by n -by-4 array P where the equation of the i -th cut plan is given by

$$P(i,1)x + P(i,2)y + P(i,3)z + P(i,4) = 0.$$

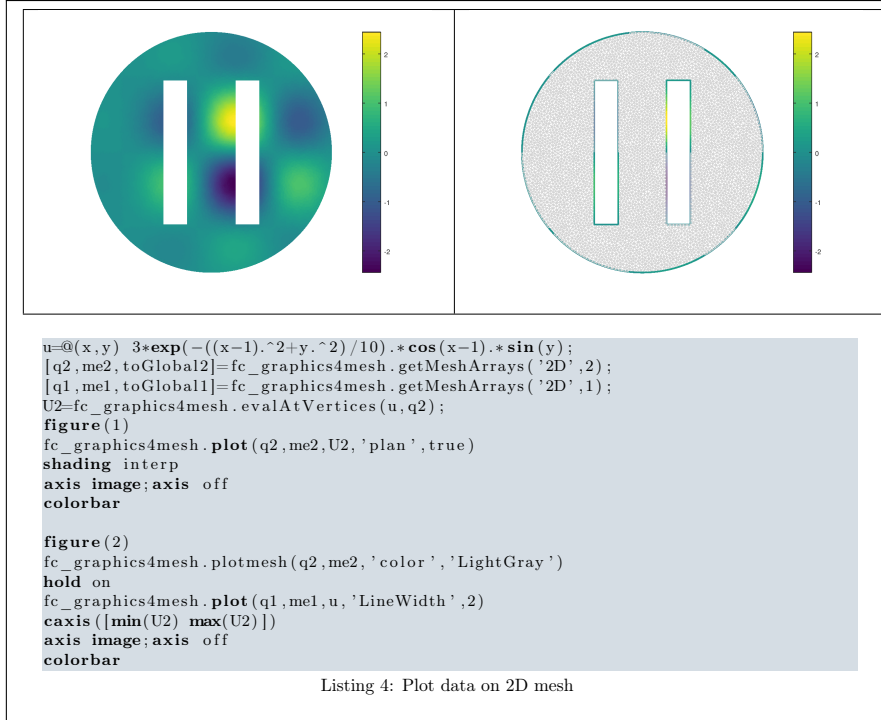
The normal vector $P(i, 1 : 3)$ pointed to the part of the mesh not displayed. default : `[]` (no cut).

The options of second level depend on the type of elementaries mesh elements to represent.

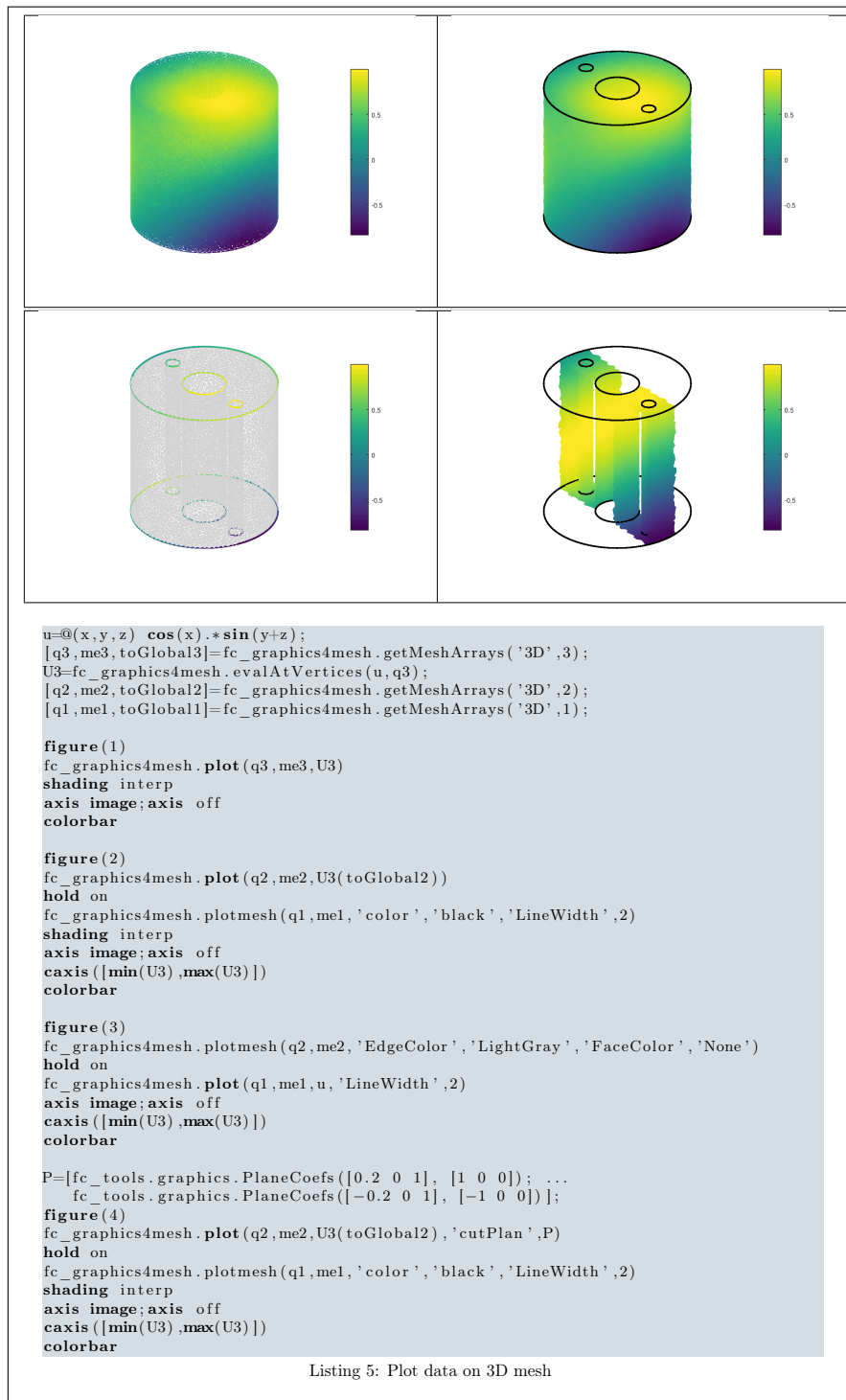
One can use any option of the following functions according to the type of d -simplex to be represented.

