



# FC-HYPERMESH Octave package, User's Guide <sup>\*</sup> under rhum-ubuntu-16-04-3lts computer

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## Abstract

This object-oriented Octave package allows to mesh any d-orthotopes (hyperrectangle in dimension d) and their m-faces by simplices or orthotopes. It was created to show the implementation of the vectorized algorithms presented in [1]. The FC-HYPERMESH package uses Octave objects and is provided with meshes visualisation tools for dimension less than or equal to 3.

## 0 Contents

<b>1</b>	<b>Introduction</b>	<b>2</b>
<b>2</b>	<b>Installation</b>	<b>2</b>
2.1	Installation via pkg command (recommended)	2
2.2	All-in-one installation	3
<b>3</b>	<b>Using the FC-HYPERMESH package</b>	<b>4</b>
3.1	Class object <code>OrthMesh</code>	4
3.1.1	Constructor	5
3.1.2	plotmesh method	5
3.2	2d-orthotope meshing by simplices	5
3.3	3d-orthotope meshing by simplices	6

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<sup>\*</sup>Compiled with Octave 4.2.1

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3.4	2d-orthotope meshing by orthotopes . . . . .	8
3.5	3d-orthotope meshing by orthotopes . . . . .	8
3.6	Mapping of a 2d-orthotope meshing by simplices . . . . .	10
3.7	3d-orthotope meshing by orthotopes . . . . .	11

## 1 Introduction

The FC-HYPERMESH package contains a simple class object `OrthMesh` which permits, in any dimension  $d \geq 1$ , to obtain a simplicial mesh or orthotope mesh with all their  $m$ -faces,  $0 \leq m < d$ . It is also possible with the method function `plotmesh` of the class object `OrthMesh` to represent a mesh or its  $m$ -faces for  $d \leq 3$ .

This package was tested under

**Windows 10.0.16299:** with Octave 4.2.0 and 4.2.1

**Mac OS X 10.12.6:** with Octave 4.2.1 (installed with homebrew)

**Ubuntu 14.04.5 LTS:** with Octave 4.2.0 and 4.2.1 (both compiled from source)

**Ubuntu 16.04.3 LTS:** with Octave 4.2.0 and 4.2.1 (both compiled from source)

**Ubuntu 17.10:** with Octave 4.2.0 and 4.2.1 (both compiled from source)

**Fedora 27:** with Octave 4.2.0 and 4.2.1 (both compiled from source)

It is not compatible with Octave 4.0.x and previous.

In the following section, the class object `OrthMesh` is presented. Thereafter some warning statements on the memory used by these objects in high dimension are given. Finally computation times for orthotope meshes and simplicial meshes are given in dimension  $d \in \llbracket 1, 5 \rrbracket$ .

## 2 Installation

### 2.1 Installation via pkg command (recommended)

- Download the packages. For example, in a terminal:

```
# wget http://www.math.univ-paris13.fr/~cuvelier/software/codes/
#   octave/fc-tools/0.0.20/fc-tools-0.0.20.tar.gz
# wget http://www.math.univ-paris13.fr/~cuvelier/software/codes/
#   octave/fc-hypermesh/0.0.7/fc-hypermesh-0.0.7.tar.gz
```

- Under Octave :

```
>> pkg install fc-tools-0.0.20.tar.gz
>> pkg install fc-hypermesh-0.0.7.tar.gz
```

- Now to use `fc-hypermesh` in any Octave session, it is necessary to load the package:

```
>> pkg load fc-hypermesh
```

- To try the package, one can launch a demo:

```
>> fc_hypermesh.demo01
```

For uninstalling the package, just do in an Octave session:

```
>> pkg uninstall fc-hypermesh  
>> pkg uninstall fc-tools
```

## 2.2 All-in-one installation

For this method, one just has to get/download the install file

`ofc_hypermesh_install.m`

or get it on the dedicated web page. Thereafter, it should be run under Octave. This command downloads, extracts and configures the *fc-hypermesh* and the required *fc-tools* packages in the current directory.

