



# **simesh** Octave package, User's Guide<sup>\*</sup>

version 0.4.0

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## Abstract

This object-oriented Octave package allows to use simplicial meshes generated from `gmsh` (in dimension 2 or 3) or an hypercube triangulation (in any dimension). For graphical representation the `csiplt` package is used.

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<sup>\*</sup>LATEX manual, revision 0.4.0.a, compiled with Octave 5.2.0, and packages `fc-simesh[0.4.0]`, `fc-tools[0.0.30]`, `fc-bench[0.1.2]`, `fc-hypermesh[1.0.3]`, `fc-amat[0.1.2]`, `fc-meshtools[0.1.3]`, `fc-graphics4mesh[0.1.1]`, `fc-oogmsh[0.2.2]`, `fc-siplt[0.2.0]`

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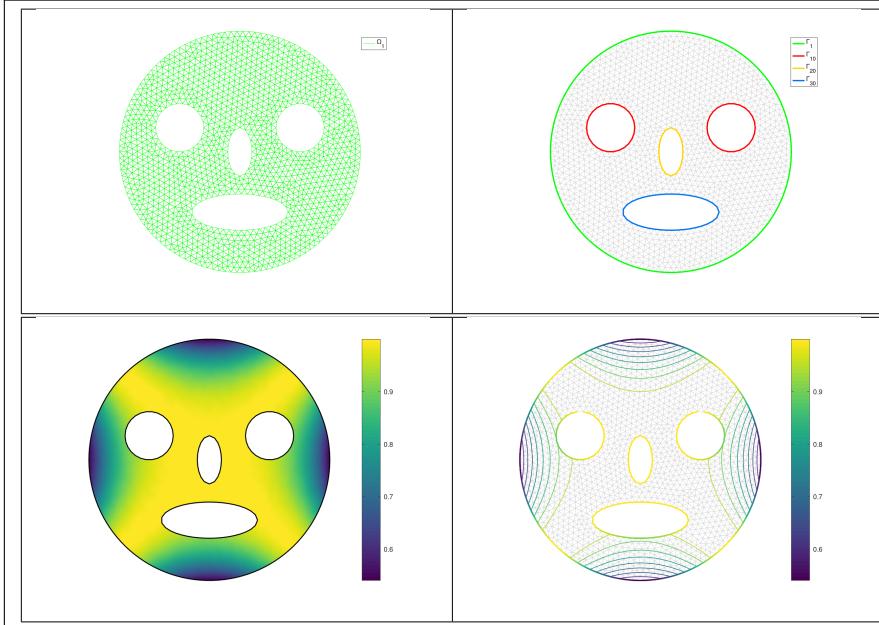
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## 1 Introduction

---

The `fc_simesh` Octave package was created to simplify the use of simplicial meshes and to easily represent data on all or parts of them. In 2D or 3D `gmsh` can be used under Octave to build triangular or tetrahedral meshes by using the `Coogmsh` package[1]. Thereafter the mesh stored as a file (.msh) can be read by using the `fc_simesh.siMesh` object. In Listing 1, a 2D example is provided with the 4 generated figures. For graphic representations, the `fc_siplt` package[2] is used by the `fc_simesh.siMesh` object `Th` as follows `Th.plotmesh(...)` is `fc_siplt.plotmesh(Th,...)`, `Th.plot(...)` is `fc_siplt.plot(Th,...)` and so on.



```

close all
geofile=fc_simesh.get_geo(2,2,'sample2D01.geo');
% Using GMSH >= 4.0.0 to create mesh file
meshfile=fc_oogmsh.gmsh.buildmesh2d(geofile,200,'force',true);
% Creating siMesh object by reading the mesh file
Th=fc_simesh.siMesh(meshfile);
% Computing datas on siMesh object
u=@(x,y) cos(x.^2-y.^2);
U=Th.eval(u);
% Graphics
figure(1)
Th.plotmesh('inlegend',true)
axis image; axis off
legend()

figure(2)
Th.plotmesh('color','LightGray')
hold on
Th.plotmesh('d',1,'inlegend',true,'LineWidth',2)
axis image; axis off
legend()

figure(3)
Th.plot(U,'plane',true)
colorbar
shading interp
axis image; axis off
hold on
Th.plotmesh('d',1,'LineWidth',1.5,'color','k')

figure(4)
Th.plotmesh('color','LightGray')
axis image; axis off
hold on
Th.plot(U,'d',1,'LineWidth',2,'plane',true)
colorbar
Th.plotiso(U,'niso',10,'LineWidth',1,'plane',true)

```

Listing 1: `fc_simesh.demos.sample2D01` script with figure 1 (top left), figure 2 (top right), figure 3 (bottom left) and figure 4 (bottom right).

In higher dimension the `fc_hypermesh` package[3] can be used to obtain meshes of an hypercube by using the `fc_simesh.HyperCube` function.

## 2 Installation

This package was tested on various OS with Octave releases:

Operating system	4.4.0	4.4.1	5.1.0	5.2.0
CentOS 7.7.1908	✓	✓	✓	✓
Debian 9.11	✓	✓	✓	✓
Fedora 29	✓	✓	✓	✓
OpenSUSE Leap 15.0	✓	✓	✓	✓
Ubuntu 18.04.3 LTS	✓	✓	✓	✓
MacOS High Sierra 10.13.6		✓	✓	✓
MacOS Mojave 10.14.4		✓	✓	✓
MacOS Catalina 10.15.2		✓	✓	✓
Windows 10 (1909)	✓	✓	✓	✓

It is not compatible with Octave releases prior to 4.2.0. Here are the links used to install the Octave releases tested:

- **Linux** : sources from <https://www.gnu.org/software/octave/>;
- **MacOS** : release 4.4.1 installed with dmg file from <http://octave-app.org/Download.html>, releases 5.1.0 and 5.2.0 installed with Homebrew;
- **Windows** : binaries from <https://www.gnu.org/software/octave/>.

### 2.1 Installation automatic, all in one (recommended)

For this method, one just have to get/download the install file

`ofc_simesh_install.m`

or get it on the dedicated web page. Thereafter, one run it under Octave. This command download, extract and configure the *fc-simesh* and the required packages (*fc-tools*, *fc-oogmsh*, *fc-hypermesh*) in the current directory.

For example, to install this package in `~/Octave/packages` directory, one have to copy the file `mfc_simesh_install.m` in the `~/Octave/packages` directory. Then in a Octave terminal run the following commands to install the *fc-simesh* package with graphical extension

```
>> cd ~/Octave/packages  
>> mfc_simesh_install
```

There is the output of the `mfc_simesh_install` command on a Linux computer:

```

Parts of the <fc-simesh> Octave package.
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1- Downloading and extracting the packages
2- Setting the <fc-simesh> package
Write in ...
    ~/Matlab/toolboxes/fc-simesh-full/fc_simesh-0.4.0/configure_loc.m ...
3- Using packages :
    ->          fc-tools : 0.0.30
    ->          fc-bench : 0.1.2
    ->          fc-hypermesh : 1.0.3
    ->          fcamat : 0.1.2
    ->          fc-meshtools : 0.1.3
    ->          fc-graphics4mesh : 0.1.1
    ->          fc-oogmsh : 0.2.2
    ->          fc-siptl : 0.2.0
with          fc-simesh : 0.4.0
*** Using instructions
To use the <fc-simesh> package:
addpath('~/Matlab/toolboxes/fc-simesh-full/fc_simesh-0.4.0')
fc_simesh.init()

See ~/Matlab/toolboxes/ofc_simesh_set.m

```

The complete package (i.e. with all the other needed packages) is stored in the directory `~/Octave/packages/fc-simesh-full` and, for each Octave session, one have to set the package by:

```

>> addpath('~/Octave/packages/fc-simesh-full/fc_simesh-0.4.0')
>> fc_simesh.init()

```

If it's the first time the `fc_simesh.init()` function is used, then its output is

```

Try to use default parameters!
  Use fc_tools.configure to configure.
Write in ...
  ~/Matlab/toolboxes/fc-simesh-full/fc_tools-0.0.30/configure_loc.m ...
Try to use default parameters!
  Use fc_bench.configure to configure.
Write in ...
  ~/Matlab/toolboxes/fc-simesh-full/fc_bench-0.1.2/configure_loc.m ...
Try to use default parameters!
  Use fc_hypermesh.configure to configure.
Write in ...
  ~/Matlab/toolboxes/fc-simesh-full/fc_hypermesh-1.0.3/configure_loc.m ...
...
Try to use default parameters!
  Use fc_amat.configure to configure.
Write in ...
  ~/Matlab/toolboxes/fc-simesh-full/fc_amat-0.1.2/configure_loc.m ...
Try to use default parameters!
  Use fc_meshtools.configure to configure.
Write in ...
  ~/Matlab/toolboxes/fc-simesh-full/fc_meshtools-0.1.3/configure_loc.m ...
...
Try to use default parameters!
  Use fc_graphics4mesh.configure to configure.
Write in ...
  ~/Matlab/toolboxes/fc-simesh-full/fc_graphics4mesh-0.1.1/configure_loc.m ...
...
Try to use default parameters!
  Use fc_oogmsh.configure to configure.
Write in ...
  ~/Matlab/toolboxes/fc-simesh-full/fc_oogmsh-0.2.2/configure_loc.m ...
Configured to use gmsh 4.5.1 with default MSH file format version 4.1
Try to use default parameters!
  Use fc_siplt.configure to configure.
Write in ...
  ~/Matlab/toolboxes/fc-simesh-full/fc_siplt-0.2.0/configure_loc.m ...
Using fc_simesh[0.4.0] with fc_tools[0.0.30], fc_bench[0.1.2], ...
  fc_hypermesh[1.0.3],
  fc_amat[0.1.2], fc_meshtools[0.1.3], fc_graphics4mesh[0.1.1], ...
  fc_oogmsh[0.2.2], fc_siplt[0.2.0].

```

Otherwise, the output of the `fc_simesh.init()` function is

```

Configured to use gmsh 4.5.1 with default MSH file format version 4.1
Using fc_simesh[0.4.0] with fc_tools[0.0.30], fc_bench[0.1.2], ...
  fc_hypermesh[1.0.3],
  fc_amat[0.1.2], fc_meshtools[0.1.3], fc_graphics4mesh[0.1.1], ...
  fc_oogmsh[0.2.2], fc_siplt[0.2.0].

```

For **uninstalling**, one just have to delete directory

```
~/Octave/packages/fc-simesh-full
```

### 2.1.1 Mesh Objects

In geometry, a simplex is a generalization of the notion of a triangle or tetrahedron to arbitrary dimensions. Specifically, a  $k$ -simplex in  $\mathbb{R}^{\dim}$ ,  $0 \leq k \leq \dim$ , is a polytope which is the convex hull of its  $k+1$  vertices of  $\mathbb{R}^{\dim}$ . More formally, suppose the  $k+1$  vertices  $q^0, \dots, q^k \in \mathbb{R}^{\dim}$  such that  $q^1 - q^0, \dots, q^k - q^0$  are linearly independent. Then, the  $k$ -simplex  $K$  determined by them is the set of points

$$K = \left\{ \sum_{i=0}^k \lambda_i q^i \mid \lambda_i \geq 0, i \in \llbracket 0, k \rrbracket, \text{ with } \sum_{i=0}^k \lambda_i = 1 \right\}.$$

We denote by  **$k$ -simplicial elementary mesh** in  $\mathbb{R}^{\text{dim}}$ ,  $0 \leq k \leq \text{dim}$ , a mesh with **unique label** only composed with  $k$ -simplices.

A  **$d$ -simplicial mesh** in  $\mathbb{R}^{\text{dim}}$ ,  $0 \leq d \leq \text{dim}$ , is an union of  $k$ -simplicial elementary meshes with  $k \in [0, d]$ .

## 2.2 fc\_simesh.siMeshElt object

---

An elementary  $d$ -simplicial mesh in dimension  $\text{dim}$  is represented by the class **fc\_simesh.siMeshElt**. We give properties of this class :

## Properties of `fc_simesh.siMeshElt` object for $d$ -simplicial elementary meshes in $\mathbb{R}^{\text{dim}}$

<code>dim</code>	: integer space dimension
<code>d</code>	: integer ( $0 \leq d \leq \text{dim}$ )
<code>nq</code>	: integer number of vertices
<code>nme</code>	: integer number of elements ( $d$ -simplices)
<code>q</code>	: $\text{dim}$ -by- <code>nq</code> array of reals array of vertex coordinates
<code>me</code>	: ( $d + 1$ )-by- <code>nme</code> array of integers connectivity array for <b>mesh elements</b>
<code>vols</code>	: 1-by- <code>nme</code> array of reals array of mesh element volumes
<code>h</code>	: double mesh step size (=maximum edge length in the mesh)
<code>toGlobal</code>	: 1-by- <code>nq</code> array of integers convert from local to global mesh vertices numbering. Prefer the use of <code>toParents{end}</code> instead. <i>It will be removed in a future release.</i>
<code>toParent</code>	: 1-by- <code>nq</code> array of integers convert from local to parent mesh vertices numbering (same as <code>toGlobal</code> if not part of a partitioned mesh). Prefer the use of <code>toParents{1}</code> instead. <i>It will be removed in a future release.</i>
<code>nqParents</code>	: 1-by- $n$ array of integers <code>nqParents{1}</code> number of vertices in the <i>parent</i> mesh, <code>nqParents{2}</code> number of vertices in the <i>parent</i> of the <i>parent</i> mesh, <code>nqParents{end}</code> number of vertices in the <i>global</i> mesh.
<code>toParents</code>	: 1-by- $n$ cell array <code>toParents{1}</code> indices array which convert local vertices numbering to the <i>parent</i> mesh vertices numbering, <code>toParents{2}</code> indices array which convert local vertices numbering to the <i>parent</i> of the <i>parent</i> mesh, <code>toParents{end}</code> indices array which convert local vertices numbering to the <i>global</i> mesh.

More precisely

- $q(i,j)$  is the  $i$ -th coordinate of the  $j$ -th vertex,  $i \in \{1, \dots, \text{dim}\}$ ,  $j \in \{1, \dots, nq\}$ . The  $j$ -th vertex will be also denoted by  $q^j = q(:, j)$ .
- $me(r,k)$  is the storage index of the  $r$ -th vertex of the  $k$ -th element ( $d$ -simplex), in the array `q`, for  $r \in \{1, \dots, d + 1\}$  and  $k \in \{1, \dots, nme\}$ . So  $q(:, me(r,k))$  represents the coordinates of the  $r$ -th vertex of the  $k$ -th mesh element.
- $vols(k)$  is the volume of the  $k$ -th  $d$ -simplex .

## 2.3 fc\_simesh.siMesh object

A  $d$ -simplicial mesh in dimension `dim`, represented as an `fc_simesh.siMesh` object, is an union of `fc_simesh.siMeshElt` objects which are elementary  $l$ -simplicial meshes ( $0 \leq l \leq d$ ) in space dimension `dim`.

fc_simesh.siMesh object properties	
<code>dim</code>	: integer space dimension
<code>d</code>	: integer $d$ -dimensional simplicial mesh
<code>sTh</code>	: array of <code>fc_simesh.siMeshElt</code> objects
<code>nsTh</code>	: number of <code>fc_simesh.siMeshElt</code> objects
<code>sThsimp</code>	: array of <code>nsTh</code> integers $i$ -th <code>fc_simesh.siMeshElt</code> object in <code>sTh</code> is a <code>sThsimp(i)</code> -simplicial elementary mesh
<code>sThlab</code>	: array of <code>nsTh</code> integers in <code>sTh</code> label of $i$ -th <code>fc_simesh.siMeshElt</code> object in <code>sTh</code> is number <code>sThlab(i)</code>
<code>nq</code>	: integer number of vertices in the mesh
<code>toGlobal</code>	: 1-by- <code>nq</code> array of integers convert from local to global mesh vertices numbering. Prefer the use of <code>ndtoParent</code> instead. <i>It will be removed in a future release.</i>
<code>toParent</code>	: 1-by- <code>nq</code> array of integers convert from local to parent mesh vertices numbering (same as <code>toGlobal</code> if not part of a partitioned mesh). Prefer the use of <code>toParents1</code> instead. <i>It will be removed in a future release.</i>
<code>nqParents</code>	: 1-by- $n$ array of integers Only used with partitioned mesh and the <b>FC-PSIMESH</b> package.
<code>toParents</code>	: 1-by- $n$ cell array Only used with partitioned mesh and the <b>FC-PSIMESH</b> package.