- In dimension 3, **patch** function is used.
- In dimension 2,
 - if $d == 2$, **surf** or **patch** (option 'plan' to true) function is used,
 - if $d == 1$, **patch** function is used,
- In dimension 1, **plot** function is used.

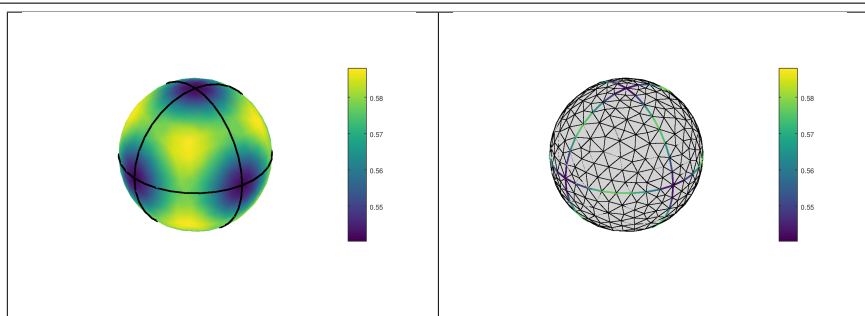
2D example



3D example



3D surface example



```

u=@(x,y,z) cos(x).*cos(y).*cos(z);
[q2,me2,toGlobal2]=fc_graphics4mesh.getMesh3Ds(2);
[q1,me1,toGlobal1]=fc_graphics4mesh.getMesh3Ds(1);
U2=fc_graphics4mesh.evalAtVertices(u,q2);
U1=fc_graphics4mesh.evalAtVertices(u,q1);
figure(1)
fc_graphics4mesh.plot(q2,me2,U2)
hold on
fc_graphics4mesh.plotmesh(q1,me1,'color','k','LineWidth',2)
shading interp
axis image;axis off
colorbar
figure(2)
fc_graphics4mesh.plotmesh(q2,me2,'color','LightGray')
hold on
fc_graphics4mesh.plot(q1,me1,U1,'LineWidth',2)
axis image;axis off
caxis([min(U2),max(U2)])
colorbar
P=fc_tools.graphics.PlaneCoefs([0 0 0], [0 0 1]);
figure(3)
fc_graphics4mesh.plot(q2,me2,U2,'cutPlan',P)
hold on
fc_graphics4mesh.plotmesh(q1,me1,'color','k','LineWidth',2)
shading interp
axis image;axis off
caxis([min(U2),max(U2)])
colorbar
figure(4)
fc_graphics4mesh.plotmesh(q2,me2,'color','LightGray','cutPlan',P)
hold on
fc_graphics4mesh.plot(q1,me1,U1,'LineWidth',2,'cutPlan',P)
axis image;axis off
caxis([min(U2),max(U2)])
colorbar

```

Listing 6: 3D surface mesh : plot function

6

PLOTISO function

The function **PLOT** displays isolines from datas on a 2-simplicial mesh given by its vertices array q and its connectivity array me .

Syntax

```

fc_graphics4mesh.plotiso(q,me,u)
fc_graphics4mesh.plotiso(q,me,u,Name,Value,...)

```

Description

`plotiso(q,me,u)` displays isolines from datas on the 2-simplicial mesh given by the vertices array q and the connectivity array me . The data u can be an

handle function or an array.