For example, to install this package in directory `~/Octave/packages`, in a terminal one can do:

```
# mkdir -p ~/Octave/packages  
# cd ~/Octave/packages  
# wget http://www.math.univ-paris13.fr/~cuvelier/software/codes/Octave/fc-  
-hypermesh/0.0.7/ofc_hypermesh_install.m
```

Then in a Octave terminal run the following commands

```
>> cd ~/Octave/toolboxes  
>> ofc_hypermesh_install
```

This is the output of the `ofc_hypermesh_install` command:

```
1- Downloading and extracting the packages  
-> <fc-tools>[0.0.20] ... OK  
-> <fc-hypermesh>[0.0.7] ... OK  
2- Setting the <fc-hypermesh> package  
Write in ~/Octave/toolboxes/fc-hypermesh-full/fc_hypermesh-0.0.7/  
    configure_loc.m ...  
-> done  
3- Using the <fc-hypermesh> package  
Under Octave:  
    addpath('~/Octave/toolboxes/./fc-hypermesh-full/fc_hypermesh-0.0.7')  
    fc_hypermesh.init()  
  
See ~/Octave/toolboxes/ofc_hypermesh_set.m
```

The complete package (i.e. with all the other needed packages) is stored in the directory `~/Octave/packages/fc-hypermesh-full` and, for each Octave session, one has to set the package by:

```
>> addpath('~/Octave/packages/fc-hypermesh-full/ofc-hypermesh-0.0.7')  
>> fc_hypermesh.init()
```

To **uninstall**, one just has to delete directory `~/Octave/packages/fc-hypermesh-full`

## 3 Using the fc-hypermesh package

First of all, the main class object `OrthMesh` is presented. Thereafter some usage samples are given.

### 3.1 Class object `OrthMesh`

The aim of the class object `OrthMesh` is to efficiently create an object which contains a mesh of a  $d$ -orthotope and all its  $m$ -face meshes. An elementary mesh class object `EltMesh` is used to store only one mesh, the main mesh as well as any of the  $m$ -face meshes. This class `EltMesh` also simplifies (for me) the codes writing. Its fields are the following:

- $d$ , space dimension
- $m$ , kind of mesh ( $m = d$  for the main mesh)
- type, 0 for simplicial mesh or 1 for orthotope mesh
- $n_q$ , number of vertices
- $q$ , vertices array of dimension  $d$ -by- $n_q$
- $n_{me}$ , number of mesh elements
- $me$ , connectivity array of dimension  $(d + 1)$ -by- $n_{me}$  for simplices elements or  $2^d$ -by- $n_{me}$  for orthotopes elements
- `toGlobal`, index array linking local array  $q$  to the one of the main mesh
- label, name/number of this elementary mesh
- color, color of this elementary mesh (for plotting purpose)

Let the  $d$ -orthotope defined by  $[a_1, b_1] \times \dots \times [a_d, b_d]$ . The class object `OrthMesh` corresponding to this  $d$ -orthotope contains the main mesh and all its  $m$ -face meshes,  $0 \leq m < d$ . Its Fields are the following

- $d$ : space dimension
- type: string 'simplicial' or 'orthotope' mesh
- Mesh: main mesh as an `EltMesh` object
- Faces: list of arrays of `EltMesh` objects such that `Faces(1)` is an array of all the  $(d - 1)$ -face meshes, `Faces(2)` is an array of all the  $(d - 2)$ -face meshes, and so on
- box: a  $d$ -by-2 array such that  $\text{box}(i, 1) = a_i$  and  $\text{box}(i, 2) = b_i$ .

## Constructor

The `OrthMesh` constructor is :

$$Oh = \text{OrthMesh}(d, N)$$

where  $N$  is either a 1-by- $d$  array/list such that  $N[i-1]$  is the number of discretization for  $[a_i, b_i]$  or either an integer if the the number of discretization is the same in all space directions.