Let `Th` be a `fc_simesh.siMesh` object. The global `dim`-by-`(Th.nq)` array `q` of mesh vertices is not explicitly stored in `Th`, however one can easily build it if necessary:

```
q=zeros(Th.dim,Th.nq);
for i=Th.find(Th.d)
    q(:,Th.sTh{i}.toParents{1})=Th.sTh{i}.q;
end
```

## 2.4 Mesh samples

### 2.4.1 2-simplicial mesh in $\mathbb{R}^2$

```
Listing 2: 2D fc_simesh.siMesh object from sample20.geo
meshfile=fc_oogmsh.gmsh.buildmesh2d('sample20',20,'force',false);
Th=fc_simesh.siMesh(meshfile);
fprintf('***_Th:\n');
disp(Th)
fprintf('***_Th.sTh{9}:\n')
disp(Th.sTh{9})
```

Output

```
[fc-oogmsh] Input file : <fc-oogmsh>/geodir/2d/sample20.geo
[fc-oogmsh] Starting building mesh <fc-oogmsh>/meshes/sample20-20.msh with gmsh 4.5.2
[fc-oogmsh] Using command : gmsh -2 -setnumber N 20 -string "Mesh.MshFileVersion=4.1;" ...
<fc-oogmsh>/geodir/2d/sample20.geo -o <fc-oogmsh>/meshes/sample20-20.msh
Be patient...
[fc-oogmsh] Using gmsh 4.5.2 to write MSH file format version 4.1 in ...
<fc-oogmsh>/meshes/sample20-20.msh
*** Th:
fc_simesh.siMesh with properties:
  bbox: [ -1 1 -1 1 ] (1x4 double)
  d: 2 double
  dim: 2 double
  nq: 2326 double
  nqParents: 2326 double
  nsTh: 11 double
  other: (1x1 struct)
  sTh: (1x11 cell)
  sThboundlabs: []
  sThcolors: (11x3 double)
  sTheolab: []
  sThlab: [ 1 2 10 20 1 2 20 101 102 103 104 ] (1x11 double)
  sThpartlabs: []
  sThphyslab: [ 1 2 10 20 ] (1x4 double)
  sThsimp: [ 2 2 2 2 1 1 1 1 1 1 1 1 ] (1x11 double)
  toGlobal: (1x2326 double)
  toParent: (1x2326 double)
  toParents: (1x1 cell)
*** Th.sTh{9}:
siMeshEl with properties:
  Tag: (1x30 char)
  bbox: [ 1 1 -1 1 ] (1x4 double)
  color: [ 0.0544828 0.448276 0.0689655 ] (1x3 double)
  d: 1 double
  dim: 2 double
  geolab: []
  gradBaCo: (40x2x2 double)
  h: 0.05 double
  label: 102 double
  me: (2x40 double)
  nme: 40 double
  nq: 41 double
  nqGlobal: 41 double
  nqParent: 41 double
  nqParents: 41 double
  order: 1 double
  partlab: []
  q: (2x41 double)
  toGlobal: (1x41 double)
  toParent: (1x41 double)
  toParents: (1x1 cell)
  vols: (1x40 double)
```

From the output of the Listing 2 or from the Figure 1 the complete domain is

$$\Omega = \Omega_1 \cup \Omega_2 \cup \Omega_{10} \cup \Omega_{20}$$

and we note

$$\Gamma = \Gamma_1 \cup \Gamma_2 \cup \Gamma_{20} \cup \Gamma_{101} \cup \Gamma_{102} \cup \Gamma_{103} \cup \Gamma_{104}.$$

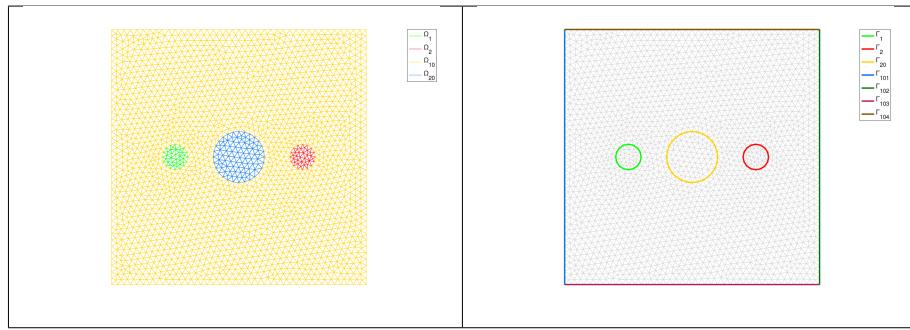


Figure 1: 2D `fc_simesh.siMesh` object from `sample20.geo`

So this mesh is 2-simplicial mesh in  $\mathbb{R}^2$  and is composed of :

- four 2-simplicial elementary meshes :  $\Omega_i, \forall i \in \{1, 2, 10, 20\}$
- seven 1-simplicial elementary meshes :  $\Gamma_i \forall i \in \{1, 2, 20, 101, 102, 103\}$

### 2.4.2 Sample of a 3-simplicial mesh in $\mathbb{R}^3$

```

Listing 3: 3D Mesh from quart_sphere2.geo

meshfile=fc_oogmsh.gmsh.buildmesh3d('quart_sphere2',5);
Th=fc_simesh.siMesh(meshfile);
fprintf('***_Th:\n')
disp(Th)
fprintf('***_Th.sTh{9}:\n')
disp(Th.sTh{9})

```

Output

```

[fc-oogmsh] Input file : <fc-oogmsh>/geodir/3d/quart_sphere2.geo
[fc-oogmsh] Starting building mesh <fc-oogmsh>/meshes/quart_sphere2-5.msh with gmsh 4.5.2
[fc-oogmsh] Using command : gmsh -3 -setnumber N 5 -string "Mesh.MshFileVersion=4.1;" ...
<fc-oogmsh>/geodir/3d/quart_sphere2.geo -o <fc-oogmsh>/meshes/quart_sphere2-5.msh
Be patient...
[fc-oogmsh] Using gmsh 4.5.2 to write MSH file format version 4.1 in ...
<fc-oogmsh>/meshes/quart_sphere2-5.msh
Mesh quart_sphere2-5.msh is a 3-dimensional mesh
Force dimension to 3
*** Th:
fc_simesh.siMesh with properties:
    bbox: [ -1 1 0 1 0 1 ] (1x6 double)
    d: 3 double
    dim: 3 double
    nq: 1171 double
    nqParents: 1171 double
    nsTh: 23 double
    other: (1x1 struct)
    sTh: (1x23 cell)
    sThboundlabs: []
    sThcolors: (23x3 double)
    sThgeolab: []
    sThlab: [ 1 2 1 2 3 4 5 6 7 1 2 3 4 5 6 7 8 9 1 2 3 4 5 ] (1x23 double)
    sThpartlabs: []
    sThphyslab: [ 1 2 ] (1x2 double)
    sThsimp: [ 3 3 2 2 2 2 2 1 1 1 1 1 1 1 1 0 0 0 0 0 ] (1x23 double)
    toGlobal: (1x1171 double)
    toParent: (1x1171 double)
    toParents: (1x1 cell)
*** Th.sTh{9}:
siMeshElt with properties:
    Tag: (1x30 char)
    bbox: [ 0 1 0 1 0 1 ] (1x6 double)
    color: [ 0.517241 0.310345 0 ] (1x3 double)
    d: 2 double
    dim: 3 double
    geolab: []
    gradBaCo: (359x3x3 double)
    h: 0.127349 double
    label: 7 double
    me: (3x359 double)
    nme: 359 double
    nq: 203 double
    nqGlobal: 203 double
    nqParent: 203 double
    nqParents: 203 double
    order: 1 double
    partlab: []
    q: (3x203 double)
    toGlobal: (1x203 double)
    toParent: (1x203 double)
    toParents: (1x1 cell)
    vols: (1x359 double)

```

The mesh obtained from Listing 3 is a 3-simplicial mesh in  $\mathbb{R}^3$  and is composed of :

- two 3-simplicial elementary meshes :  $\Omega_i$ ,  $\forall i \in \{1, 2\}$
- seven 2-simplicial elementary meshes :  $\Gamma_i$   $\forall i \in \llbracket 1, 7 \rrbracket$
- nine 1-simplicial elementary meshes :  $\partial\Gamma_i$   $\forall i \in \llbracket 1, 9 \rrbracket$

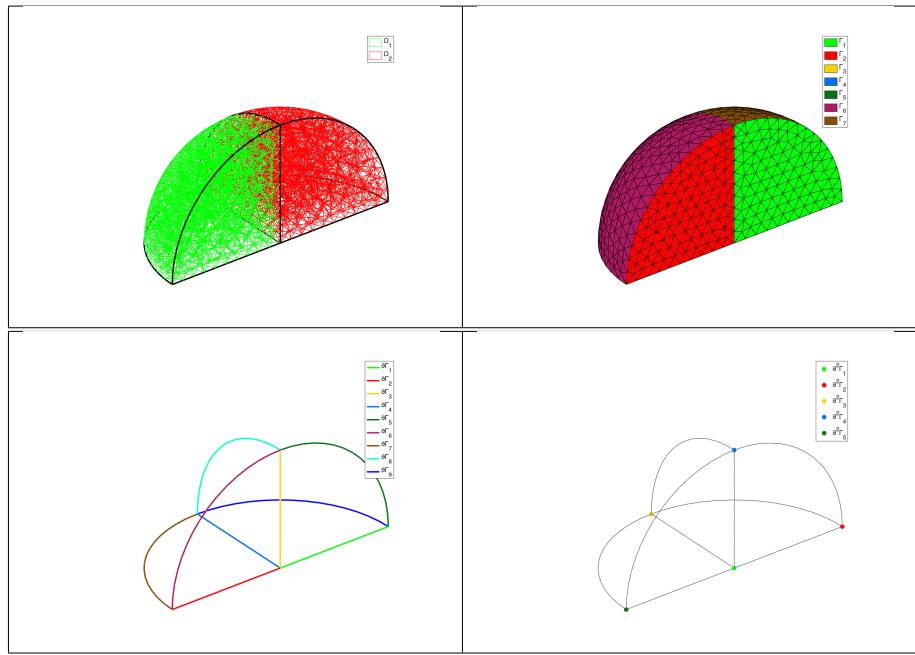


Figure 2: 3D Mesh from `quart_sphere2.geo`

- five 0-simplicial elementary meshes :  $\partial^2 \Gamma_i \quad \forall i \in \llbracket 1, 5 \rrbracket$

### 2.4.3 Sample of a 2-simplicial mesh in $\mathbb{R}^3$

```

Listing 4: 3D surface Mesh from demisphere4surf.geo

meshfile=fc_oogmsh.gmsh.buildmesh3ds('demisphere4surf',5,'force',true);
Th=fc_simesh.siMesh(meshfile);
fprintf('***_Th:\n')
disp(Th)
fprintf('***_Th.sTh{9}:\n')
disp(Th.sTh{9})

Output
[fc-oogmsh] Input file : <fc-oogmsh>/geodir/3ds/demisphere4surf.geo
[fc-oogmsh] Starting building mesh <fc-oogmsh>/meshes/demisphere4surf-5.msh with gmsh 4.5.2
[fc-oogmsh] Using command : gmsh -2 -setnumber N 5 -string "Mesh.MshFileVersion=4.1;" ...
    <fc-oogmsh>/geodir/3ds/demisphere4surf.geo -o <fc-oogmsh>/meshes/demisphere4surf-5.msh
Be patient...
[fc-oogmsh] Using gmsh 4.5.2 to write MSH file format version 4.1 in ...
    <fc-oogmsh>/meshes/demisphere4surf-5.msh
Mesh demisphere4surf-5.msh is a 3-dimensional mesh
    Force dimension to 3
*** Th:
fc_simesh.siMesh with properties:
    bbox: [ -1 1 -1 1 0 1 ] (1x6 double)
        d: 2 double
        dim: 3 double
        nq: 228 double
    nqParents: 228 double
        nsTh: 12 double
        other: (1x1 struct)
        sTh: (1x12 cell)
    sThboundlabs: []
        sThcolors: (12x3 double)
        sThgeolab: []
            sThlab: [ 1 2 3 4 1 2 3 4 5 6 7 8 ] (1x12 double)
    sThpartlabs: []
        sThphyslab: [ 1 2 3 4 ] (1x4 double)
            sThsimp: [ 2 2 2 2 1 1 1 1 1 1 1 1 ] (1x12 double)
                toGlobal: (1x28 double)
                toParent: (1x28 double)
                toParents: (1x1 cell)
*** Th.sTh{9}:
siMeshElt with properties:
    Tag: (1x26 char)
        bbox: [ -1 0 0 0 0 1 ] (1x6 double)
        color: [ 0.0344828 0.448276 0.0689655 ] (1x3 double)
            d: 1 double
            dim: 3 double
            geolab: []
        gradBaCo: (8x2x3 double)
            h: 0.196034 double
        label: 5 double
            me: (2x8 double)
            nme: 8 double
            nq: 9 double
        nqGlobal: 9 double
        nqParent: 9 double
        nqParents: 9 double
            order: 1 double
            partlab: []
                q: (3x9 double)
            toGlobal: (1x9 double)
            toParent: (1x9 double)
            toParents: (1x1 cell)
            vols: [ 0.196034 0.196034 0.196034 0.196034 0.196034 0.196034 0.196034 ] ...
                (1x8 double)

```

The mesh obtained from the Listing 4 or from the Figure 3 is a 2-simplicial mesh in  $\mathbb{R}^3$  and is composed of :

- four 2-simplicial elementary meshes :  $\Omega_i$ ,  $\forall i \in \llbracket 1, 4 \rrbracket$
- eight 1-simplicial elementary meshes :  $\Gamma_i$   $\forall i \in \llbracket 1, 8 \rrbracket$

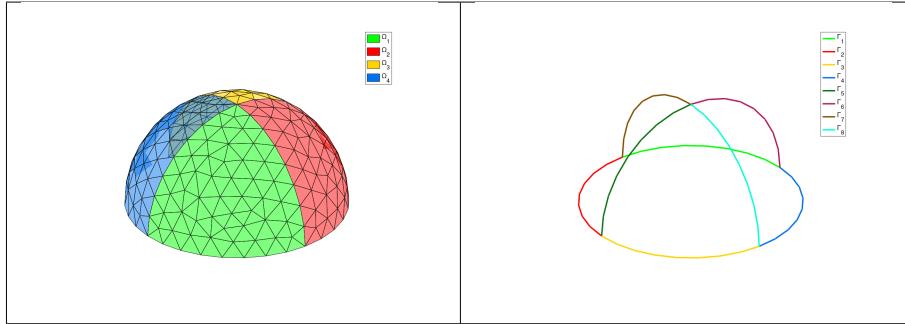


Figure 3: 3D surface Mesh from `demisphere4surf.geo`, label of the domains (left) and label of the boundaries (right)

## 2.5 Methods of the `fc_simesh.siMesh` object

### 2.5.1 `fc_simesh.siMesh` constructor

The constructor of the `fc_simesh.siMesh` class can initialize the object from various kind of mesh file format : `.msh` (default `gmsh` format), `.mesh` (`FreeFEM++` or `Medit`) or ... (`triangle`).

#### Syntaxe

```
Th=fc_simesh.siMesh( meshfile )
Th=fc_simesh.siMesh( meshfile ,Name, Value )
```

#### Description

`Th=fc_simesh.siMesh(meshfile)` create the `fc_simesh.siMesh` object  $\mathcal{T}_h$  from the mesh file `meshfile` (`gmsh` format by default).

`Th=fc_simesh.siMesh(meshfile,Key,Value, ...)` specifies function options using one or more `Key,Value` pair arguments. The string `Key` options can be

- `'format'` : to specify the format of the mesh file `meshfile`. `Value` must be `'medit'`, `'gmsh'` (default), `'freefem'` or `'triangle'`.
- `'dim'` : to specify the space dimension (default 2),
- `'d'` : to specify the dimensions of the simplices to read, (default `[dim,dim-1]`)

**Examples** The following example use the function `fc_oogmsh.gmsh.buildmesh2d` of the `FC-OOGMSH` package to build the mesh from the `.geo` file `condenser11.geo`. This `.geo` file is located in the directory `geodir/2d` of the `FC-OOGMSH` package.

```
Listing 5: fc_simesh.siMesh constructor
meshfile=fc_oogmsh.gmsh.buildmesh2d('condenser11',25,'verbose',0);
disp('*** Read mesh ***')
Th=fc_simesh.siMesh(meshfile)
```

#### Output

```
[fc-oogmsh] Using gmsh 4.5.2 to write MSH file format version 4.1 in ...
<fc-oogmsh>/meshes/condenser11-25.msh
*** Read mesh ***
Th =

fc_simesh.siMesh with properties:
    bbox: [-1 1 -1 1] (1x4 double)
        d: 2 double
        dim: 2 double
        nq: 3162 double
    nqParents: 3162 double
        nsTh: 19 double
        other: (1x1 struct)
            sTh: (1x19 cell)
    sThboundlabs: []
        sThcolors: (19x3 double)
        sTheolab: []
        sThlab: [2 4 6 8 10 20 1 2 3 4 5 6 7 8 20 101 102 103 104] (1x19 double)
    sThpartlabs: []
        sThphyslab: [2 4 6 8 10 20] (1x6 double)
        sThsimp: [2 2 2 2 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1] (1x19 double)
        toGlobal: (1x3162 double)
        toParent: (1x3162 double)
        toParents: (1x1 cell)
```

### 2.5.2 find method

We denote by `Th` a `fc_simesh.siMesh` object.

- `Th.find(d)` : returns the sorted indices array of the `d`-simplicial elementary meshes in the array `Th.sTh`.
- `Th.find(d,labels)` : returns the sorted indices of the `d`-simplicial elementary meshes with label in `labels`. `labels` could be an index, an array of indices. If nothing is found then return `[]`.

Several examples are given in functions:

`fc_simesh.demos.find2D()`, `fc_simesh.demos.find3D()`, `fc_simesh.demos.find3Ds()`  
Now some very basic samples are presented.

```

Listing 6: fc_simesh.siMesh find method samples
meshfile=fc_oogmsh.gmsh.buildmesh3d('quart_sphere2',5,'verbose',0);
Th=fc_simesh.siMesh(meshfile,'dim',3);
disp(Th)
idx=Th.find(3);
fprintf('3-simplices_siMeshElt_\nindices : [%s], ...'
    labels=[%s]\n',num2str(idx),num2str(Th.sThlab(idx)) )
idx=Th.find(2);
fprintf('2-simplices_siMeshElt_\nindices : [%s], ...'
    labels=[%s]\n',num2str(idx),num2str(Th.sThlab(idx)) )
idx=Th.find(2,4);
fprintf('2-simplices_siMeshElt_with_label==4\nindices : [%s], ...'
    labels=[%s]\n',num2str(idx),num2str(Th.sThlab(idx)) )
idx=Th.find(2,[6,4,2,10]);
fprintf('2-simplices_siMeshElt_with_label_in_[6,4,2,10]\nindices : [%s], ...'
    labels=[%s]\n',num2str(idx),num2str(Th.sThlab(idx)) )

```

Output

```

fc_simesh.siMesh with properties:
  bbox: [-1 1 0 1 0 1] (1x6 double)
    d: 3 double
    dim: 3 double
    nq: 1171 double
    nqParents: 1171 double
    nsTh: 23 double
    other: (1x1 struct)
      sTh: (1x23 cell)
    sThboundlabs: []
    sThcolors: (23x3 double)
    sTheolab: []
      sThlab: [1 2 1 2 3 4 5 6 7 1 2 3 4 5 6 7 8 9 1 2 3 4 5] (1x23 double)
    sThpartlabs: []
    sThphyslab: [1 2] (1x2 double)
      sThimp: [3 3 2 2 2 2 2 2 1 1 1 1 1 1 1 1 0 0 0 0 0] (1x23 double)
    toGlobal: (1x1171 double)
    toParent: (1x1171 double)
    toParents: (1x1 cell)
3-simplices siMeshElt
  indices: [1 2], labels=[1 2]
2-simplices siMeshElt
  indices: [3 4 5 6 7 8 9], labels=[1 2 3 4 5 6 7]
2-simplices siMeshElt with label==4
  indices: [6], labels=[4]
2-simplices siMeshElt with label in [6,4,2,10]
  indices: [4 6 8], labels=[2 4 6]

```

### 2.5.3 feval method

Evaluates a vectorized function at vertices of the mesh. We denote by `Th` a `fc_simesh.siMesh` object.