`plotiso(q,me,u,Name,Value, ...)` specifies function options using one or more Name,Value pair arguments. Options of first level are

- **'niso'** : to specify the number of isolines (default : 10)
- **'isorange'** : to specify the list of isovalues (default : empty)
- **'isocolorbar'** : if true, colorbar with isovalues is drawn (default : false)
- **'format'** : to specify the format of the isovalues on the colorbar (default : '%g')
- **'plan'** : if true, (default : false)
- **'color'** : to specify one color for all isolines (default : empty)

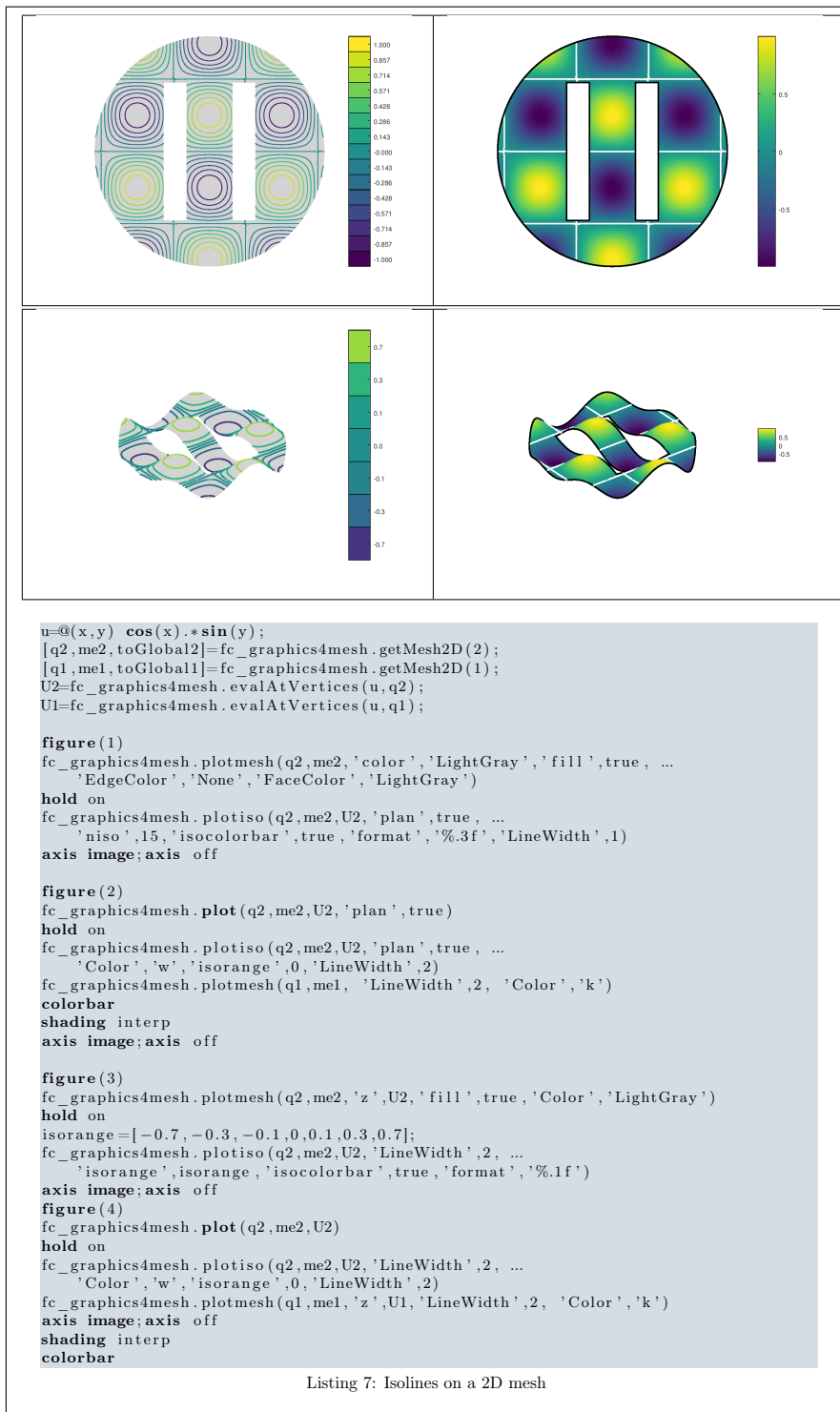
The options of second level are all options of

- **plot3** function in dimension 3 or in dimension 2 with **'plan'** set to false
- **plot** function in 2 with **'plan'** set to true

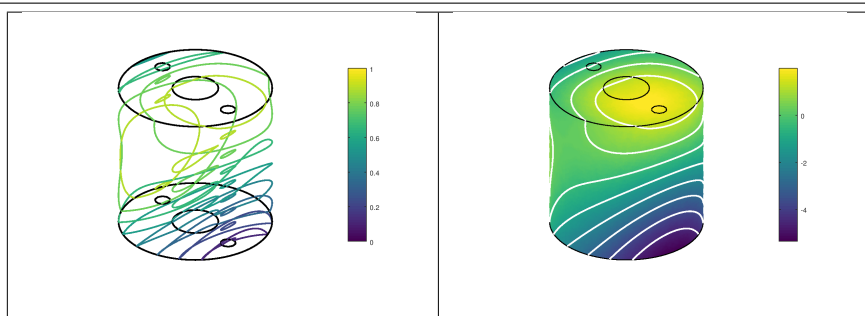
This function accepts until 3 output arguments :

- bullet* 1st output is the colors of the isolines
- bullet* 2nd output is the isovalues of the isolines
- bullet* 3th output is all the handles of the isolines as an 2D-array of dimension N-by-niso, where N is the number of 2-simplex elementary meshes where isolines are drawn.