Some options are proposed with the constructor:

$$Oh = \text{OrthMesh}(d, N, \text{Name}, \text{Value})$$

Options are defined with one or more `Name, Value` pair arguments. The `Name` argument could be the string

- `'box'` : used to specify the  $d$ -orthotope  $[a_1, b_1] \times \dots \times [a_d, b_d]$  by setting `Value` as an  $d$ -by-2 array such that  $a_i = \text{Value}(i, 1)$  and  $b_i = \text{Value}(i, 2)$ .
- `'type'` : used to select the kind of elements used for meshing. The default value is `'simplicial'` and otherwise `'orthotope'` can be used.

## plotmesh method

The `plotmesh()` member function can be used to represent the mesh given by an `OrthMesh` object if the space dimension is less than or equal to 3. Some options are proposed with this function:

$$\text{plotmesh}(\text{Name}, \text{Value})$$

- `'legend_=_value'` : if `value` is `True`, a legend is displayed. Default is `False`.
- `m = value` : plots all the  $m$ -faces of the mesh. Default  $m = d$  i.e. the main mesh. ( $0 \leq m \leq d$ )
- ...

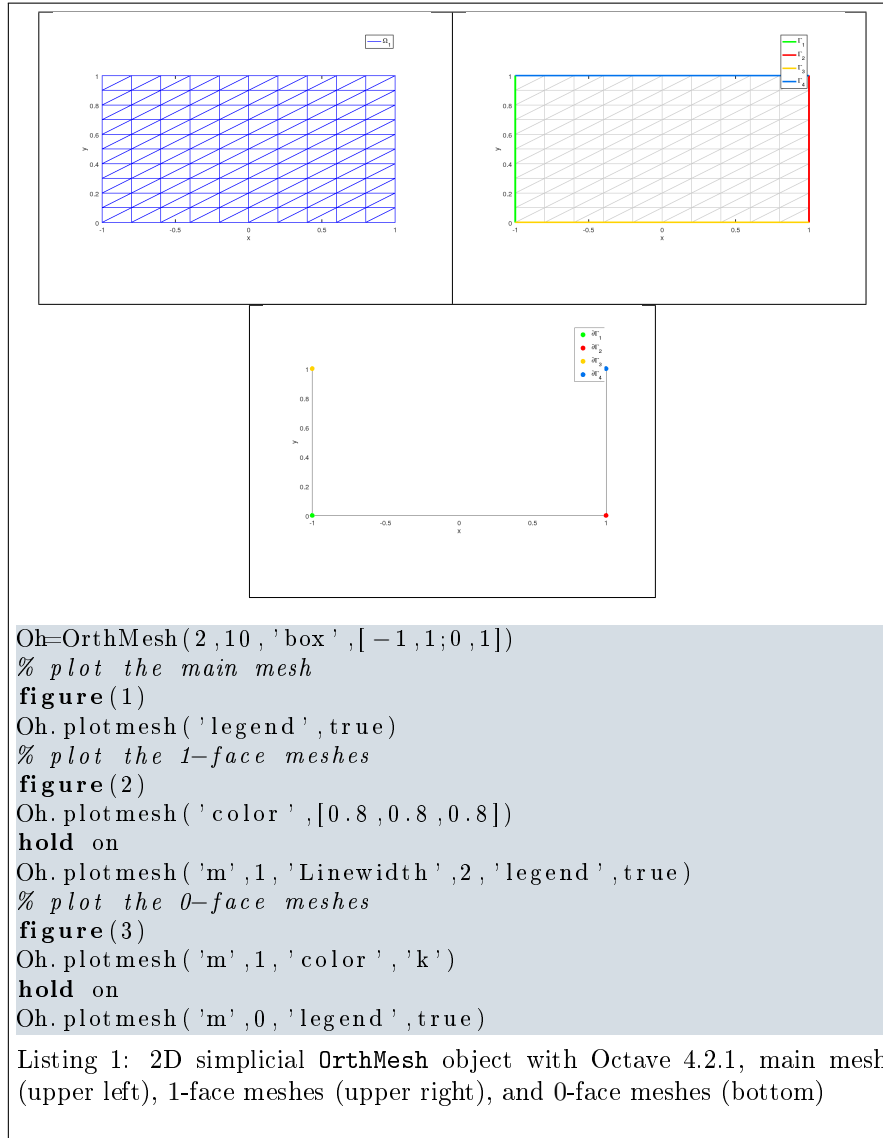
### 3.2

### 2d-orthotope meshing by simplices

In Listing 15, an `OrthMesh` object is built under Octave by using command

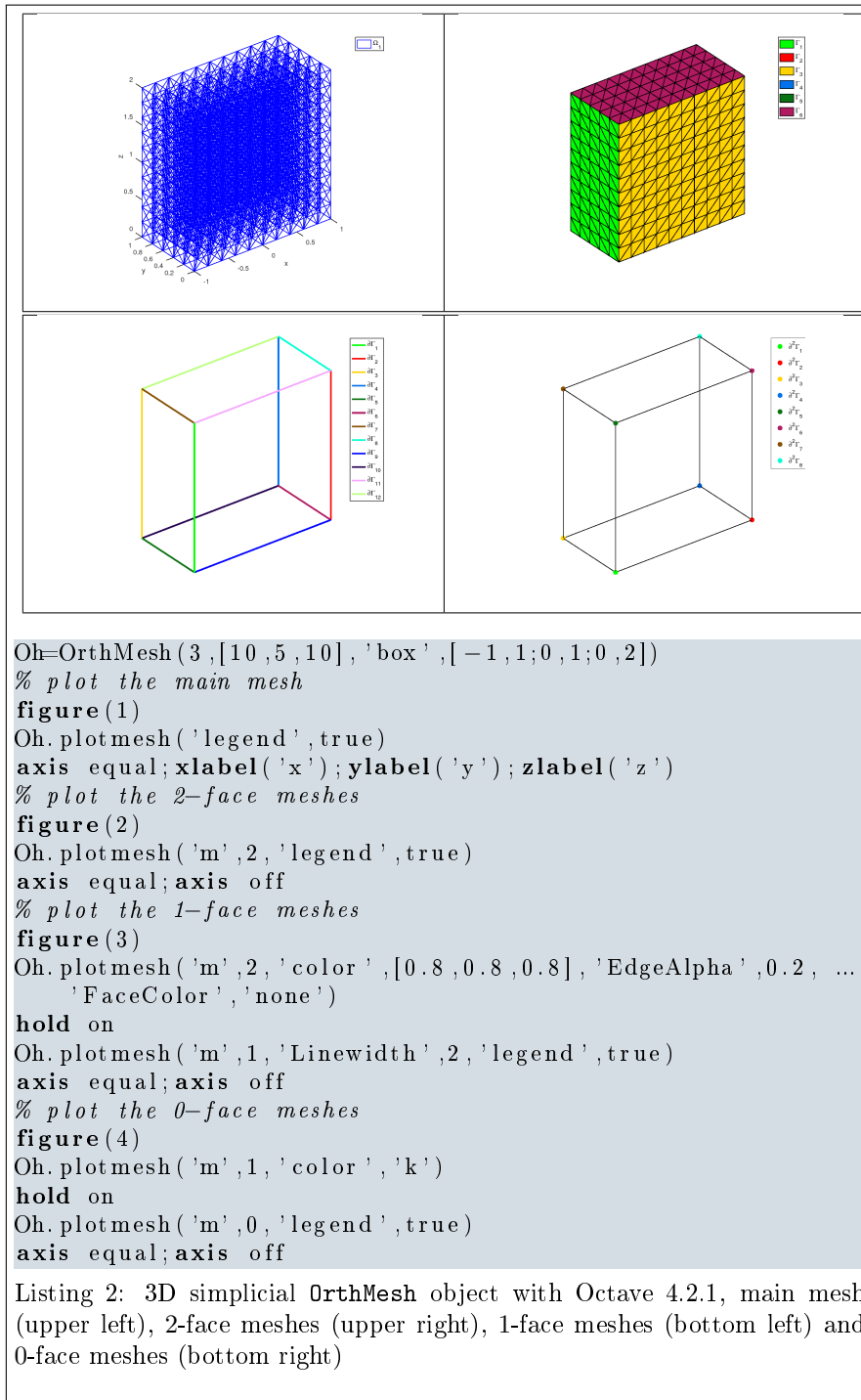
```
Oh=OrthMesh(2,10,'box',[-1,1;0,1])
```

So the `Oh` object is the tessellations of the orthotope  $[-1, 1] \times [0, 1]$  with simplicial elements. In each direction  $10 + 1 (= 11!)$  points are taken. So we have  $11^2$  vertices in this mesh. The main mesh and all the  $m$ -face meshes of the resulting object are plotted by using `plotmesh` method.