- `res=Th.eval(fun)` : the input parameter `fun` is either a function or a cell array of function handles for vector-valued functions. If `fun` is a function then the output is an `Th.nq`-by-1 array. If `fun` is a cell array of function handles then the output is an `Th.nq`-by-`length(fun)` array.
- `res=Th.eval(fun,key,value,...)` specifies function options using one or more `key,value` pair arguments. The string `key` options could be
  - `d` : to specify the `d`-simplicial elementary meshes on which to evaluate the function (default `Th.d`). A zero value is set on all vertices not in these elementary meshes.
  - `labels` : to specify the labels of the elementary meshes on which to evaluate the function (default is all). A zero value is set on all vertices not in these elementary meshes.

Several examples are given in functions:

`fc_simesh.demos.feval2D01()`, `fc_simesh.demos.feval3D01()`, ...

We present now some very basic samples.

**Sample 1** Let  $g : \mathbb{R}^2 \mapsto \mathbb{R}$  defined by  $g(x, y) = \cos(x)\sin(y)$ . We propose in Listing 7 four approaches to define this function for using with `feval` method.

Listing 7: `feval` method, four ways to define a function

```

meshfile=fc_oogmsh.gmsh.buildmesh2d('condenser11',50,'verbose',0);
Th=fc_simesh.siMesh(meshfile);

g1=@(x,y) cos(x).*sin(y); % .* for vectorized function
g2=@(X) cos(X(1,:)).*sin(X(2,:));

z1=Th.fevel(g1);
z2=Th.fevel(g2);

fprintf('max( abs( z2-z1 ) )=%e\n',max(abs(z2-z1)))

```

Output

```

[fc-oogmsh] Using gmsh 4.5.2 to write MSH file format version 4.1 in ...
<fc-oogmsh>/meshes/condenser11-50.msh
max(abs(z2-z1))=0.000000e+00

```

## Sample 2

Listing 8: `feval` method with a vector-valued function

```

meshfile=fc_oogmsh.gmsh.buildmesh2d('condenser11',50,'verbose',0);
Th=fc_simesh.siMesh(meshfile)

% f : R^2 -> R^3
f=[@(x,y) cos(2*x).*sin(3*y),@(x,y) cos(3*x).*sin(4*y),@(x,y) cos(4*x).*sin(5*y)];
z=Th.fevel(f);
fprintf('*** nq=%d, size(z)==[%d,%d]\n', Th.nq, size(z))

```

Output

```

Th =

  fc_simesh.siMesh with properties:
    bbox: [-1 1 -1 1] (1x4 double)
    d: 2 double
    dim: 2 double
    nq: 11945 double
    nqParents: 11945 double
    nsTh: 19 double
    other: (1x1 struct)
    sTh: (1x19 cell)
  sThboundlabs: []
    sThcolors: (19x3 double)
    sTheolab: []
    sThlab: [ 2 4 6 8 10 20 1 2 3 4 5 6 7 8 20 101 102 103 104 ] (1x19 double)
  sThpartlabs: []
  sThphyslab: [ 2 4 6 8 10 20 ] (1x6 double)
    sThsimp: [ 2 2 2 2 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 ] (1x19 double)
    toGlobal: (1x11945 double)
    toParent: (1x11945 double)
    toParents: (1x1 cell)

*** nq=11945, size(z)==[11945,3]

```

### 2.5.4 eval method

Evaluates numerical datas or vectorized functions at vertices of the mesh. We denote by `Th` a `fc_simesh.siMesh` object and  $n_q = Th.nq$  the total number of vertices.

- `res=Th.eval(data)` : the input parameter `data` could be

- a scalar,
- a handle to a vectorized function,
- a  $n_q$ -by-1 array,
- a 1-by- $m$  cell array of mixed previous kinds, ( $m \geq 1$ ).

The return value is a  $n_q$ -by-1 array if the input parameter `data` is not a cell array otherwise it's a  $n_q$ -by- $m$  array.

- `res=Th.eval(data,key,value,...)` specifies function options using one or more `key,value` pair arguments. The string `key` options could be

- `d` : to specify the  $d$ -simplicial elementary meshes on which to evaluate `data` (default `Th.d`). A zero value is set on all vertices not in these elementary meshes.
- `labels` : to specify the labels of the elementary meshes on which to evaluate `data` (default is all). A zero value is set on all vertices not in these elementary meshes.

Several examples are given in functions:

`fc_simesh.demos.eval2D01()`, `siMesh.demos.eval3D01()`, ...

We present now some very basic samples.

## Sample 1

```
Listing 9: eval method, four ways to defined a function
meshfile=fc_oogmsh.gmsh.buildmesh2d('condenser11',50,'verbose',0);
Th=fc_simesh.siMesh(meshfile);

g1=pi*ones(Th.nq,1);
g2=pi*ones(1,Th.nq);
g3=@(X) pi;

z1=Th.eval(g1);
z2=Th.eval(g2);
z3=Th.eval(g3);

fprintf('size(z1)=%d,%d]\n',size(z1))
fprintf('size(z2)=%d,%d]\n',size(z2))
fprintf('size(z3)=%d,%d]\n',size(z3))
fprintf('max(abs(z2-z1))=%e\n',max(abs(z2-z1)))
fprintf('max(abs(z3-z1))=%e\n',max(abs(z3-z1)))
```

Output

```
size(z1)=[11945,1]
size(z2)=[11945,1]
size(z3)=[11945,1]
max(abs(z2-z1))=0.000000e+00
max(abs(z3-z1))=0.000000e+00
```

## Sample 2

```

Listing 10: eval method with a vector-valued function
meshfile=fc_oogmsh.gmsh.buildmesh2d('condenser11',50,'verbose',0);
Th=fc_simesh.siMesh(meshfile);
u=Th.eval(@(x,y) cos(3*x).*sin(4*y));
% f : R^2 -> R^3
f=@(x,y) cos(2*x).*sin(3*y),u,@(x,y) cos(4*x).*sin(5*y),pi];
z=Th.eval(f);
fprintf('*** nq=%d, size(z)==[%d,%d] ',Th.nq,size(z))

```

Output

```
*** nq=11945, size(z)==[11945,4]
```

### 2.5.5 get\_h method

returns the maximum edges length of the mesh. We denote by `Th` a `fc_simesh.siMesh` object.

- `h=Th.get_h()`

### 2.5.6 get\_mesh method

Returns a vertices array `q`, a connectivity array `me` and a `toGlobal` indices array.

- `[q,me,toGlobal]=Th.get_mesh()` : returns the global vertices array `q`, the connectivity array `me` (i.e. all the `Th.d`-simplices of the mesh). In this case, `toGlobal` is just `1:Th.nq`.
- `[q,me,toGlobal]=Th.get_mesh(key,value,...)` specifies function options using one or more `key,value` pair arguments. The string `key` options could be
  - `'d'` : to specify the `d`-simplicial elementary meshes to consider.
  - `'labels'` : to specify the labels of the elementary meshes to consider.

In this case, `toGlobal` is a 1-by-`length(q)` array (subset of `1:Th.nq`). If we denote by `qglob` the global vertices array then  
`qglob(:,toGlobal)==q`

Several examples are given in functions:

`fc_simesh.demos.get_mesh2D()`, `siMesh.demos.get_mesh3D()`, `siMesh.demos.get_mesh3Ds()`

```

Listing 11: get_mesh method, four ways to defined a function
meshfile=fc_oogmsh.gmsh.buildmesh2d('condenser11',50,'verbose',0);
Th=fc_simesh.siMesh(meshfile);

[q,me,toGlobal]=Th.get_mesh();
[q2,me2,toGlobal2]=Th.get_mesh('labels',2:2:8);
[q1,me1,toGlobal1]=Th.get_mesh('d',1,'labels',1:8);

fprintf('norm(q(:,toGlobal2)-q2,Inf)=%e\n',norm(q(:,toGlobal2)-q2,Inf))
fprintf('norm(q(:,toGlobal1)-q1,Inf)=%e\n',norm(q(:,toGlobal1)-q1,Inf))

```

Output

```
norm(q(:,toGlobal2)-q2,Inf)=0.000000e+00
norm(q(:,toGlobal1)-q1,Inf)=0.000000e+00
```

### 2.5.7 get\_nme method

Returns the number of  $d$ -simplicial elements with  $d = \mathcal{T}_h.d$  by default. We denote by  $\text{Th}$  a `fc_simesh.siMesh` object.

- `nme=Th.get_nme()` : returns the number of  $\text{Th}.d$ -simplicial elements in the mesh.
- `nme=Th.get_mesh(key,value,...)` specifies function options using one or more `key,value` pair arguments. The string `key` options could be
  - '`d`' : to specify the  $d$ -simplicial elementary meshes to consider.
  - '`labels`' : to specify the labels of the elementary meshes to consider.

Listing 12: `get_nme` method

```

meshfile=fc_oogmsh.gmsh.buildmesh3d('quart_sphere2',5);
Th=fc_simesh.siMesh(meshfile);
for d=[Th.d:-1:0]
  fprintf('Number of %d-simplices : %d\n',d,Th.get_nme('d',d))
end

nme=Th.get_nme('d',2,'labels',1:4);
fprintf('Number of 2-simplices in union of label 's_1 to 4 : %d\n',nme);

```

Output

```

[fc-oogmsh] Input file : <fc-oogmsh>/geodir/3d/quart_sphere2.geo
[fc-oogmsh] Mesh file <fc-oogmsh>/meshes/quart_sphere2-5.msh [version 4.1] already exists.
-> Use "force" flag to rebuild if needed.
Mesh quart_sphere2-5.msh is a 3-dimensional mesh
  Force dimension to 3
Number of 3-simplices : 4784
Number of 2-simplices : 1651
Number of 1-simplices : 115
Number of 0-simplices : 5
Number of 2-simplices in union of label's 1 to 4 : 748

```

### 2.5.8 get\_nq method

Returns the number of vertices in the union of some elementary meshes. By default all the ( $\text{Th}.d$ )-simplicial elementary meshes are selected. We denote by  $\text{Th}$  a `fc_simesh.siMesh` object.

- `nq=Th.get_nq()` : returns the number of vertices in the union of the  $\text{Th}.d$ -simplicial elementary meshes.
- `nq=Th.get_nq(key,value,...)` specifies function options using one or more `key,value` pair arguments. The string `key` options could be
  - '`d`' : to specify the  $d$ -simplicial elementary meshes to consider.
  - '`labels`' : to specify the labels of the elementary meshes to consider.

Listing 13: `get_nqe` method

```

meshfile=fc_oogmsh.gmsh.buildmesh3d('quart_sphere2',5);
Th=fc_simesh.siMesh(meshfile);
for d=[Th.d:-1:0]
    fprintf('Number of vertices in %d-simplices elementary meshes : ...%
            \n',d,Th.get_nq('d',d))
end

nq=Th.get_nq('d',2,'labels',1:4);
fprintf('Number of vertices in the union of 2-simplices elementary meshes of ...
        label ''s_1_to_4 : %d\n',nq);

```

#### Output

```

[fc-oogmsh] Input file : <fc-oogmsh>/geodir/3d/quart_sphere2.geo
[fc-oogmsh] Mesh file <fc-oogmsh>/meshes/quart_sphere2-5.msh [version 4.1] already exists.
-> Use "force" flag to rebuild if needed.
Mesh quart_sphere2-5.msh is a 3-dimensional mesh
Force dimension to 3
Number of vertices in 3-simplices elementary meshes : 1171
Number of vertices in 2-simplices elementary meshes : 811
Number of vertices in 1-simplices elementary meshes : 111
Number of vertices in 0-simplices elementary meshes : 5
Number of vertices in the union of 2-simplices elementary meshes of label's 1 to 4 : 405

```

### 2.5.9 plotmesh method

The `plotmesh` method displays the mesh or parts of the mesh defined by an `fc_simesh.siMesh` object.

#### Syntaxe

```

Th.plotmesh()
Th.plotmesh(Name, Value, ...)

```

#### Description

`Th.plotmesh()` displays all the (`Th.d`)-dimensional simplices elements of `Th`, a `fc_simesh.siMesh` object.

`Th.plotmesh(Name,Value, ...)` specifies function options using one or more `Name,Value` pair arguments. Options of first level are

- '`d`' : to specify the dimension of the simplices elements (default : `Th.d`)
- '`labels`' : to select the labels of the elements to display,
- '`color`' : to specify the color of the displayed mesh elements. (default : use one color by displayed mesh elements),
- '`inlegend`' : add a legend name to graph if true (default : `false`)
- '`bounds`' : If `true`, draw the borders of the selected elementaries mesh elements (only for 2-dimensional simplices). (default : `false`)
- '`cutPlane`' : cut mesh by  $n$  plans given by  $n$ -by-4 array  $P$  where the equation of the  $i$ -th cut plane is given by

$$P(i,1)x + P(i,2)y + P(i,3)z + P(i,4) = 0.$$

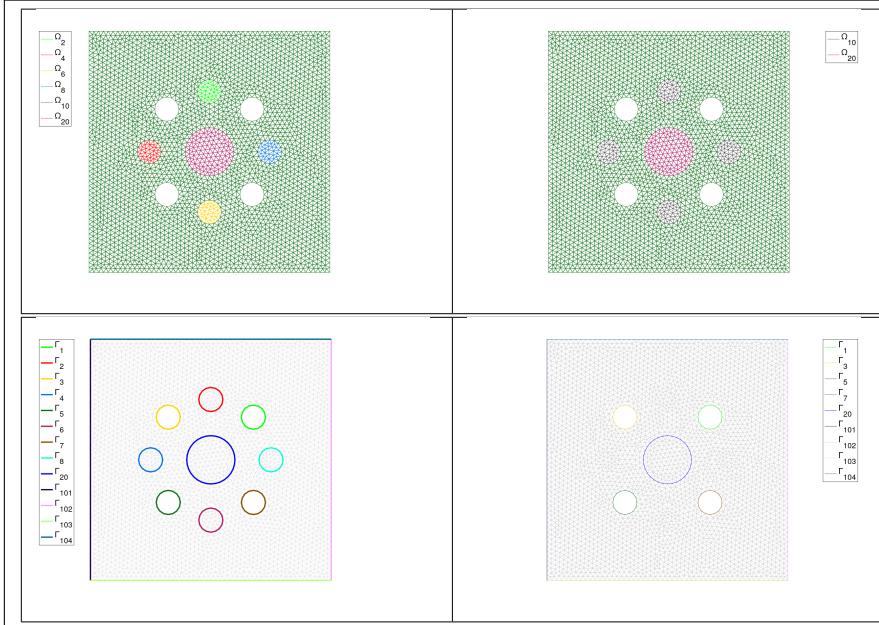
The normal vector  $P(i,1 : 3)$  pointed to the part of the mesh not displayed. (only for simplices in dimension 3) default : [] (no cut).

The options of second level depend on the type of elementaries mesh elements to represent.

One can use any option of the following functions according to the type of  $d$ -simplex to be represented.

- In dimension 3,
  - if  $d == 3$ , **patch** function is used,
  - if  $d == 2$ , **trimesh** function is used,
  - if  $d == 1$ , **plot3** function is used,
  - if  $d == 0$ , **plot3** function is used,
- In dimension 2,
  - if  $d == 2$ , **trimesh** function is used,
  - if  $d == 1$ , **plot** function is used,
  - if  $d == 0$ , **plot** function is used,
- In dimension 1,
  - if  $d == 1$ , **line** function is used,
  - if  $d == 0$ , **plot** function is used,

**2D example** The following example use the *.geo* file **condenser11.geo** which is in the directory **geodir** of the toolbox ....