2D example



3D example



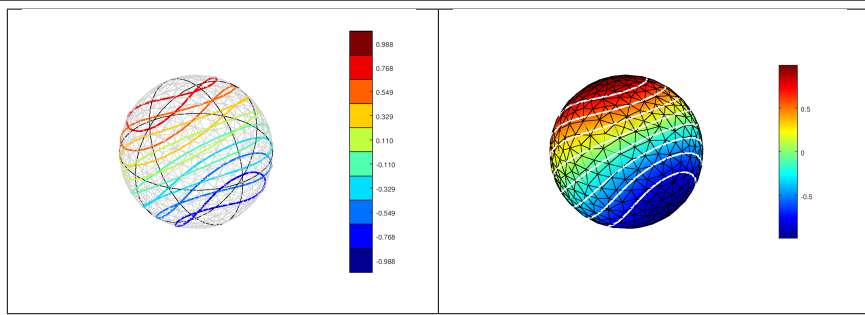
```

u=@(x,y,z) -2+4*cos(x).*sin(y+z);
[q2,me2,toGlobal2]=fc_graphics4mesh.getMeshArrays('3D',2);
U2=fc_graphics4mesh.evalAtVertices(u,q2);
[q1,me1,toGlobal1]=fc_graphics4mesh.getMeshArrays('3D',1);
U1=fc_graphics4mesh.evalAtVertices(u,q1);
figure(1)
fc_graphics4mesh.plotmesh(q1,me1,'color','black','LineWidth',2)
hold on
fc_graphics4mesh.plotiso(q2,me2,U2,'LineWidth',2)
colorbar
shading interp
axis image;axis off
figure(2)
fc_graphics4mesh.plot(q2,me2,U2)
hold on
fc_graphics4mesh.plotiso(q2,me2,U2,'color','white','LineWidth',2)
fc_graphics4mesh.plotmesh(q1,me1,'color','black','LineWidth',1)
shading interp
axis image;axis off
colorbar

```

Listing 8: Isolines on surfaces of a 3D mesh

3D surface example



```

u=@(x,y,z) cos(x).*sin(y+z);
[q2,me2,toGlobal2]=fc_graphics4mesh.getMeshArrays('3Ds',2);
U2=fc_graphics4mesh.evalAtVertices(u,q2);
[q1,me1,toGlobal1]=fc_graphics4mesh.getMeshArrays('3Ds',1);
figure(1)
colormap('jet')
fc_graphics4mesh.plotmesh(q2,me2,'EdgeColor','LightGray','FaceColor','None')
hold on
fc_graphics4mesh.plotmesh(q1,me1,'Color','black')
fc_graphics4mesh.plotiso(q2,me2,U2,'isocolorbar',true,'format','%f', ...
'LineWidth',2)
axis image;axis off
figure(2)
colormap('jet')
fc_graphics4mesh.plot(q2,me2,U2)
hold on
fc_graphics4mesh.plotmesh(q1,me1,'Color','black')
fc_graphics4mesh.plotiso(q2,me2,U2,'LineWidth',2,'Color','w')
colorbar
axis image;axis off

```

Listing 9: 3D surface mesh : plotiso function

7

SLICEMESH function

The **SLICEMESH** function displays intersection of a plane and a 3D mesh given by its vertices array q and its connectivity array me .

Syntaxe

```

fc_graphics4mesh.slicemesh(q,me,P)
fc_graphics4mesh.slicemesh(q,me,P,Name,Value,...)

```

Description

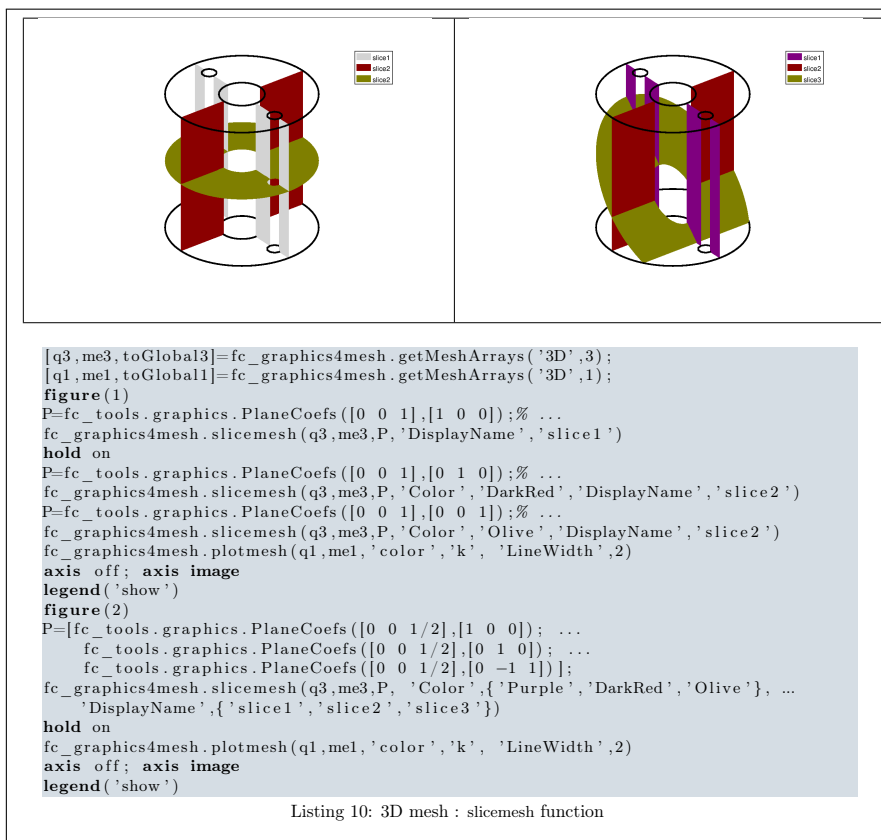
`slicemesh(q,me,P)` displays intersection of the plane defined by $P(1)x + P(2)y + P(3)z + P(4) = 0$ and all the 3-dimensional simplices elements given by q and me arrays. To compute P one can use the `fc_tools.graphics.PlaneCoefs` function of the **FC-TOOLS** package. The 1-by-4 array P , is obtained with $P = \text{fc_tools.graphicsPlaneCoefs}(Q,V)$ where Q is a point in the plane and V is a vector orthogonal to it. One can also used a n -by-4 array P where each line define a plane.