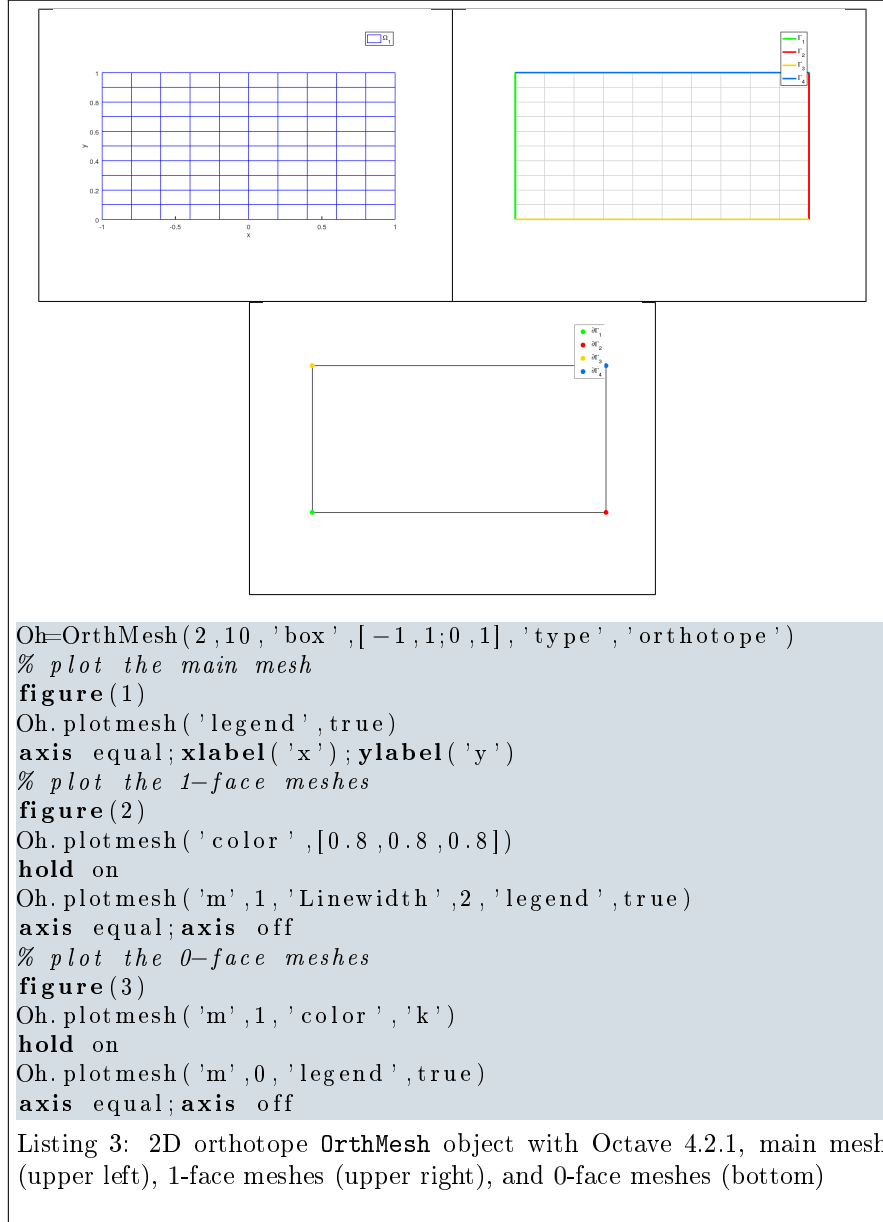
### 3.3 3d-orthotope meshing by simplices

In Listing 22, an `OrthMesh` object is built under Octave for the orthotope  $[-1,1] \times [0,1] \times [0,2]$  with simplicial elements and  $\mathbf{N} = (10,5,10)$ . The main mesh and all the  $m$ -face meshes of the resulting object are plotted.