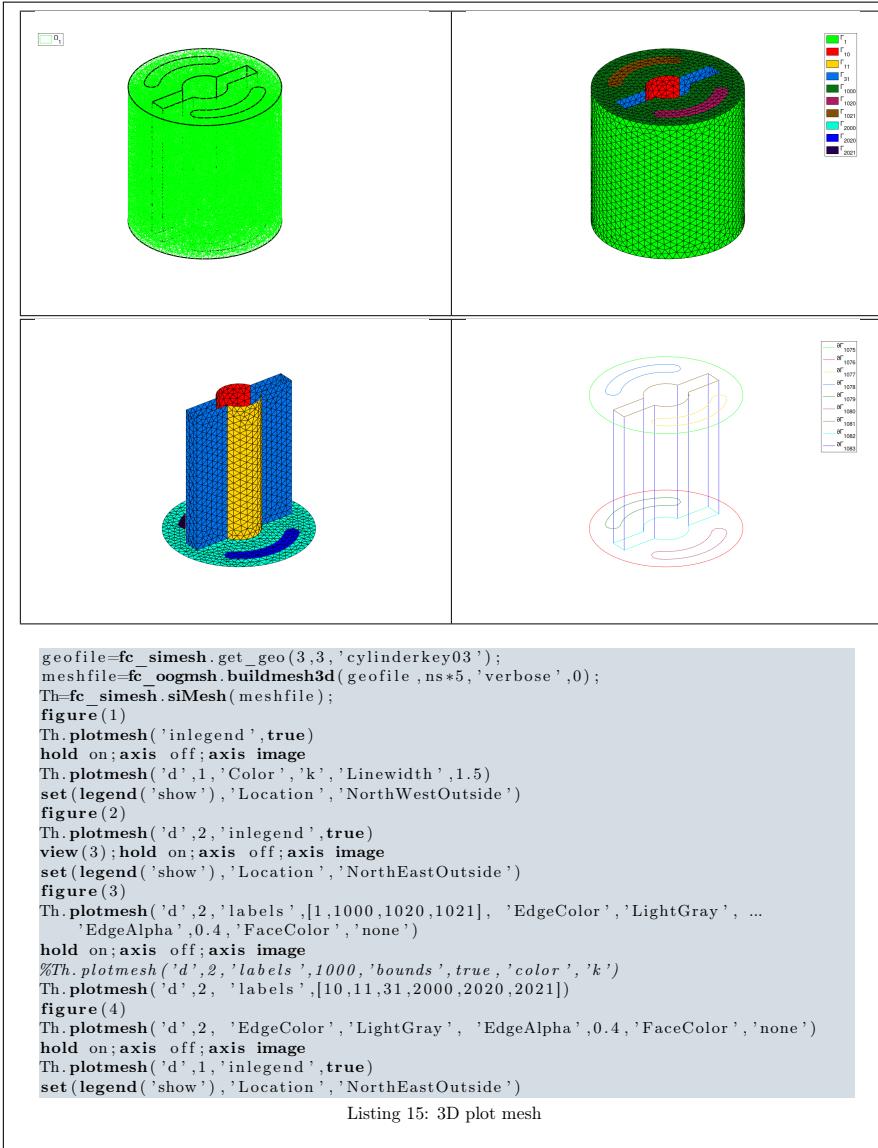
```

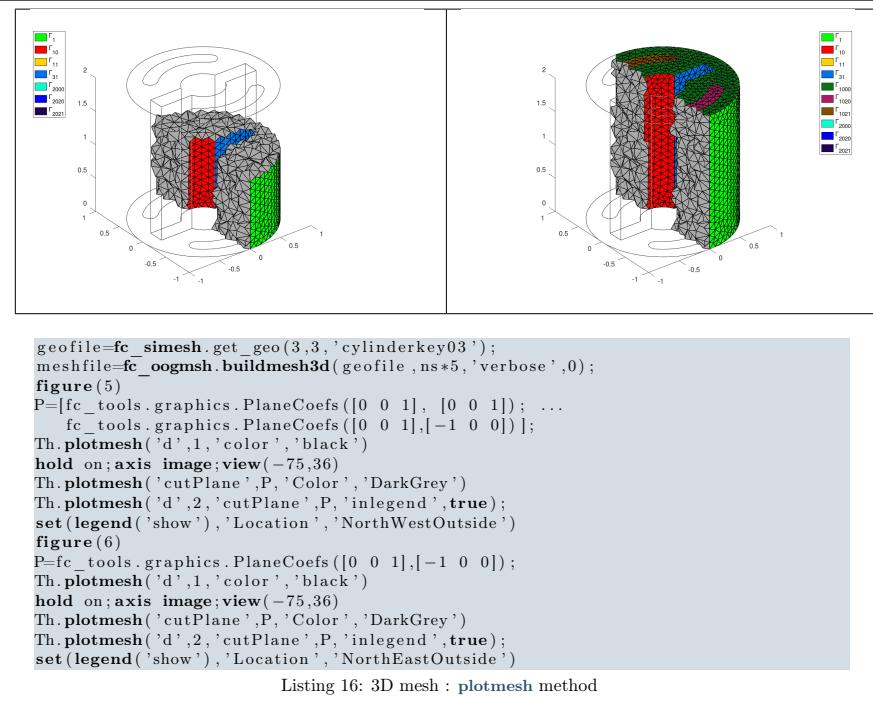
meshfile=fc_oogmsh.gmsh.buildmesh2d('condenser11',25,'verbose',0);
Th=fc_simesh.siMesh(meshfile);
figure(1)
Th.plotmesh('inlegend',true)
axis off; axis image;
set(legend('show'), 'Location', 'NorthWestOutside', 'fontsize',12)
figure(2)
Th.plotmesh('labels',[10,20], 'inlegend',true)
hold on; axis off; axis image
Th.plotmesh('labels',[2,4,6,8], 'Color', 'k', 'Linestyle', ':')
set(legend('show'), 'Location', 'NorthEastOutside', 'fontsize',12)
figure(3)
Th.plotmesh('Color',0.9*[1,1,1])
hold on; axis off; axis image;
Th.plotmesh('d',1,'inlegend',true, 'LineWidth',2)
set(legend('show'), 'Location', 'NorthWestOutside', 'fontsize',12)
figure(4)
Th.plotmesh('Color','LightGray')
hold on; axis off; axis image
Th.plotmesh('d',1,'inlegend',true, 'labels',[1:2:7,20,101:104])
set(legend('show'), 'Location', 'NorthEastOutside', 'fontsize',12)

```

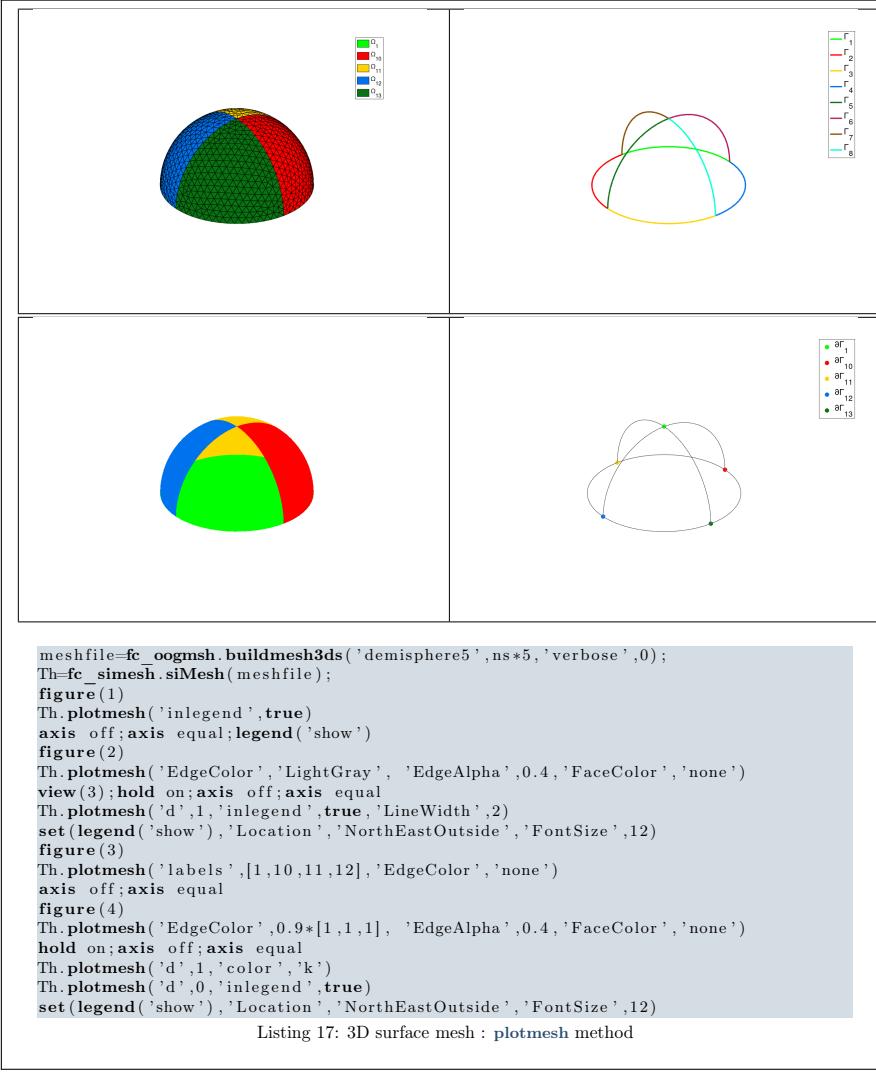
Listing 14: 2D mesh : `plotmesh` method

**3D example** The following example use the `.geo` file `cylinderkey.geo` which is in the directory `geodir` of the toolbox. This file contains description of a 3D mesh with simplices of dimensions 1, 2 and 3.





**3D surface example** The following example use the `.geo` file `demisphere5.geo` which is in the directory `geodir` of the toolbox. This file contains description of a 3D surface mesh with simplices of dimensions 1 and 2.



### 2.5.10 plot method

The `plot` method displays scalar datas on the mesh or parts of the mesh defined by an `fc_simesh.siMesh` object.

#### Syntaxe

<code>Th.plot(u)</code>
<code>Th.plot(u,Name,Value, ...)</code>

#### Description

`Th.plot(u)` displays data `u` on all the (`Th.d`)-dimensional simplices elements of `Th`, a `fc_simesh.siMesh` object. The data `u` is an 1D-array of size `Th.nq` or `Th.nqGlobal` or `Th.nqParent`.

`Th.plot(u,Name,Value, ...)` specifies function options using one or more `Name,Value` pair arguments. Options of first level are

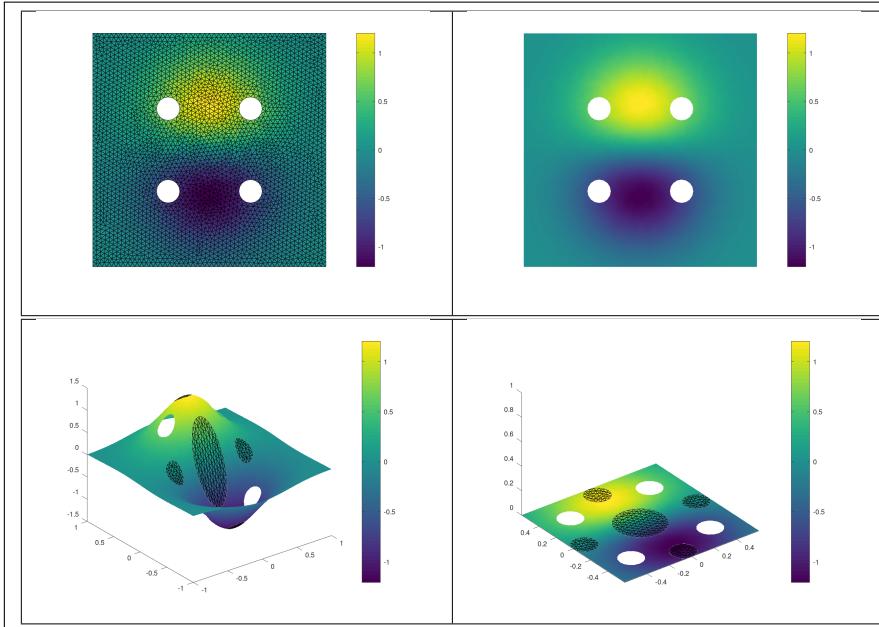
- '`d`' : to specify the dimension of the simplices elements (default : `Th.d`)
- '`labels`' : to select the labels of the elements to display data,
- '`plane`' : if true, made a 2D representation in the  $xy$ -plane, otherwise made a 3D representation with  $z$ -value set to `u` (default : `false`)

The options of second level depend on the type of elementaries mesh elements on which we want to represent datas.

One can use any option of the following functions according to the type of  $d$ -simplex.

- In dimension 3, `patch` function is used for  $d \in [1, 3]$ .
- In dimension 2,
  - for  $d == 2$ , if '`plane`' option is true, `patch` function is used, otherwise it's `trisurf` function,
  - for  $d == 1$ , `patch` function is used.
- In dimension 1 and  $d == 1$ , `plot` function is used

**2D example** The following example use the `.geo` file `condenser11.geo` which is in the directory `geodir` of the toolbox.



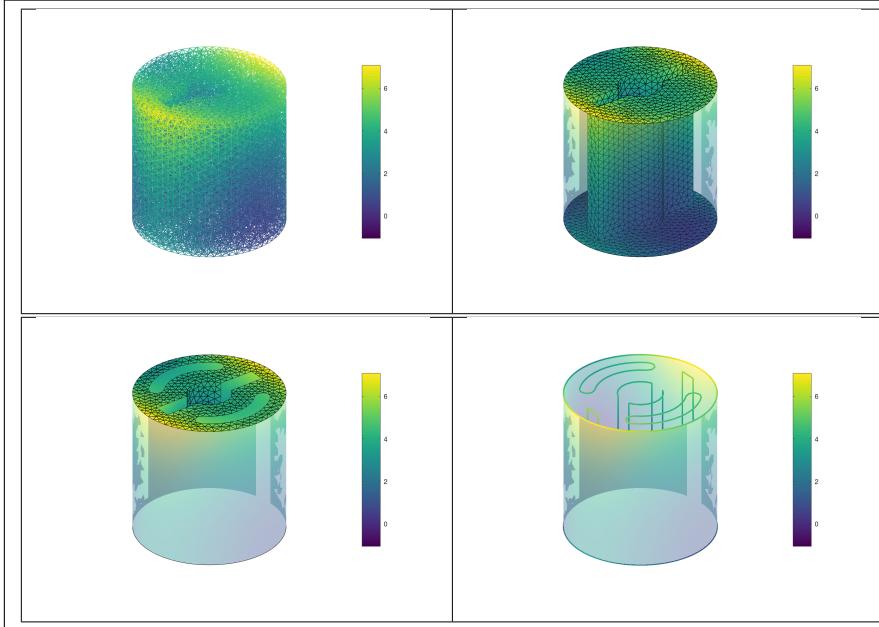
```

geofile=fc_simesh.get_geo(2,2,'condenser11');
meshfile=fc_oogmsh.gmsh.buildmesh2d(geofile,25,'verbose',0);
Th=fc_simesh.siMesh(meshfile);
u=Th.eval(@(x,y) 5*exp(-3*(x.^2+y.^2)).*cos(x).*sin(y));
figure(1)
Th.plot(u)
axis off;axis image;colorbar
figure(2)
Th.plot(u)
axis off;axis image;shading interp;colorbar
figure(3)
Th.plot(u,'labels',[2:2:8,20],'FaceColor','interp')
view(3);hold on;colorbar
Th.plot(u,'labels',10,'FaceColor','interp','EdgeColor','none')
figure(4)
Th.plot(u,'labels',[2:2:8,20], 'plane',true,'FaceColor','interp')
view(3);hold on;axis image;colorbar
Th.plot(u,'labels',10, 'plane',true, 'FaceColor','interp','EdgeColor','none')

```

Listing 18: 2D mesh : `plot` method

**3D example** The following example use the `.geo` file `cylinderkey.geo` which is in the directory `geodir` of the toolbox. This file contains description of a 3D mesh with simplices of dimensions 1, 2 and 3.



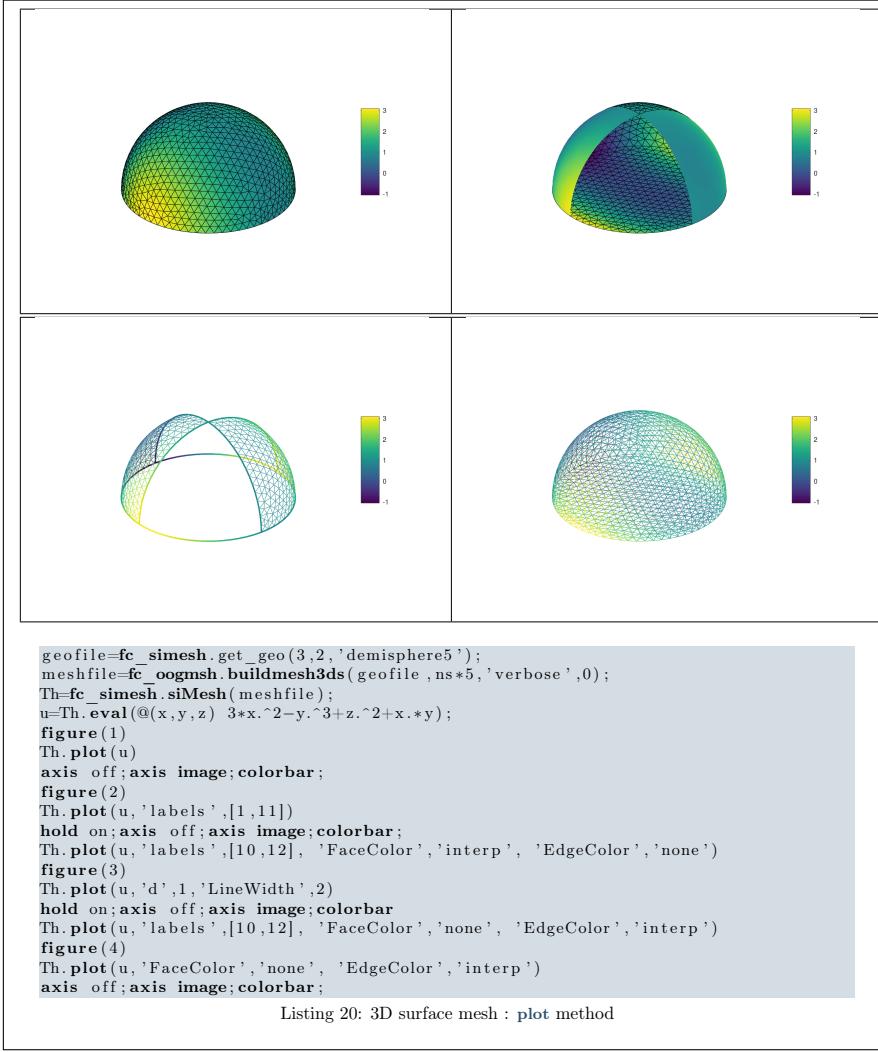
```

geoFile=fc_simesh.get_geo(3,3,'cylinderkey03');
meshfile=fc_oogmsh.buildmesh3d(geoFile,ns*5);
Th=fc_simesh.siMesh(meshfile);
u=Th.eval(@(x,y,z) 3*x.^2-y.^3+z.^2+x.*y);
figure(1)
Th.plot(u);
axis off; axis image; colorbar
figure(2)
Th.plot(u,'d',2,'labels',[10,11,31,1000,1020,1021,2000,2020,2021])
hold on; axis off; axis image; colorbar
Th.plot(u,'d',2,'labels',1,'FaceColor','interp',...
'EdgeColor','none','FaceAlpha',0.4)
figure(3)
Th.plot(u,'d',2,'labels',1,'FaceColor','interp',...
'EdgeColor','none','FaceAlpha',0.4)
hold on; axis off; axis image; colorbar
Th.plot(u,'d',2,'labels',[10,11,1000,2000])
Th.plot(u,'d',2,'labels',[31,1020,1021,2020,2021],...
'FaceColor','interp','EdgeColor','none')
figure(4)
Th.plot(u,'d',2,'labels',1,'FaceColor','interp',...
'EdgeColor','none','FaceAlpha',0.4)
hold on; axis off; axis image; colorbar
Th.plot(u,'d',1,'LineWidth',2)

```

Listing 19: 3D mesh : `plot` method

**3D surface example** The following example use the `.geo` file `demisphere5.geo` which is in the directory `geodir` of the toolbox. This file contains description of a 3D surface mesh with simplices of dimensions 1 and 2.