`slicemesh(q,me,P,Name,Value,...)` specifies function options using one or more `Name,Value` pair arguments. Options of first level are

- 'color' : to specify the slice color (default : 'LightGray', rgb=[0.9,0.9,0.9])

The options of second level are all options of the **patch** function except 'FaceColor' and 'EdgeColor'

3D example



8

SLICE function

The **S**LICE function displays intersection of a plane and a 3D mesh given by its vertices array q and its connectivity array me.

Syntaxe

```

fc_graphics4mesh.slice(q,me,u,P)
fc_graphics4mesh.slice(q,me,u,P,Name,Value,...)

```

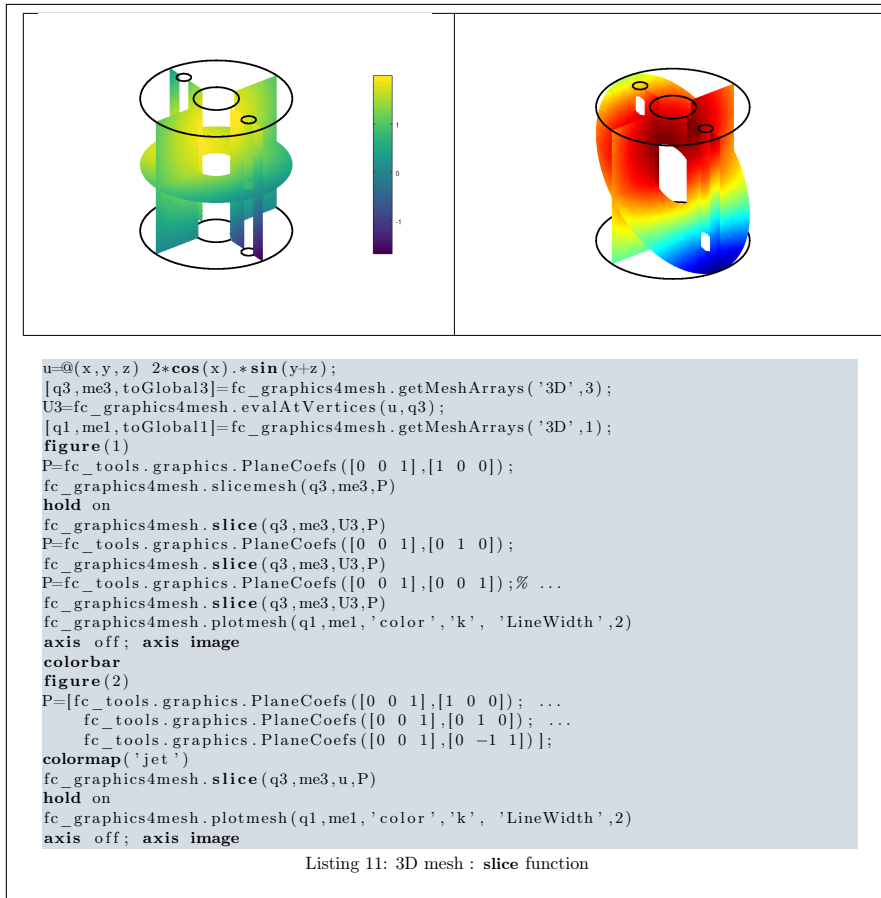
Description

slice(q,me,u,P) displays data on the intersection of the plane defined by $P(1)x + P(2)y + P(3)z + P(4) = 0$ and all the 3-dimensional simplices

elements given by q and me arrays. To compute P one can use the `fc_tools.graphics.PlaneCoefs` function of the **FC-TOOLS** package. The array P , is obtained with `P=fc_tools.graphics.PlaneCoefs(Q,V)` where Q is a point in the plane and V is a vector orthogonal to it. One can also used a n -by-4 array P where each line define a plane.