### 3.4 2d-orthotope meshing by orthotopes

In Listing 22, an `OrthMesh` object is built under Octave for the orthotope  $[-1, 1] \times [0, 1] \times [0, 2]$  with orthotope elements and  $\mathbf{N} = (10, 5, 10)$ . The main mesh and all the  $m$ -face meshes of the resulting object are plotted.

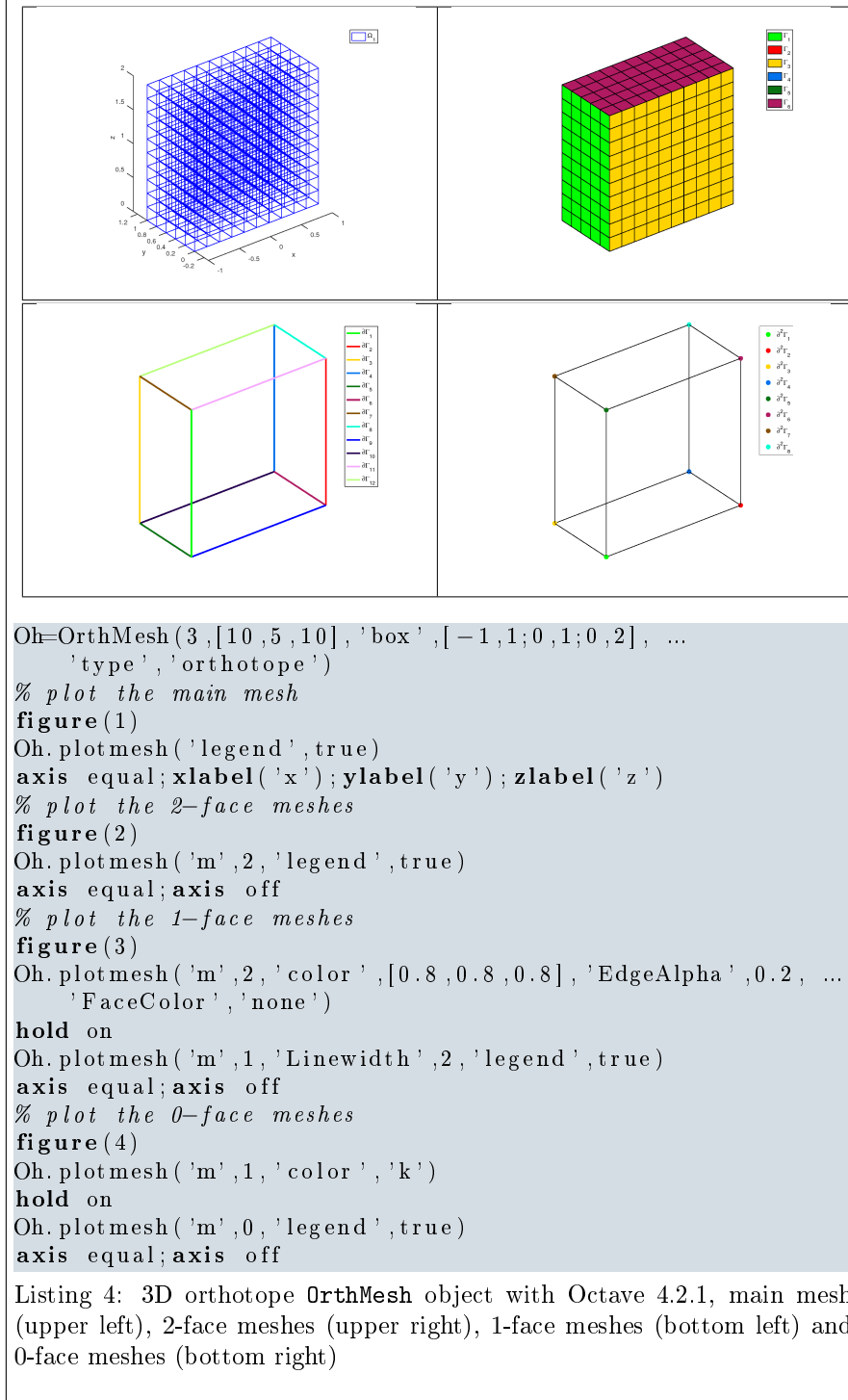