### 2.5.11 `plotiso` method

The `plotiso` method displays isolines from datas on the mesh or parts of the mesh defined by an `fc_simesh.siMesh` object. This function only works with 2-simplices in space dimension 2 or 3.

#### Syntaxe

```

Th.plotiso(u)
Th.plotiso(u,Name,Value, ...)
```

#### Description

`Th.plotiso(u)` displays data `u` on all the 2-dimensional simplices elements of `Th`, a `fc_simesh.siMesh` object.. The data `u` is an 1D-array of size `Th.nq` or `Th.nqGlobal` or `Th.nqParent`.

`Th.plotiso(u,key,value, ...)` ] specifies function options using one or more `key,value` pair arguments. Options of first level are

- '`niso`' : to specify the number of isolines (default : 10)
- '`isorange`' : to specify the list of isovalues (default : empty)
- '`isocolorbar`' : if `true`, colorbar with isovalues is drawn (default : `false`)
- '`format`' : to specify the format of the isovalues on the colorbar (default : '`%%g`')
- '`labels`' : to select the labels of the elements to display data,
- '`plane`' : if true, isolines are in the  $xy$ -plane, otherwise isolines are in 3D with  $z$ -value set to `u` (default : `false`)
- '`color`' : to specify one color for all isolines (default : empty)
- '`mouse`' : if `true`, display information on clicked isoline (default : `false`)

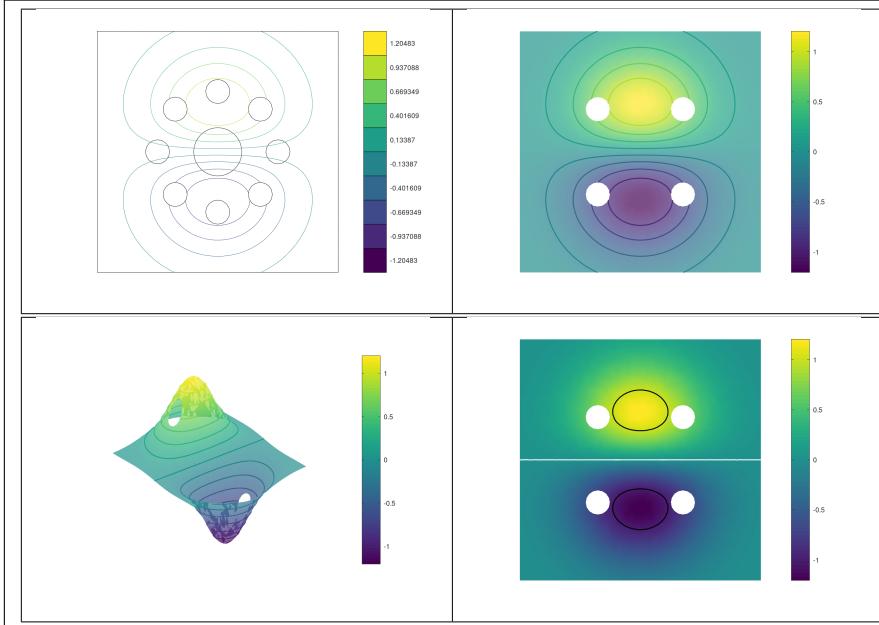
The options of second level are all options of

- `plot3` function in dimension 3 or in dimension 2 with '`plane`' option set to `false`
- `plot` function in 2 with '`plane`' option set to `true`

This function accepts until 4 output arguments :

- 1st output is the colors of the isolines
- 2nd output is the isovalues of the isolines
- 3th output is the handle of the colobar iso.
- 4th output is all the handles of the isolines as an 2D-array of dimension N-by-niso, where N is the number of 2-simplex elementary meshes where isolines are drawn.

**2D example** The following example use the `.geo` file `condenser11.geo` which is in the directory `geodir` of the toolbox.



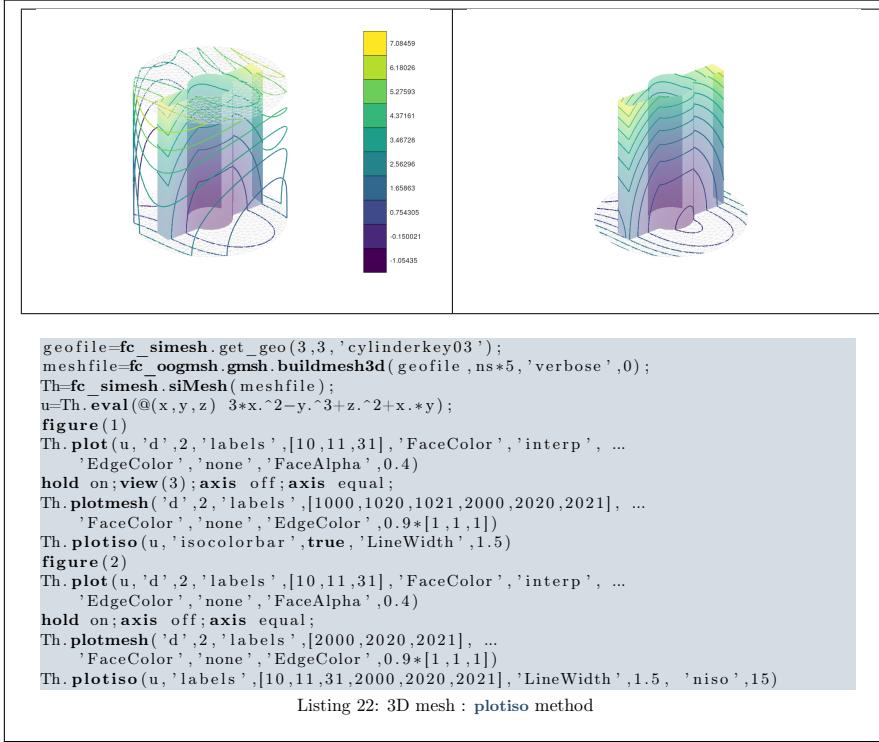
```

meshfile=fc_oogmsh.gmsh.buildmesh2d('condenser11',25,'verbose',0);
Th=fc_simesh.siMesh(meshfile);
u=Th.eval(@(x,y) 5*exp(-3*(x.^2+y.^2)).*cos(x).*sin(y));
figure(1)
Th.plotmesh('d',1,'color','k')
hold on;axis off;axis image;
Th.plotiso(u,'isocolorbar',true)
figure(2)
Th.plot(u,'plane',true,'FaceAlpha',0.7)
hold on;axis off;axis image;shading interp;
Th.plotiso(u,'plane',true,'LineWidth',1.5)
colorbar
figure(3)
Th.plot(u,'FaceAlpha',0.7)
view(3)
shading interp;hold on;axis off;axis image;
Th.plotiso(u,'nisos',15,'LineWidth',1.5)
colorbar
figure(4)
Th.plot(u,'plane',true)
shading interp;hold on;axis off;axis image;
Th.plotiso(u,'isorange',0,'LineWidth',1.5,'color','w')
Th.plotiso(u,'isorange',[-1,1],'LineWidth',1.5,'color','k','plane',true)
axis off;axis image;colorbar

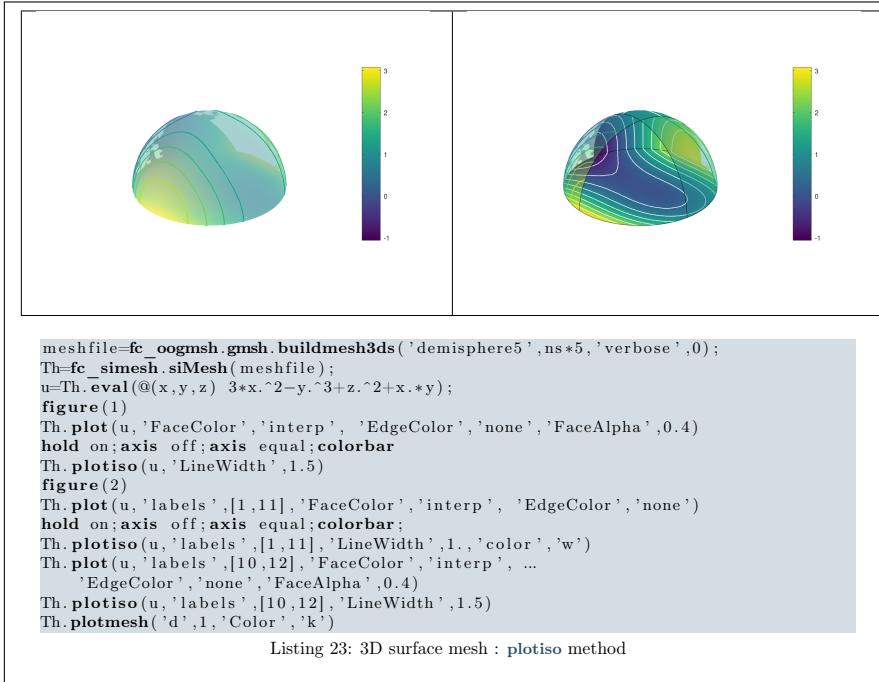
```

Listing 21: 2D mesh : `plotiso` method

**3D example** The following example use the `.geo` file `cylinderkey.geo` which is in the directory `geodir` of the toolbox. This file contains description of a 3D mesh with simplices of dimensions 1, 2 and 3.



**3D surface example** The following example use the `.geo` file `demisphere5.geo` which is in the directory `geodir` of the toolbox. This file contains description of a 3D surface mesh with simplices of dimensions 1 and 2.



### 2.5.12 slicemesh method

The **slicemesh** method displays intersection of a plane and a 3D mesh or parts of a 3D mesh defined by an **fc\_simesh.siMesh** object.

#### Syntaxe

```
Th.slicemesh(P)
Th.slicemesh(P,Name,Value, ...)
```

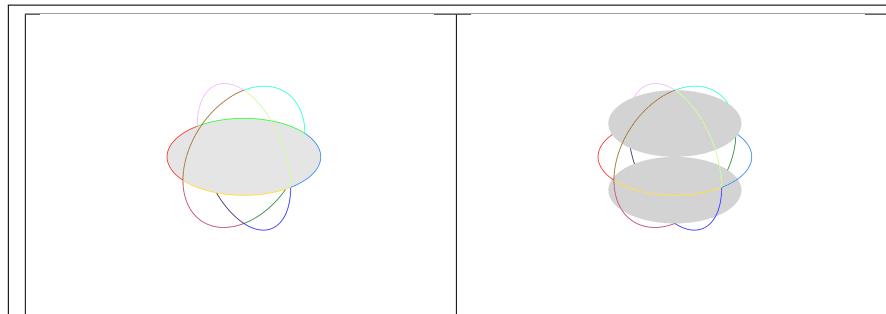
#### Description

**Th.slicemesh(P)** displays intersection of the plane defined by  $P(1)x + P(2)y + P(3)z + P(4) = 0$  and all the 3-dimensional simplices elements of **Th**, a **fc\_simesh.siMesh** object. To compute **P** one can use the function **fc\_tools.graphics.PlaneCoefs** of the **ctools** package. With this function, the array **P**, is obtained with **P=fc\_tools.graphics.PlaneCoefs(Q,V)** where **Q** is a point in the plane and **V** is a vector orthogonal to it.

**Th.slicemesh(P,Name,Value, ...)** specifies function options using one or more Name,Value pair arguments. Options of first level are

- 'color' : to specify the slice color (default : 'lightgrey', **rgb** =[0.9,0.9,0.9])
- 'labels' : to select the labels of the elements to intersect,

**3D example** The following example use the **.geo** file **ball18.geo** which is in the directory **geodir** of the toolbox. This file contains description of a 3D mesh with simplices of dimensions 1, 2 and 3.



```
meshfile=fc_oogmsh.buildmesh3d('ball18',ns*10,'verbose',0);
Th=fc_simesh.siMesh(meshfile);
figure(1)
Th.plotmesh('d',1,'LineWidth',1)
hold on;axis off;axis image;
P=fc_tools.graphics.PlaneCoefs([0 0 0],[0 0 1]);
Th.slicemesh(P,'color',0.9*[1 1 1])
figure(2)
P=[fc_tools.graphics.PlaneCoefs([0 0 -0.5],[0 0 1]); ...
    fc_tools.graphics.PlaneCoefs([0 0 0.5],[0 0 1])];
Th.plotmesh('d',1,'LineWidth',1)
hold on;axis off;axis image;
Th.slicemesh(P,'Color','LightGray')
```

Listing 24: 3D mesh : **slicemesh** method

### 2.5.13 slice method

The method `slice` method displays datas on the intersection of a plane and a 3D mesh or parts of a 3D mesh defined by an `fc_simesh.siMesh` object.

#### Syntaxe

```
Th. slice(u,P)
Th. slice(u,P,Name,Value, ...)
```

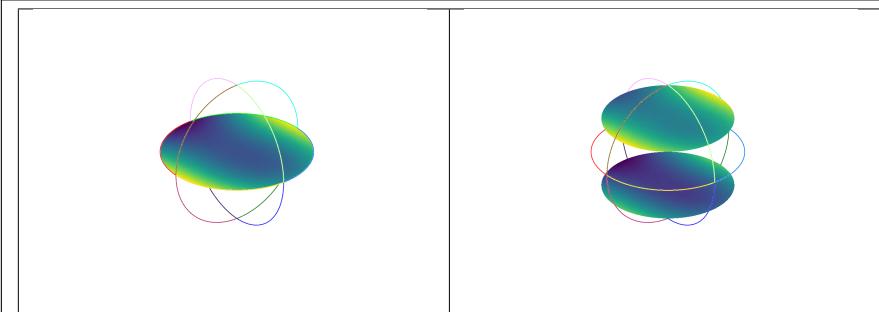
#### Description

`Th.slice(u,P)` displays `u` data on the intersection of the plane defined by  $P(1)x + P(2)y + P(3)z + P(4) = 0$  and all the 3-dimensional simplices elements of `Th`, a `fc_simesh.siMesh` object. The data `u` is an 1D-array of size `Th.nq` or `Th.nqGlobal` or `Th.nqParent`. To compute `P` one can use the function `fc_tools.graphics.PlaneCoefs` of the `fc_tools` package. With this function, the array `P`, is obtained with `P=fc_tools.graphics.PlaneCoefs(Q,V)` where `Q` is a point in the plane and `V` is a vector orthogonal to it.

`Th.slice(u,P,Name,Value, ...)` specifies function options using one or more `Name,Value` pair arguments. Options of first level are

- '`labels`' : to select the labels of the elements to intersect,

**3D example** The following example use the `.geo` file `ball18.geo` which is in the directory `geodir` of the toolbox. This file contains description of a 3D mesh with simplices of dimensions 1, 2 and 3.



```
meshfile=fc_oogmsh.buildmesh3d('ball18',ns*10,'verbose',0);
Th=fc_simesh.siMesh(meshfile);
u=Th.eval(@(x,y,z) 3*x.^2-y.^3+z.^2+x.*y+z);
figure(1)
Th.plotmesh('d',1,'LineWidth',1)
hold on;axis off;axis image;
P=fc_tools.graphics.PlaneCoefs([0 0 0],[0 0 1]);
Th.slice(u,P,'Facecolor','interp')
figure(2)
P=[fc_tools.graphics.PlaneCoefs([0 0 -0.5],[0 0 1]); ...
    fc_tools.graphics.PlaneCoefs([0 0 0.5],[0 0 1])];
Th.plotmesh('d',1,'LineWidth',1);
hold on;axis off;axis image;
Th.slice(u,P,'Facecolor','interp')
```

Listing 25: 3D mesh `:slice` method

### 2.5.14 sliceiso method

The `sliceiso` method displays isolines of data on the intersection of a plane and a 3D mesh or parts of a 3D mesh defined by an `fc_simesh.siMesh` object.

#### Syntaxe

```
Th.sliceiso(u,P)
Th.sliceiso(u,P,Name,Value, ...)
```

#### Description

`Th.sliceiso(u,P)` displays `u` data as isolines on the intersection of the plane defined by  $P(1)x + P(2)y + P(3)z + P(4) = 0$  and all the 3-dimensional simplices elements of `Th`, a `fc_simesh.siMesh` object. The data `u` is an 1D-array of size `Th.nq` or `Th.nqGlobal` or `Th.nqParent`. To compute `P` one can use the function `fc_tools.graphics.PlaneCoefs` of the `fc_tools` package. With this function, the array `P`, is obtained with `P=fc_tools.graphics.PlaneCoefs(Q,V)` where `Q` is a point in the plane and `V` is a vector orthogonal to the plane.