`slice(q,me,u,P,Name,Value, ...)` specifies function options using one or more `Name,Value` pair arguments which are those of the **patch** function excepts `'FaceColor'` and `'EdgeColor'`.

3D example



9

SLICEISO function

The **SLICEISO** function displays isolines of datas on the intersection of a plane and a 3D mesh given by its vertices array q and its connectivity array me .

Syntaxe

```
fc_graphics4mesh.sliceiso(q,me,u,P)
fc_graphics4mesh.sliceiso(q,me,u,P,Name,Value, ...)
```

Description

`sliceiso(q,me,u,P)` displays isolines of data u on the intersection of the plane defined by $P(1)x + P(2)y + P(3)z + P(4) = 0$ and all the 3-dimensional simplices elements given by q and me arrays. To compute P one can use the `fc_tools.graphics.PlaneCoefs` function of the **FC-TOOLS** package. The 1-by-4 array P , is obtained with $P=fc_tools.graphics.PlaneCoefs(Q,V)$ where Q is a point in the plane and V is a vector orthogonal to it. One can also used a n -by-4 array P where each line define a plane.

`sliceiso(q,me,u,P,Name,Value, ...)` allows additional key/value pairs to be used when displaying u . The key strings could be

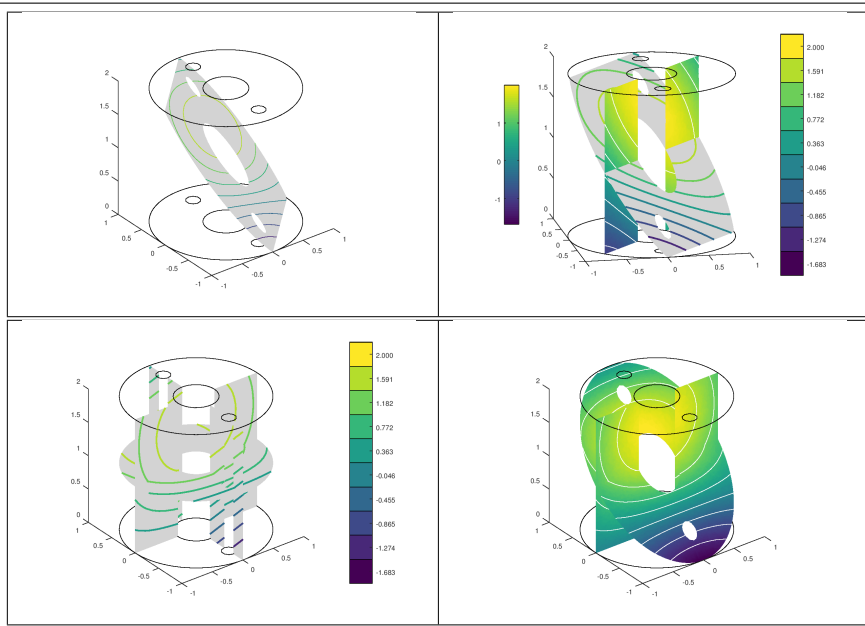
- **'niso'** : to specify the number of isolines (default : 10)
- **'isorange'** : to specify the list of isovalues (default : empty)
- **'color'** : to specify one color for all isolines (default : empty)
- **'isocolorbar'** : if true display a colorbar.Default is false.
- **'format'** : to specify the format of the isovalues print in the colorbar. Default is **'%g'**.

For key strings, one could also used any options of the `plot3` function.

This function accepts until 4 output arguments :

- 1st output is the colors of the isolines
- 2nd output is the isovalues of the isolines
- 3th output is the handle of the colobar iso.
- 4th output is all the handles of the isolines as an 2D-array of dimension N -by- $niso$, where N is the number of elementary meshes where isolines are drawn.

3D example



```

u=@(x,y,z) 2*cos(x).*sin(y+z);
[q3,me3,toGlobal3]=fc_graphics4mesh.getMeshArrays('3D',3);
U3=fc_graphics4mesh.evalAtVertices(u,q3);
[q1,me1,toGlobal1]=fc_graphics4mesh.getMeshArrays('3D',1);
figure(1)
P=fc_tools.graphics.PlaneCoefs([0 0 1],[1 -1 1]);
fc_graphics4mesh.slicemesh(q3,me3,P)
hold on;axis equal;axis image
fc_graphics4mesh.plotmesh(q1,me1,'color','k')
fc_graphics4mesh.sliceiso(q3,me3,U3,P)
figure(2)
fc_graphics4mesh.slicemesh(q3,me3,P)
hold on;axis equal;axis image
fc_graphics4mesh.plotmesh(q1,me1,'color','k')
fc_graphics4mesh.sliceiso(q3,me3,U3,P,'Linewidth',2, ...
    'isocolorbar',true,'format','%3f');
P=fc_tools.graphics.PlaneCoefs([0 0 1],[1 -1 0]);
fc_graphics4mesh.slice(q3,me3,U3,P)
fc_graphics4mesh.sliceiso(q3,me3,U3,P,'color','w');
colorbar('Location','westoutside')
caxis([min(U3),max(U3)]);view(-11,15)
figure(3)
P=[fc_tools.graphics.PlaneCoefs([0 0 1],[1 0 0]); ...
    fc_tools.graphics.PlaneCoefs([0 0 1],[0 1 0]); ...
    fc_tools.graphics.PlaneCoefs([0 0 1],[0 0 1])];
fc_graphics4mesh.slicemesh(q3,me3,P)
hold on;axis equal;axis image
fc_graphics4mesh.plotmesh(q1,me1,'color','k')
fc_graphics4mesh.sliceiso(q3,me3,U3,P,'LineWidth',2, ...
    'isocolorbar',true,'format','%3f');
figure(4)
P=[fc_tools.graphics.PlaneCoefs([0 0 1],[0 1 0]); ...
    fc_tools.graphics.PlaneCoefs([0 0 1],[0 -1 1])];
fc_graphics4mesh.slice(q3,me3,U3,P)
hold on;axis equal;axis image
fc_graphics4mesh.plotmesh(q1,me1,'color','k')
fc_graphics4mesh.sliceiso(q3,me3,U3,P,'Color','w');