### 3.5 3d-orthotope meshing by orthotopes

In Listing 22, an `OrthMesh` object is built under Octave for the orthotope  $[-1, 1] \times [0, 1] \times [0, 2]$  with orthotope elements and  $\mathbf{N} = (10, 5, 10)$ . The main



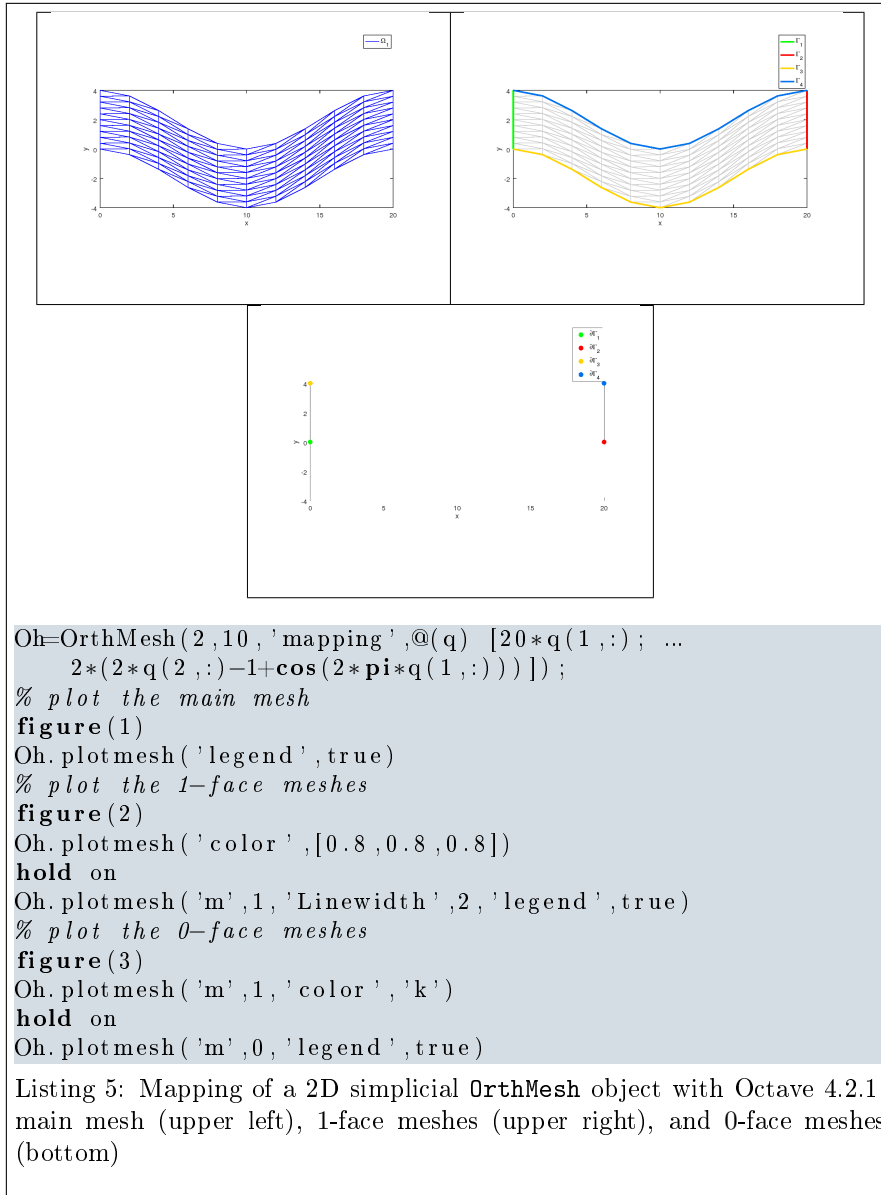
mesh and all the  $m$ -face meshes of the resulting object are plotted.