`Th.sliceiso(u,P,key,value, ...)` allows additional key/value pairs to be used when displaying `u`. The key strings could be

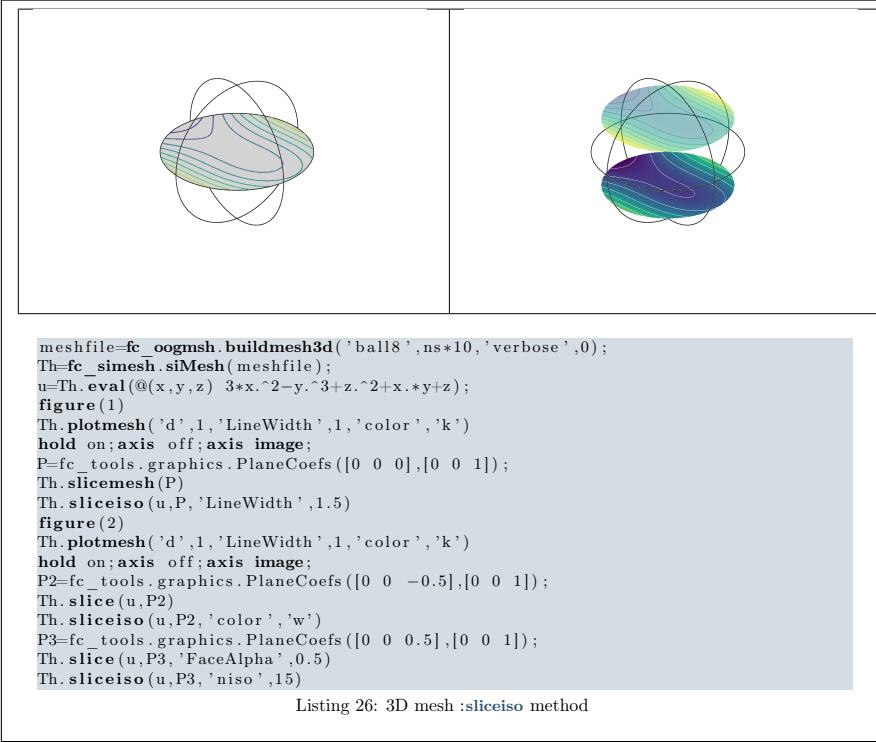
- 'labels' : to select the labels of the elements to intersect,
- 'niso' : to specify the number of isolines (default : 10)
- 'isorange' : to specify the list of isovalues (default : empty)
- 'color' : to specify one color for all isolines (default : empty)
- 'isocolorbar' : if true display a colorbar. Default is false.
- 'format' : to specify the format of the isovalues print in the colorbar. Default is '`%%g`'.

For key strings, one could also used any options of the `plot3` function.

This function accepts until 4 output arguments :

- 1st output is the colors of the isolines
- 2nd output is the isovalues of the isolines
- 3th output is the handle of the colobar iso.
- 4th output is all the handles of the isolines as an 2D-array of dimension N-by-niso, where N is the number of elementary meshes where isolines are drawn.

**3D example** The following example use the `.geo` file `ball8.geo` which is in the directory `geodir` of the toolbox. This file contains description of a 3D mesh with simplices of dimensions 1, 2 and 3.



### 2.5.15 plotquiver method

The **plotquiver** method displays vector field datas on the mesh or parts of the mesh defined by an **fc\_simesh.siMesh** object.

#### Syntaxe

```

Th.plotquiver(V)
Th.plotquiver(V,Key,Value, ...)

```

#### Description

**Th.plotquiver(V)** displays vector field **U** on all the **d**-dimensional simplices elements in dimension  $d = 2$  or  $d = 3$ . The data **V** is an 2D-array of size **Th.nq**-by-**d** or 2-by-**Th.nq**.

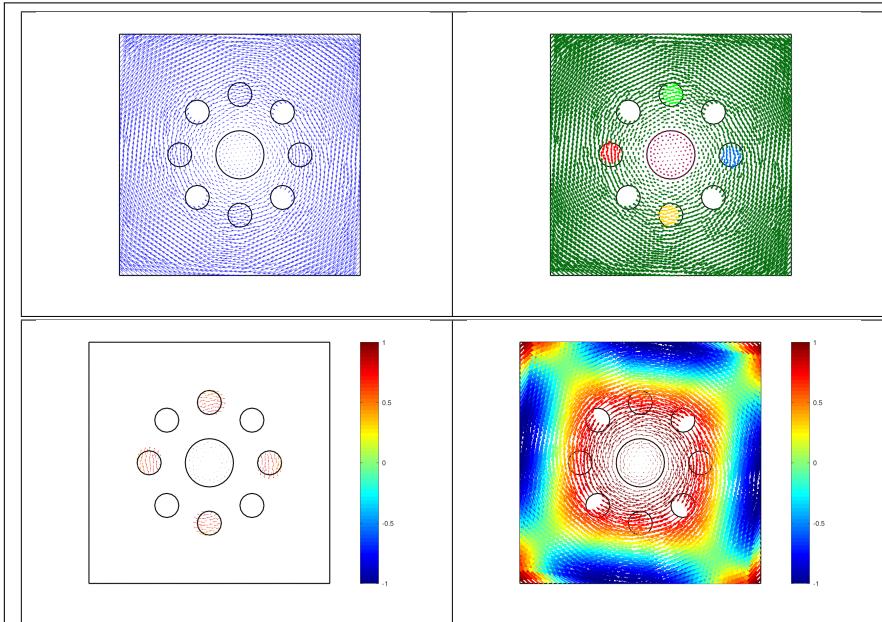
**Th.plotquiver(V,Key,Value, ...)** specifies function options using one or more **Key,Value** pair arguments. Options of first level are

- '**labels**' : to select the labels of the elements to display data,
- '**freq**' : quiver frequencie, (default : 1)
- '**scale**' : quiver scale, (default : ...)
- '**colordata**' : set colors on each quiver (default : empty ).

The options of second level depend on space dimension and '**colordata**' option. One can use any option of the following functions

- **quiver** function in dimension 2 with an empty 'colordata'
- **quiver3** function in dimension 3 with an empty 'colordata'
- **vfield3** function in dimension 2 or 3 with 'colordata' set to an 1D-array of length **Th.nq**.

**2D example** The following example use the **.geo** file **condenser11.geo**.



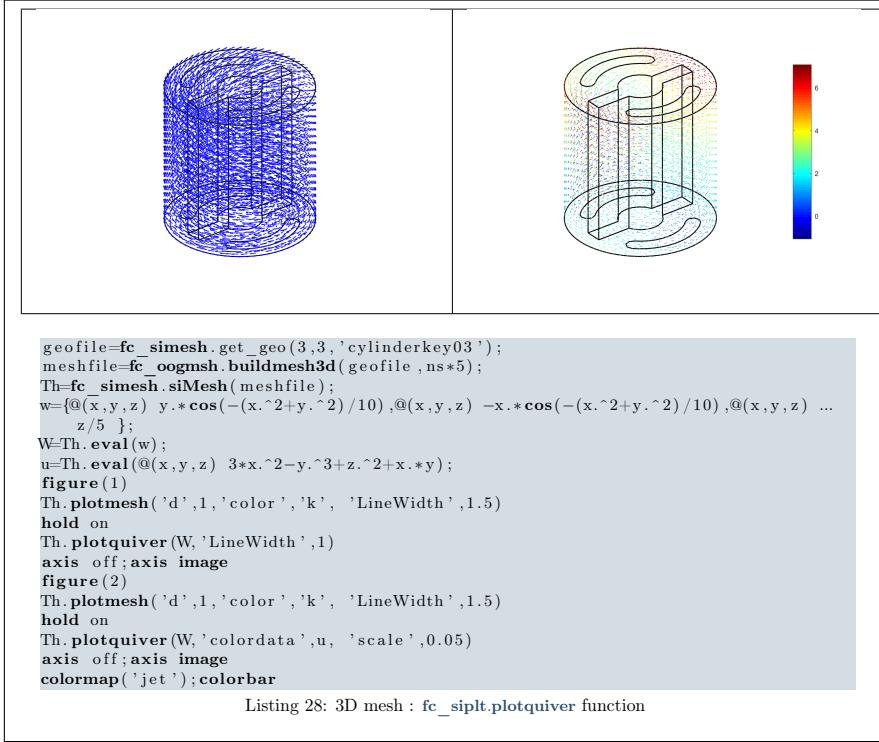
```

geofile=fc_simesh.get_geo(2,2,'condenser11');
meshfile=fc_oogmsh.buildmesh2d(geofile,25,'verbose',0);
Th=fc_simesh.siMesh(meshfile);
u=@(x,y) cos(pi*x.^2).*cos(pi*y.^2);
U=Th.eval(u);
w=@(x,y) y.*cos(-(x.^2+y.^2)/10),@(x,y) -x.*cos(-(x.^2+y.^2)/10);
W=Th.eval(w);
figure(1)
Th.plotmesh('d',1,'color','k','LineWidth',1.5)
hold on;axis off;axis image
Th.plotquiver(W)
figure(2)
Th.plotmesh('d',1,'color','k','LineWidth',1.5)
hold on;axis off;axis image
Th.plotquiver(W,'LineWidth',2,'merge',false)
figure(3)
Th.plotmesh('d',1,'color','k','LineWidth',1.5)
hold on;axis off;axis image
Th.plotquiver(W,'colordata',U,'labels',[2:2:8,20])
caxis([min(U) max(U)])
colormap('jet');colorbar
figure(4)
Th.plotmesh('d',1,'color','k','LineWidth',1.5)
hold on;axis off;axis image
Th.plotquiver(W,'colordata',U,'scale',0.2)
colormap('jet');colorbar

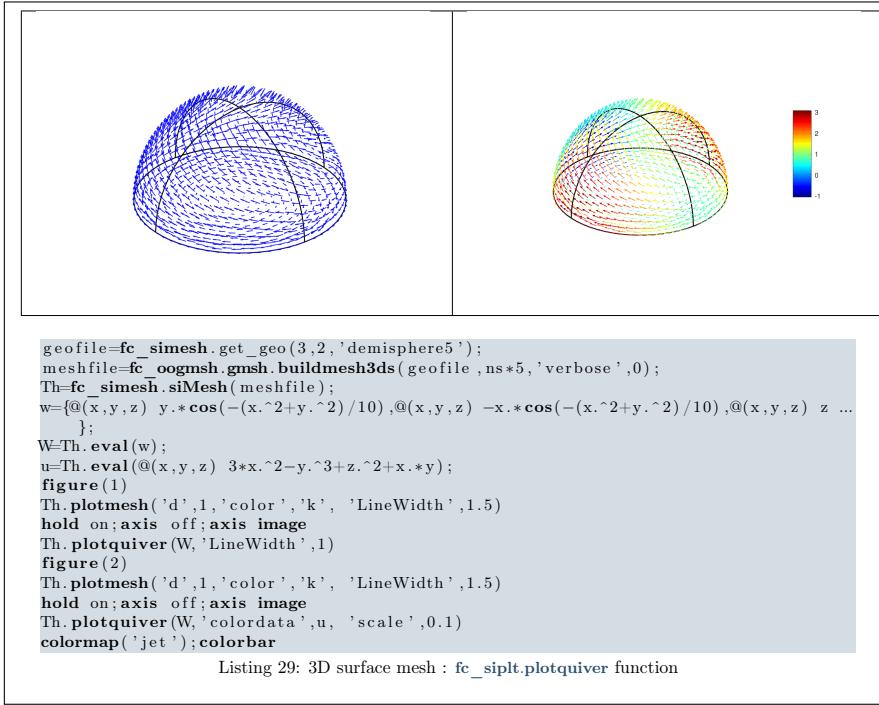
```

Listing 27: 2D mesh : **plotquiver** method

**3D example** The following example use the **.geo** file **cylinderkey03.geo**. This file contains description of a 3D mesh with simplices of dimensions 1, 2 and 3.



**3D surface example** The following example use the `.geo` file `demisphere5.geo` which is in the directory `geodir` of the toolbox. This file contains description of a 3D surface mesh with simplices of dimensions 1 and 2.



## 2.6 Hypercube as a `fc_simesh.siMesh` object

The function `fc_simesh.HyperCube` allows to create a `fc_simesh.siMesh` object representing an hypercube in any dimension. It uses the **FC-HYPERMESH** Octave package.

- `Th=fc_simesh.HyperCube(dim,N)` : return a `fc_simesh.siMesh` object representing an hypercube in dimension `dim` and ...
- `Th=fc_simesh.HyperCube(dim,N,Key,Value,...)` :

### 2.6.1 2D hypercube

In Listing 30 a usage example generating a 2D hypercube as a `fc_simesh.siMesh` object is given. This `fc_simesh.siMesh` object is representing in Figure 4 by using the **FC-SIPLT** package.

```
Listing 30: 2D Hypercube fc_simesh.siMesh object generated with the function siMesh.HyperCube
Th=fc_simesh.HyperCube(2,10);
disp(Th)
```

Output

```
fc_simesh.siMesh with properties:
  bbox: [ 0 1 0 1 ] (1x4 double)
    d: 2 double
    dim: 2 double
    nq: 121 double
  nqParents: 121 double
    nsTh: 9 double
    other: []
      sTh: (1x9 cell)
  sThboundlabs: []
    sThcolors: (9x3 double)
    sThgeolab: []
      sThlab: [ 1 1 2 3 4 1 2 3 4 ] (1x9 double)
  sThpartlabs: []
    sThphyslab: 1 double
      sThsimp: [ 2 1 1 1 1 0 0 0 0 ] (1x9 double)
    toGlobal: (1x121 double)
    toParent: (1x121 double)
    toParents: (1x1 cell)
```

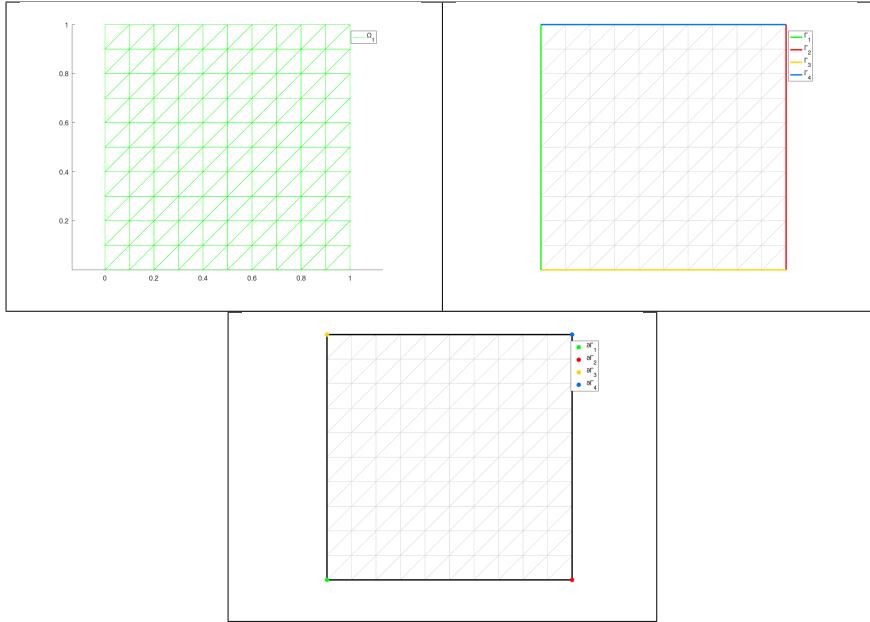


Figure 4: 2D Hypercube `fc_simesh.siMesh` object generated with the function `fc_simesh.HyperCube`, representation of the elementary meshes with 2-simplices (top left), 1-simplices (top right) and 0-simplices (bottom)

### 2.6.2 3D hypercube

In Listing 31 a usage example generating a 3D hypercube as a `fc_simesh.siMesh` object is given. This `fc_simesh.siMesh` object is representing in Figure 5 by using the the `FC-SIPLT` package. .

```
Listing 31: 3D Hypercube fc_simesh.siMesh object generated with the function fc_simesh.HyperCube
Th=fc_simesh.HyperCube(3,10);
disp(Th)

Output
fc_simesh.siMesh with properties:
  bbox: [ 0 1 0 1 0 1 ] (1x6 double)
    d: 3 double
    dim: 3 double
    nq: 1331 double
    nqParents: 1331 double
    nsTh: 27 double
    other: []
      sTh: (1x27 cell)
  sThboundlabs: []
    sThcolors: (27x3 double)
    sTheolab: []
      sThlab: (1x27 double)
  sThpartlabs: []
  sThphyslab: 1 double
    sThsimp: (1x27 double)
    toGlobal: (1x1331 double)
    toParent: (1x1331 double)
    toParents: (1x1 cell)
```