```

Listing 12: 3D mesh : sliceiso function

The function **PLOTQUIVER** displays vector field datas on a mesh given by its vertices array `q` and its connectivity array `me`.

Syntax

```
fc_graphics4mesh.plotquiver(q,me,V)
fc_graphics4mesh.plotquiver(q,me,V,Name,Value, ...)
```

Description

`plotquiver(q,me,V)` displays vector field `u` on a simplicial mesh. The vector field data `u` can be a 1-by-dim cell arrays of handle functions or an dim-by- n_q array.

`plotquiver(q,me,V,Name,Value, ...)` specifies function options using one or more Name,Value pair arguments. Options of first level are

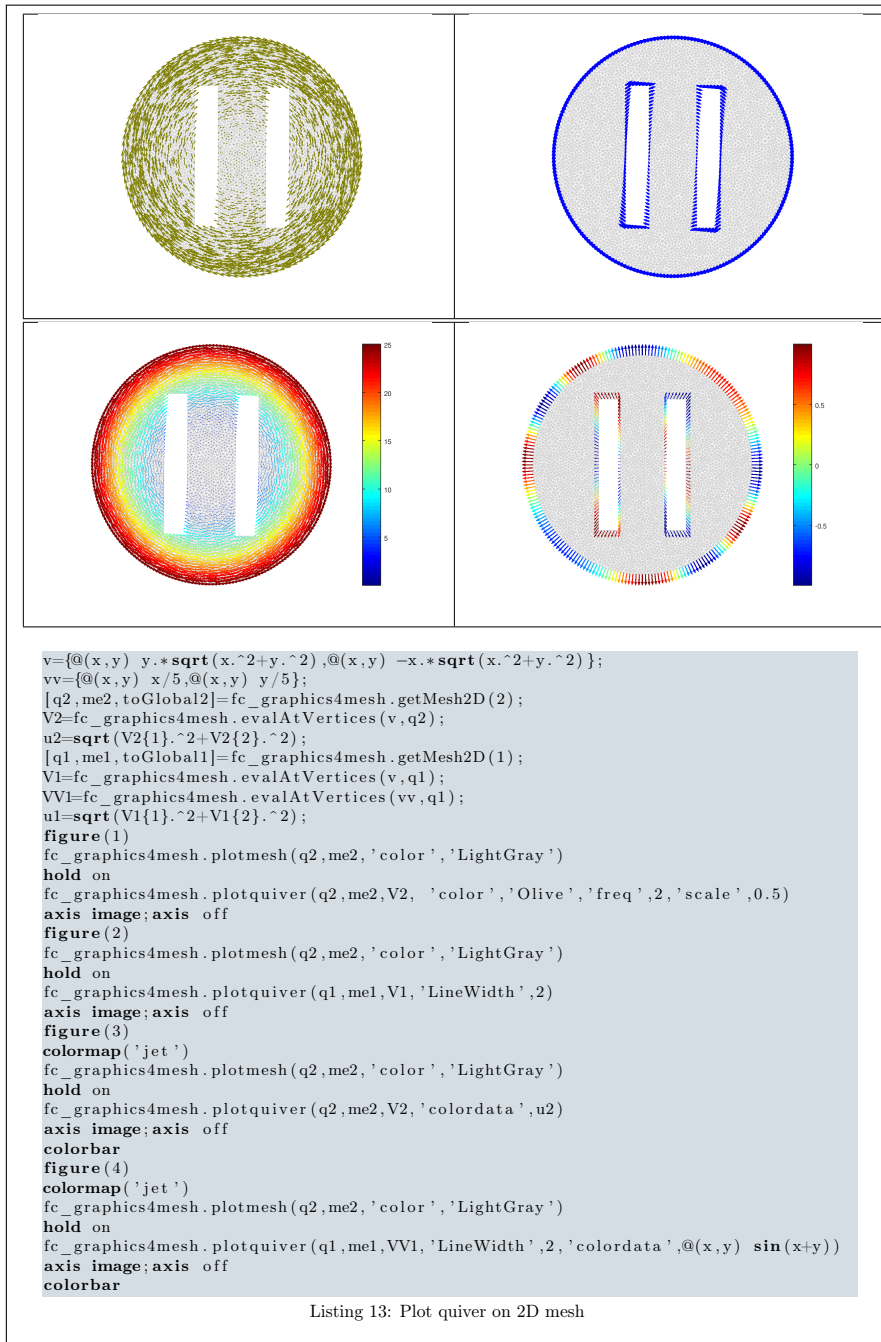
- **'freq'** : quiver frequency, (default : 1)
- **'scale'** : quiver scale, (default is `fc_graphics4mesh.getCharacteristicLength(q)/20`)
- **'color'** : set one color for all quivers (default: default color of the **quiver** or **quiver3** functions). Cannot be used with **'colordata'** option.
- **'colordata'** : each quiver is colored with a 1-by- n_q array or a handle function (it will be evaluated in all vertices) (default : empty).