For example, the following 2D geometrical transformation allows to deform the reference unit hypercube.

$$[0, 1] \times [0, 1] \longrightarrow \mathbb{R}^2$$

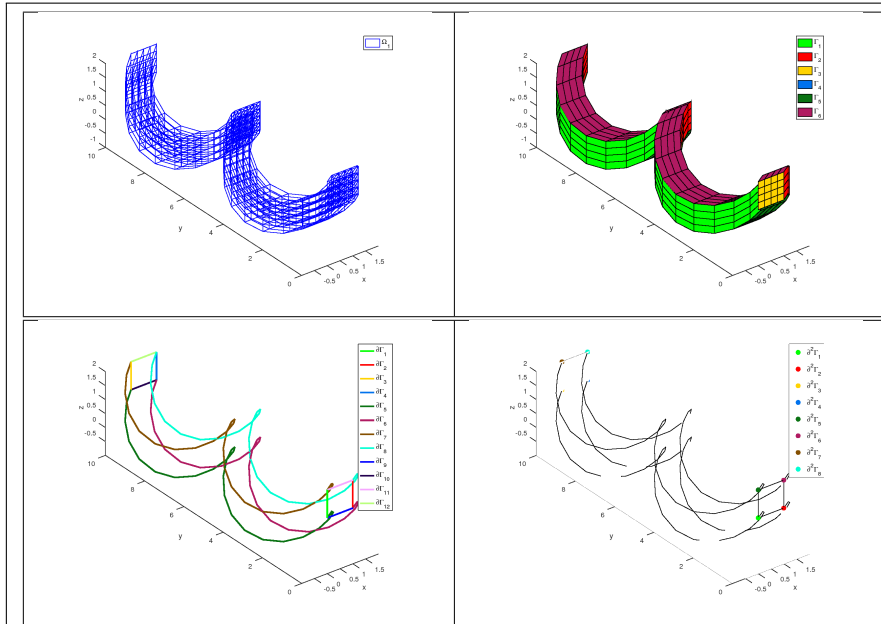
$$\begin{pmatrix} x \\ y \end{pmatrix} \longrightarrow F(x, y) = \begin{pmatrix} 20x \\ 2(2y - 1 + \cos(2\pi x)) \end{pmatrix}$$



For example, the following 3D geometrical transformation allows to deform the reference unit hypercube.

$$[0, 1] \times [0, 1] \times [0, 1] \longrightarrow \mathbb{R}^3$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} \longrightarrow F(x, y, z) = \begin{pmatrix} x + \sin(4\pi y) \\ 10y \\ z + \cos(4\pi y) \end{pmatrix}$$



```

Map=@(q) [q(1,:)+ sin(4*pi*q(2,:)); 10*q(2,:); ...
          q(3,:)+cos(4*pi*q(2,:))];
Oh=OrthMesh(3,[4,25,4], 'mapping',Map, 'type', 'orthotope');
% plot the main mesh
figure(1)
Oh.plotmesh()
legend('show')
% plot the 2-face meshes
figure(2)
Oh.plotmesh('m',2)
legend('show')
% plot the 1-face meshes
figure(3)
Oh.plotmesh('m',2, 'color',[0.8,0.8,0.8], 'EdgeAlpha',0.2, ...
           'FaceColor','none')
hold on
Oh.plotmesh('m',1, 'Linewidth',2, 'legend',true)
% plot the 0-face meshes
figure(4)
Oh.plotmesh('m',1, 'color','k')
hold on
Oh.plotmesh('m',0, 'legend',true)

```

Listing 6: Mapping of a 3D orthotope `OrthMesh` object with Octave 4.2.1, main mesh (upper left), 2-face meshes (upper right), 1-face meshes (bottom left) and 0-face meshes (bottom right)