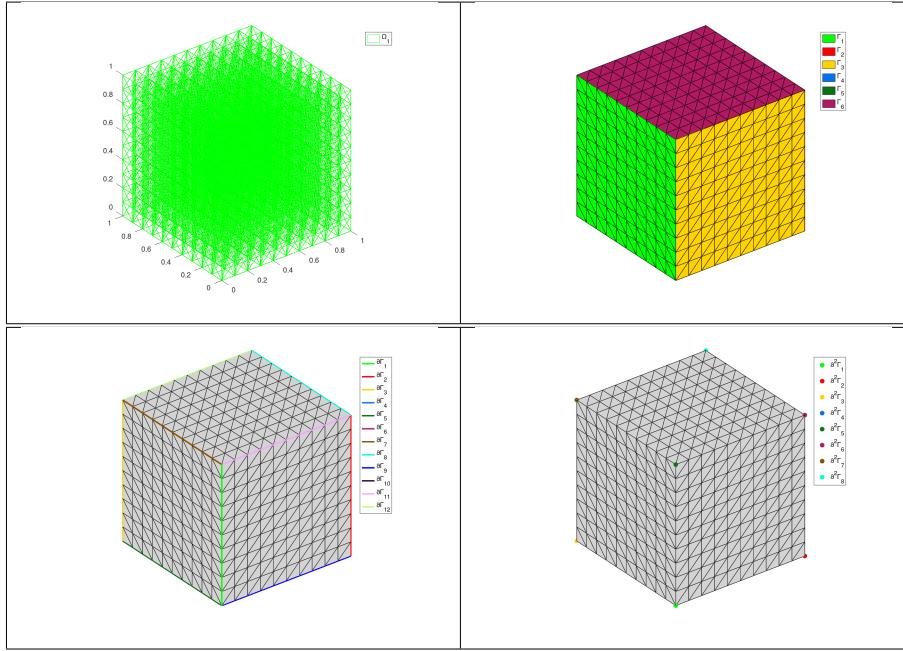


Figure 5: 3D Hypercube `fc_simesh.siMesh` object generated with the function `siMesh.HyperCube`, representation of the elementary meshes with 3-simplices (top left), 2-simplices (top right), 1-simplices (bottom left) and 0-simplices (bottom right)

### 2.6.3 4D hypercube

In Listing 32 a usage example generating a 4D hypercube as a `fc_simesh.siMesh` object is given.

```
Listing 32: function fc_simesh.HyperCube
Th=fc_simesh.HyperCube(4,10);
disp(Th)
```

Output

```
fc_simesh.siMesh with properties:
    bbox: [ 0 1 0 1 0 1 0 1 ] (1x8 double)
    d: 4 double
    dim: 4 double
    nq: 14641 double
    nqParents: 14641 double
    nsTh: 81 double
    other: []
    sTh: (1x81 cell)
sThboundlabs: []
sThcolors: (81x3 double)
sTheolab: []
sThlab: (1x81 double)
sThpartlabs: []
sThphyslab: 1 double
sThsimp: (1x81 double)
toGlobal: (1x14641 double)
toParent: (1x14641 double)
toParents: (1x1 cell)
```

#### 2.6.4 5D hypercube

In Listing 32 a usage example generating a 5D hypercube as a `fc_simesh.siMesh` object is given.

```

Listing 33: function siMesh.HyperCube
Th=fc_simesh.HyperCube(5,6);
disp(Th)

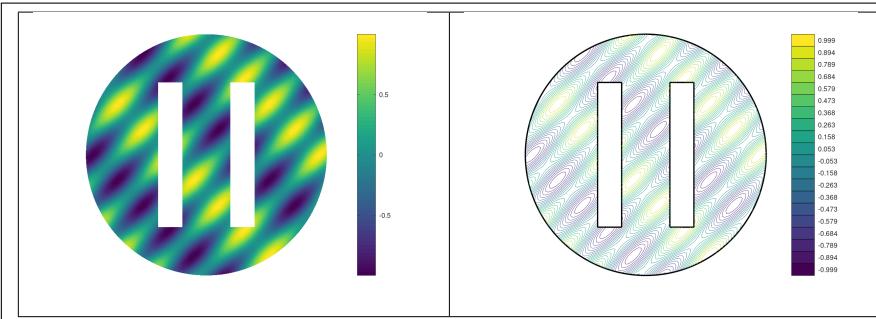
Output
fc_simesh.siMesh with properties:
  bbox: [ 0 1 0 1 0 1 0 1 0 1 ] (1x10 double)
    d: 5 double
    dim: 5 double
    nq: 16807 double
    nqParents: 16807 double
    nsTh: 243 double
    other: []
    sTh: (1x243 cell)
    sThboundlabs: []
    sThcolors: (243x3 double)
    sThegeolab: []
    sThlab: (1x243 double)
    sThpartlabs: []
    sThphyslab: 1 double
    sThsimp: (1x243 double)
    toGlobal: (1x16807 double)
    toParent: (1x16807 double)
    toParents: (1x1 cell)
```

## 3 Graphic representations on `fc_simesh.siMeshElt` object

Actually the `fc_siplt` package is used as graphic kernel of the `fc_simesh.siMesh` objects. So for each methods `plot`, `plotmesh`, `plotiso`, `plotquiver`, `slice`, `slicemesh` and `sliceiso` one can refers to the corresponding functions of the `fc_siplt` package:  
For a `fc_simesh.siMesh` object, named `Th`, we have

- `Th.plotmesh(...)`: calls of the function `fc_siplt.plotmesh(Th,...)`
- `Th.plot(...)`: calls of the function `fc_siplt.plot(Th,...)`
- `Th.plotiso(...)`: calls of the function `fc_siplt.plotiso(Th,...)`
- `Th.plotquiver(...)`: calls of the function `fc_siplt.plotquiver(Th,...)`
- `Th.slicemesh(...)`: calls of the function `fc_siplt.slicemesh(Th,...)`
- `Th.slice(...)`: calls of the function `fc_siplt.slice(Th,...)`
- `Th.sliceiso(...)`: calls of the function `fc_siplt.sliceiso(Th,...)`

### 3.1 Data 2D mesh

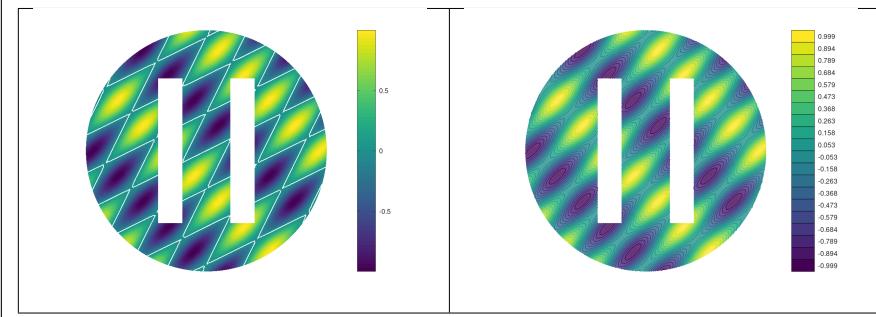


```

meshfile=fc_oogmsh.gmsh.buildmesh2d('condenser',10);
Th=fc_simesh.siMesh(meshfile);
u=@(x,y) cos(2*x-y).*sin(x-2*y);
U=Th.eval(u);
figure(1);
Th.plot(U)
shading interp;axis off;axis image
colorbar
figure(2)
Th.plotmesh('d',1,'color','k','Linewidth',2);
hold on;axis off;axis image
Th.plotiso(U,'niso',20,'isocolorbar',true,'format','%.3f');

```

Listing 34: Data representations on a 2D mesh

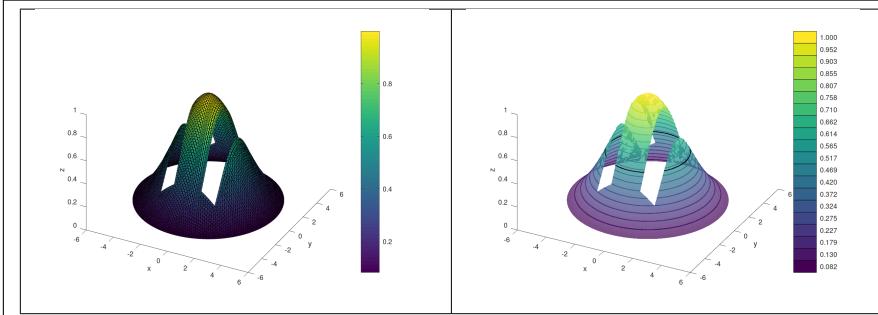


```

meshfile=fc_oogmsh.gmsh.buildmesh2d('condenser',10);
Th=fc_simesh.siMesh(meshfile);
u=@(x,y) cos(2*x-y).*sin(x-2*y);
U=Th.eval(u);
figure(1);
Th.plot(U)
hold on
Th.plotiso(U,'isorange',0,'color','w','Linewidth',1.5);
axis off, axis image, shading interp, colorbar
figure(2)
Th.plot(U,'FaceAlpha',0.8)
hold on
[Colors,isorange]=Th.plotiso(U,'niso',20,'Linewidth',1.5);
axis off, axis image, shading interp
fc_tools.graphics.colorbarIso(Colors,isorange,'%.3f')

```

Listing 35: Data representations on a 2D mesh. White lines are zero isolines (left)



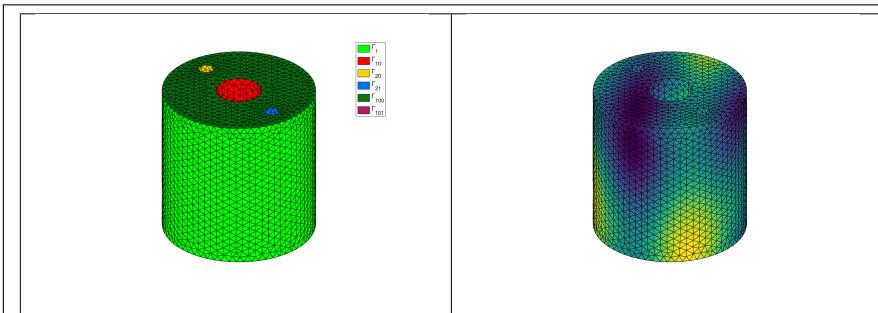
```

meshfile=fc_oogmsh.gmsh.buildmesh2d('condenser',7);
Th=fc_simesh.siMesh(meshfile);
u=@(x,y)exp(-(x.^2+y.^2)/10);
U=Th.eval(u);
figure(1)
Th.plot(U)
colorbar
view(27,39)
xlabel('x'),ylabel('y'),zlabel('z')
figure(2);
Th.plot(U,'FaceAlpha',0.7)
hold on
Th.plotiso(U,'nis0',20,'Linewidth',1.5,'isocolorbar',true,'format','%3f');
Th.plotiso(U,'isorange',0.5,'color','k','Linewidth',1.5);
shading interp
view(27,39)
xlabel('x'),ylabel('y'),zlabel('z')

```

Listing 36: Data representations on a 2D mesh. Black lines are zero isolines (right)

### 3.2 3D mesh

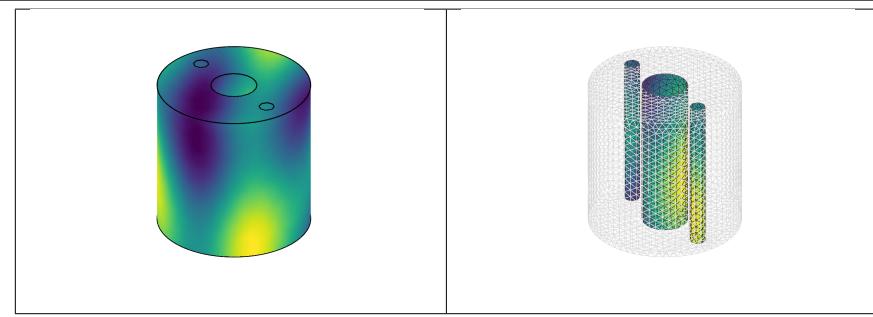


```

meshfile=fc_oogmsh.gmsh.buildmesh3d('cylinder3holes',ns*5);
Th=fc_simesh.siMesh(meshfile);
u=@(x,y,z) cos(2*x-y-z).*sin(x-2*y+z);
U=Th.eval(u);
figure(1);
Th.plotmesh('d',2,'inlegend',true)
axis off; axis image; legend('show')
figure(2)
Th.plot(U,'d',2)
axis off; axis image

```

Listing 37: Data representations on a 3D mesh

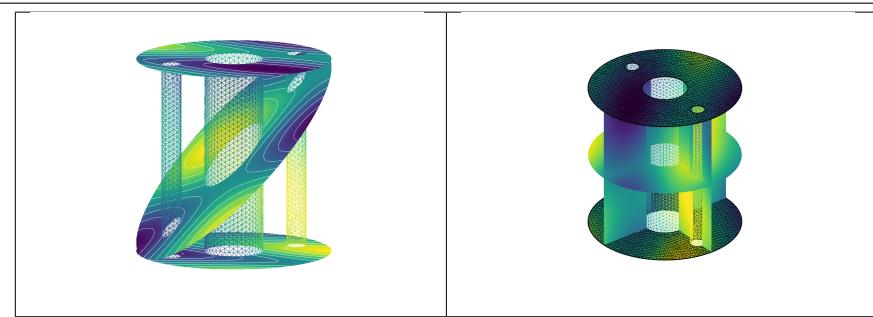


```

meshfile=fc_oogmsh.gmsh.buildmesh3d('cylinder3holes',ns*5);
Th=fc_simesh.siMesh(meshfile);
u=@(x,y,z) cos(2*x-y-z).*sin(x-2*y+z);
U=Th.eval(u);
figure(1)
Th.plot(U,'d',2)
caxis([min(U),max(U)])
axis off;axis image
shading interp
hold on
Th.plotmesh('d',1,'color','k','Linewidth',1.5)
figure(2)
Th.plotmesh('d',2,'FaceColor','none','EdgeColor','LightGray')
hold on;axis off;axis image;caxis([min(U),max(U)])
Th.plot(U,'d',2,'labels',[10,20,21])

```

Listing 38: Data representations on a 3D mesh



```

meshfile=fc_oogmsh.gmsh.buildmesh3d('cylinder3holes',ns*10);
Th=fc_simesh.siMesh(meshfile);
u=@(x,y,z) cos(2*x-y-z).*sin(x-2*y+z);
U=Th.eval(u);
figure(1);
P=fc_tools.graphics.PlaneCoefs([0 0 1],[0 1 1]);
Th.slice(U,P,'FaceColor','interp','EdgeColor','none')
axis off, axis image, hold on
Th.plot(U,'d',2,'labels',[100,101], 'FaceColor','interp','EdgeColor','none')
caxis([min(U),max(U)])
isorange=linspace(min(U),max(U),10);
Th.plot(U,'d',2,'labels',[10,20,21], 'FaceColor','none','EdgeColor','interp')
Th.plotiso(U,'labels',[100,101], 'isorange',isorange, 'color','w')
Th.sliceiso(U,P,'isorange',isorange, 'color','w')
view(-114,11)
figure(2)
P=[fc_tools.graphics.PlaneCoefs([0 0 1],[1 0 0]); ...
    fc_tools.graphics.PlaneCoefs([0 0 1],[0 1 0]); ...
    fc_tools.graphics.PlaneCoefs([0 0 1],[0 0 1])];
Th.slice(U,P,'FaceColor','interp','EdgeColor','none')
hold on;axis off, axis image;caxis([min(U),max(U)])
Th.plot(U,'d',2,'labels',[100,101], 'FaceColor','interp')
Th.plot(U,'d',2,'labels',[10,20,21], 'FaceColor','none','EdgeColor','interp')
Th.plotmesh('d',1,'Color','k','Linewidth',1.5)

```

Listing 39: Data representations on a 3D mesh

### 3.2.1 Mapping of the unit ball

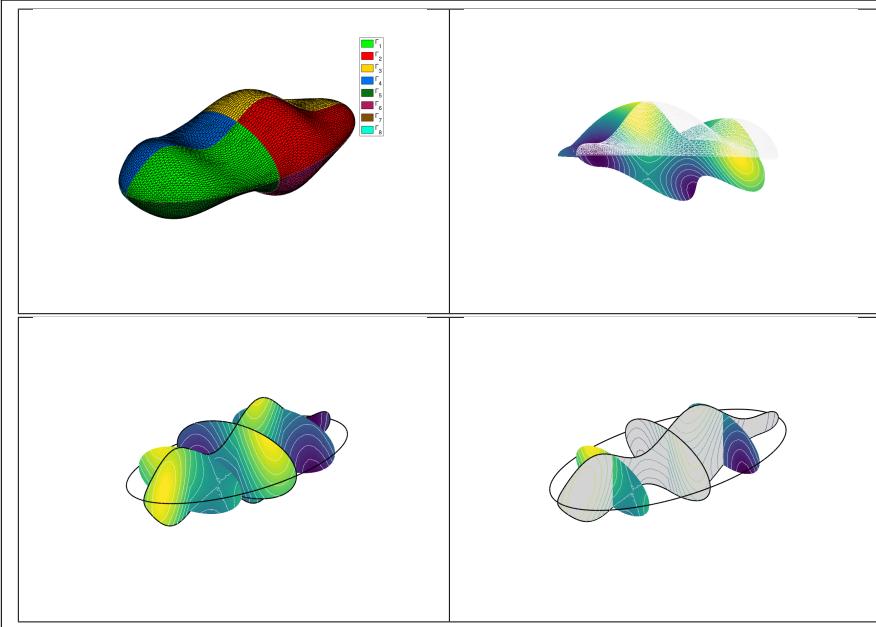
The 3D domain  $\Omega$  is constructed by mapping a discretization of the unit ball onto  $\Omega$  by

$$F(y_1, y_2, y_3) = \begin{pmatrix} 2y_1 \\ y_2 \\ \frac{1}{2}y_3(1 + \frac{1}{2}\sin(2\pi y_1)) \end{pmatrix}, \quad \forall \mathbf{y} = (y_1, y_2, y_3), \text{ such that } \|\mathbf{y}\|_2 \leq 1$$