The options of second level depend on the type of mesh elements to represent.

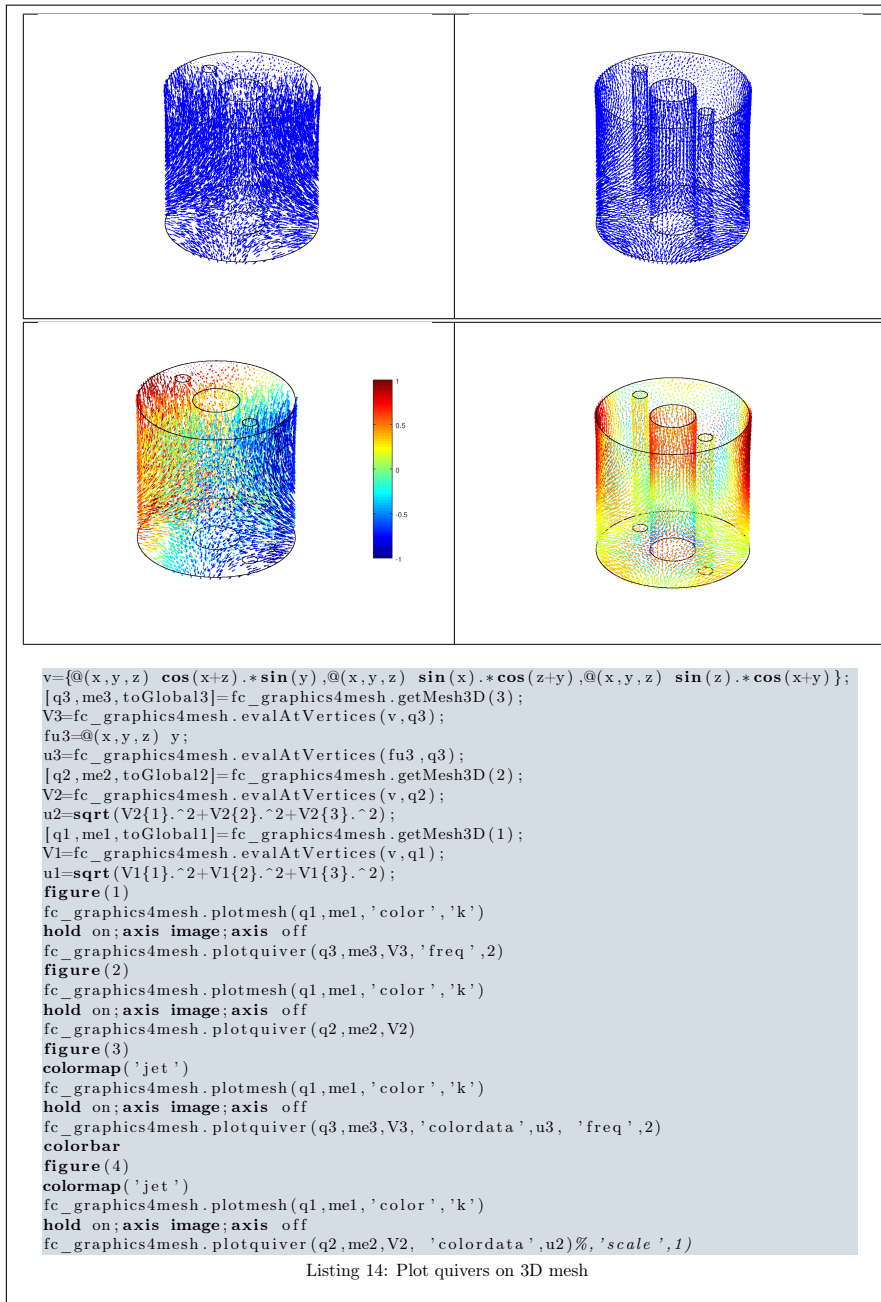
One can use any option of the following functions according to the type of d -simplex to be represented.

- In dimension 3 and with empty **'colordata'**, the **quiver3** function is used.
- In dimension 2 and with empty **'colordata'**, the **quiver** function is used.
- In dimension 2 or 3 and with no empty **'colordata'**, the third party `fc_tools.graphics.vfield3.vfield3` function is used.

2D example



3D example



3D surface example