We represent the function

$$u(x, y, z) = \cos(2x - y - z)\sin(x - 2y + z)$$

on  $\Omega$  by mapping the unit ball obtained from **gmsh** with **ball8.geo**.



```

trans=@(q) [2*q(1,:);q(2,:);0.5*q(3,:)*(1+0.5*sin(2*pi*q(1,:)))];
meshfile=fc_oogmsh.gmsh.buildmesh3d('ball18',ns*10);
Th=fc_simesh.siMesh(meshfile,'trans',trans);
u=@(x,y,z) cos(2*x-y-z).*sin(x-2*y+z);
U=Th.eval(u);
U=Th.eval(u);
figure(1)
Th.plotmesh('d',2,'inlegend',true);
axis off;axis image;legend('show')
figure(2)
P=fc_tools.graphics.PlaneCoefs([0 0 0],[0 1 1]);
Th.slice(U,P)
hold on;caxis([min(U),max(U)])
Th.plot(U,'d',2,'labels',[1,2], 'EdgeColor','None')
isorange=linspace(min(U),max(U),15);
Th.plotmesh('d',2,'labels',[3,4], 'FaceColor','none', 'EdgeColor',0.95*[1,1,1])
Th.plotiso(U,'labels',[3,4],'isorange',isorange, 'color','w')
Th.sliceiso(U,P,'isorange',isorange, 'color','w')
axis off;axis image
view(127,-1)
figure(3)
P=[fc_tools.graphics.PlaneCoefs([0 0 1],[1 0 0]); ...
    fc_tools.graphics.PlaneCoefs([0 0 1],[0 1 0]); ...
    fc_tools.graphics.PlaneCoefs([0 0 1],[0 0 1]); ...
    fc_tools.graphics.PlaneCoefs([-1 0 0],[1 0 0]); ...
    fc_tools.graphics.PlaneCoefs([1 0 0],[1 0 0])];
Th.slice(U,P, 'FaceColor','interp', 'EdgeColor','none')
hold on
Th.sliceiso(U,P,'isorange',isorange, 'color','w')
Th.plotmesh('d',1, 'color','k', 'Linewidth',1.5)
axis off;axis image
view(-52,20)
figure(4)
Th.slicemesh(P(1:2,:),'Color','LightGray')
hold on;axis off;axis image;view(-52,20)
Th.sliceiso(U,P(1:2,:),'isorange',isorange)
Th.slice(U,P(3:5,:));
Th.sliceiso(U,P(3:5,:),'isorange',isorange, 'color','w')
Th.plotmesh('d',1, 'color','k', 'Linewidth',1.5)

```

Listing 40: Data representations on a 3D mesh

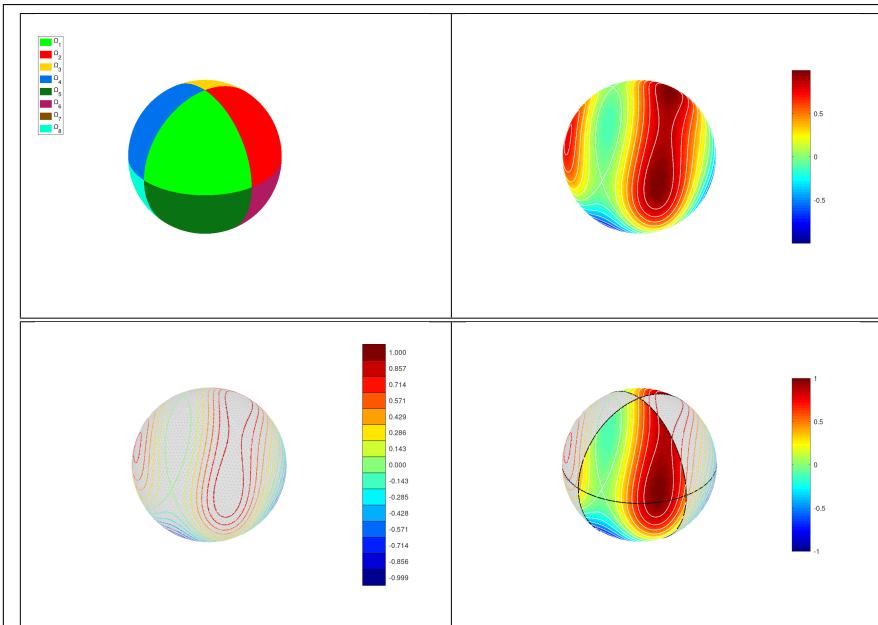
### 3.3 3D surface meshes

#### 3.3.1 Unit sphere

We represent the function

$$u(x, y, z) = \cos(2x - y - z \sin(x - 2y + z))$$

on the unit sphere obtained from gmsh with `sphere8surf.geo`.



```

meshfile=fc_oogmsh.gmsh.buildmesh3ds('sphere8surf',ns*10);
Th=fc_simesh.siMesh(meshfile);
u=@(x,y,z) cos(2*x-y-z).*sin(x-2*y+z);
U=Th.eval(u);
figure(1)
Th.plotmesh('inlegend',true,'EdgeColor','None')
axis off; axis image
legend('show','Location','NorthWestOutside')
figure(2);
colormap(jet)
Th.plot(U,'d',2)
hold on; axis off, axis image
Th.plotiso(U,'niso',15,'color','w','Linewidth',1)
caxis([min(U),max(U)])
shading interp
colorbar;
figure(3)
colormap(jet)
Th.plotmesh('FaceColor',0.9*[1 1 1], 'EdgeColor',0.8*[1 1 1]);
hold on; axis off, axis image
Th.plotiso(U,'niso',15,'Linewidth',1.5, 'isocolorbar',true,'format','%.3f')
figure(4);
colormap(jet)
Th.plot(U,'d',2,'labels',[1:2:8], 'FaceColor','interp','EdgeColor','None')
hold on
Th.plotiso(U,'labels',[1:2:8], 'niso',15,'color',[1 1 1], 'Linewidth',1)
Th.plotmesh('labels',[2:2:8], 'FaceColor',0.9*[1 1 1], 'EdgeColor',0.8*[1 1 1]);
Th.plotiso(U,'labels',[2:2:8], 'niso',15, 'Linewidth',1.5)
axis off, axis image
Th.plotmesh('d',1,'color',[0 0 0], 'Linewidth',1.5)
colorbar

```

Listing 41: Data representations on a 3D surface mesh

### 3.3.2 Mapping of the unit sphere

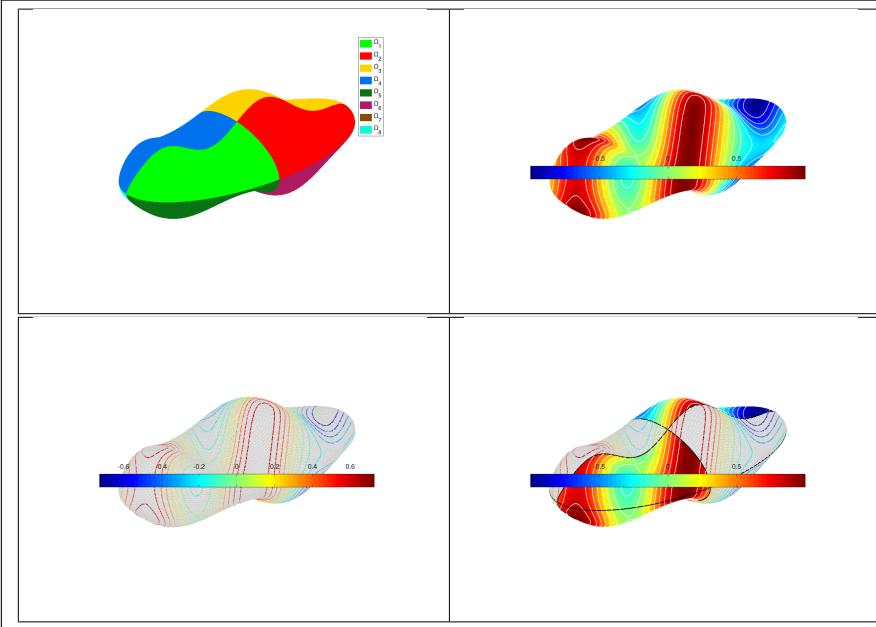
The hypersurface is constructed by mapping a discretization of the unit sphere  $S^2$  onto the surface  $\Omega$  by

$$F(y_1, y_2, y_3) = \begin{pmatrix} 2y_1 \\ y_2 \\ \frac{1}{2}y_3(1 + \frac{1}{2}\sin(2\pi y_1)) \end{pmatrix}, \quad \forall \mathbf{y} = (y_1, y_2, y_3) \in S^2$$

We represent the function

$$u(x, y, z) = \cos(2x - y - z)\sin(x - 2y + z)$$

on the surface  $\Omega$  by mapping the unit sphere obtained from `gmsh` with `sphere8surf.geo`.



```

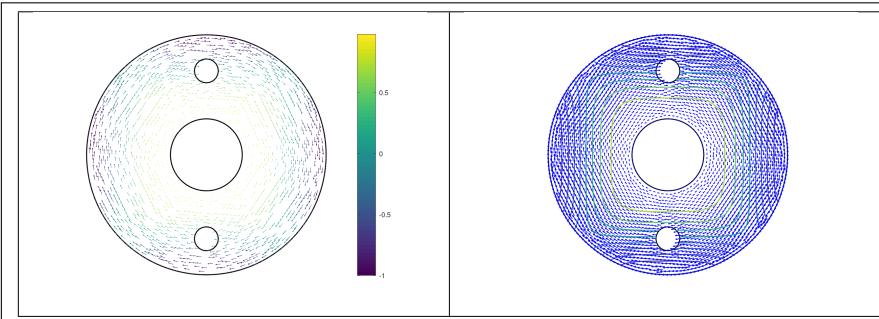
meshfile=fc_oogmsh.gmsh.buildmesh3ds('sphere8surf',ns*10);
Th=fc_simesh.siMesh(meshfile);
u=@(x,y,z) cos(2*x-y-z).*sin(x-2*y+z);
U=Th.eval(u);
figure(1)
Th.plotmesh('inlegend',true,'EdgeColor','None')
axis off; axis image
legend('show','Location','NorthWestOutside')
figure(2);
colormap(jet)
Th.plot(U,'d',2)
hold on; axis off, axis image
Th.plotiso(U,'niso',15,'color','w','Linewidth',1)
caxis([min(U),max(U)])
shading interp
colorbar;
figure(3)
colormap(jet)
Th.plotmesh('FaceColor',0.9*[1 1 1], 'EdgeColor',0.8*[1 1 1]);
hold on; axis off, axis image
Th.plotiso(U,'niso',15,'Linewidth',1.5, 'isocolorbar',true,'format','%3f')
figure(4);
colormap(jet)
Th.plot(U,'d',2,'labels',[1:2:8],'FaceColor','interp','EdgeColor','None')
hold on
Th.plotiso(U,'labels',[1:2:8],'niso',15,'color',[1 1 1], 'Linewidth',1)
Th.plotmesh('labels',[2:2:8], 'FaceColor',0.9*[1 1 1], 'EdgeColor',0.8*[1 1 1]);
Th.plotiso(U,'labels',[2:2:8],'niso',15, 'Linewidth',1.5)
axis off, axis image
Th.plotmesh('d',1,'color',[0 0 0], 'Linewidth',1.5)
colorbar

```

Listing 42: Data representations on a 3D surface mesh

## 3.4 Vector field representation on meshes

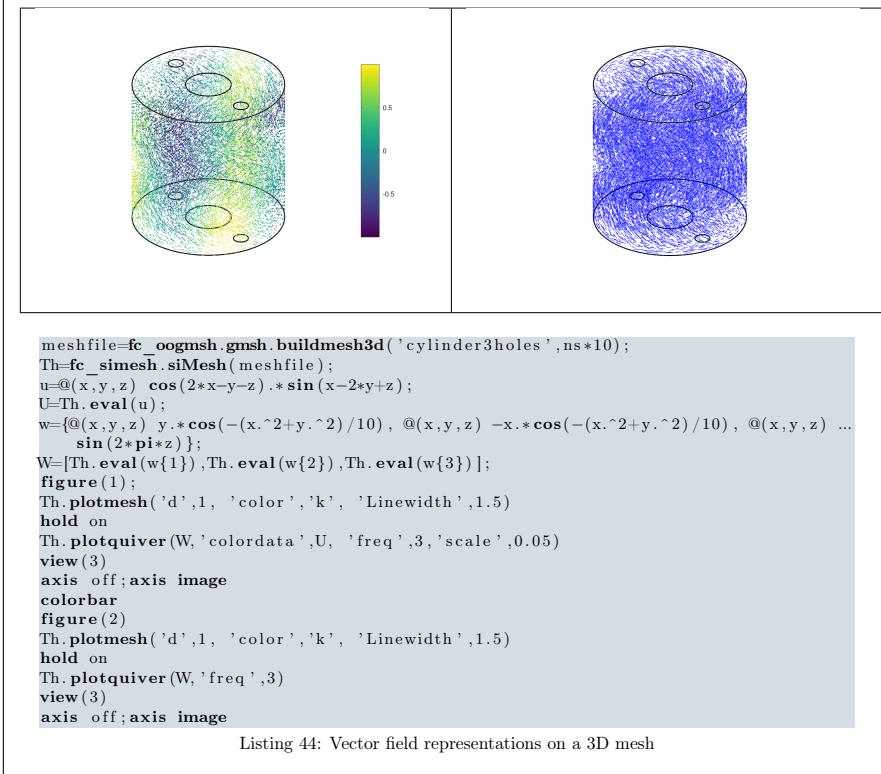
### 3.4.1 2D mesh



```
meshfile=fc_oogmsh.gmsh.buildmesh2d('disk3holes',30);
Th=fc_simesh.siMesh(meshfile);
u=@(x,y) cos(pi*x.^2).*cos(pi*y.^2);
U=Th.eval(u);
w=@(x,y) y.*cos(-(x.^2+y.^2)/10), @(x,y) -x.*cos(-(x.^2+y.^2)/10);
W=Th.eval(w);
figure(1);
Th.plotmesh('d',1,'color','k','LineWidth',1.5)
hold on
Th.plotquiver(W,'colordata',U,'freq',2,'scale',0.05)
axis off;axis image
colorbar
figure(2)
Th.plotmesh('d',1,'color','k','LineWidth',1.5)
hold on
Th.plotquiver(W,'LineWidth',1,'scale',0.05)
Th.plotiso(U,'LineWidth',1.5)
axis off;axis image
colormap('jet')
```

Listing 43: Vector field representations on a 2D mesh

### 3.4.2 3D mesh



### 3.4.3 3D surface mesh

```

meshfile=fc_oogmsh.gmsh.buildmesh3ds('sphere8surf',ns*10);
Th=fc_simesh.siMesh(meshfile);
u=@(x,y,z) cos(2*x-y-z).*sin(x-2*y+z);
U=Th.eval(u);
w=@(x,y,z) x;@(x,y,z) y; @(x,y,z) z;
W=[Th.eval(w{1}),Th.eval(w{2}),Th.eval(w{3})];
figure(1)
Th.plotmesh('labels',1:2:8, 'FaceColor','none', 'EdgeColor',0.8*[1 1 1], ...
            'EdgeAlpha',0.3);
hold on
Th.plotiso(U,'labels',[1:2:8], 'niso',15, 'Linewidth',1);
Th.plotquiver(W,'colordata',U, 'labels',1:2:8, 'freq',3, 'scale',0.1)
Th.plot(U,'d',2,'labels',[2:2:8]);
axis off;axis image

```

Listing 45: Vector field representation on a 3D surface mesh

# Appendices

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## B References

---

- [1] F. Cuvelier. fc\_oogmsh: an object-oriented Octave package to run **gmsh** and read mesh files. <http://www.math.univ-paris13.fr/~cuvelier/software/>, 2017. User's Guide.
- [2] F. Cuvelier. fc\_siplt: an add-on to the fc\_simesh Octave package for displaying simplices meshes or datas on simplices meshes. <http://www.math.univ-paris13.fr/~cuvelier/software/>, 2017. User's Guide.
- [3] F. Cuvelier. fc\_hypermesh: a object-oriented Octave package to mesh any d-orthotopes (hyperrectangle in dimension d) and their m-faces with high order simplices or orthotopes. <http://www.math.univ-paris13.fr/~cuvelier/software/>, 2019. User's Guide.

# Informations for git maintainers of the Octave package

git informations on the packages used to build this manual					
-----					
name : fc-simesh tag : 0.4.0 commit : 9e234702263df3e1dc19cff57bbdf5248859725 date : 2020-02-20 time : 10-01-30 status : 0					
-----					
name : fc-tools tag : 0.0.30 commit : 42054f06c3f484c5fc7d0a0cb425d727b50e8994 date : 2020-02-18 time : 06-46-53 status : 0					
-----					
name : fc-bench tag : 0.1.2 commit : 666dc60d1277f5fa9c99dee4ae1c33270f22c57d date : 2020-02-16 time : 06-38-46 status : 0					
-----					
name : fc-hypremesh tag : 1.0.3 commit : c520b34cf7eb0dbf9e4ecd459fd7162db73cc58 date : 2020-02-16 time : 08-34-19 status : 0					
-----					
name : fc-amat tag : 0.1.2 commit : 957340f6e71d805bdb8b9d04c434b24fd3f92591 date : 2020-02-16 time : 06-39-42 status : 0					
-----					
name : fc-meshtools tag : 0.1.3 commit : cdbc41bc98af4e4facc1746024aced1f21aae53 date : 2020-02-17 time : 10-52-56 status : 0					
-----					
name : fc-graphics4mesh tag : 0.1.1 commit : d8e283fc3e1ce5fac855064062e196750a0a0cd4 date : 2020-02-19 time : 08-50-23 status : 0					
-----					
name : fc-oogmsh tag : 0.2.2 commit : 90fc9826fea6eb8dd66afc3a58677564c8f7f442 date : 2020-02-17 time : 13-31-05 status : 0					
-----					
name : fc-sipit tag : 0.2.0 commit : e9cac51a2239a52ce34125ddcd2f1de4377dda5f date : 2020-02-20 time : 09-50-32 status : 0					
-----					

```
git informations on the LATEX package used to build this manual
```

```
-----  
name : fctools  
tag :  
commit : 57968c4a96c2593cccc9da9efd3e52b2ff012cb5  
date : 2020-02-07  
time : 06:41:09  
status : 1  
-----
```

Using the remote configuration repository:

```
url      ssh://lagagit/MCS/Cuvelier/Matlab/fc-config  
commit  b837af396f81fb38264a3affb2f2d5c779818b6c
```