



## MODELLING THE COVID-19 PANDEMIC REQUIRES A MODEL... BUT ALSO DATA!

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Colloquium, université Paris 13

#### https://coronavirus.jhu.edu/map.html



#### CSSEGISandData / COVID-19

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 O Watch
 932
 ★ Star
 22.2k
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 13.2k

♦ Code ① Issues 1,318 ⑦ Pull requests 254 ◎ Actions Ⅲ Projects 0 ⑧ Security 0 III Insights

Branch: master  COVID-19 / csse_covid_19_data / csse_covid_19_time_series /		Create new file	Find file	History
CSSEGISandData automated update		Latest commit 8390ba6 13 hours ago		
B .gitignore	update	3 months ago		
Errata.csv	Update Errata.csv		8 da	ays ago
README.md	Update README	18 days ago		
time_series_covid19_confirmed_US.csv	automated update	13 hours ago		
time_series_covid19_confirmed_global.csv	automated update	13 hours ago		
time_series_covid19_deaths_US.csv	automated update	13 hours ago		
time_series_covid19_deaths_global.csv	automated update	13 hours ago		
time_series_covid19_recovered_global.csv	automated update	13 hours ago		

#### E README.md

#### Time series summary (csse\_covid\_19\_time\_series)

This folder contains daily time series summary tables, including confirmed, deaths and recovered. All data is read in from the daily case report. The time series tables are subject to be updated if inaccuracies are identified in our historical data. The daily reports will not be adjusted in these instances to maintain a record of raw data.

Two time series tables are for the US confirmed cases and deaths, reported at the county level. They are named time\_series\_covid19\_confirmed\_US.csv , time\_series\_covid19\_deaths\_US.csv , respectively.

#### Cumulated number of confirmed cases



#### Cumulated number of deaths



• The objective **is not** to build a model... and try to "calibrate" it in order to fit the data as well as possible

- The objective **is not** to build a model... and try to "calibrate" it in order to fit the data as well as possible
- The objective is to develop a model
  - for the observed data, and validated by the data,
  - that provides good short-term predictions,
  - that is mechanistic **and** parsimonious,
  - that is implemented as an open-access interactive tool.





#### Marino Gatto talk





- E<sub>i</sub>: exposed in *i* P<sub>i</sub>: pre-symptomatic infectious in i I: symptomatic infectious in i A<sub>i</sub>: asymptomatic/mildly symptomatic infectious in i
- H<sub>i</sub>, Q<sub>i</sub>: Hospitalized, Quarantined and isolated in i D<sub>i</sub>, R<sub>i</sub>: Deceased, Recovered in i





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S<sub>i</sub>: susceptibles in site i

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HE MODEL OF COVID-1



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HE MODEL OF COVID-1





$$\dot{S}(t)=-etarac{S(t)}{N}I(t)$$

$$\dot{I}\left(t
ight)=etarac{S(t)}{N}I(t)-\mu I(t)-
u I(t)$$

$$\dot{R}(t) = \mu I(t)$$

$$\dot{H}(t) = \nu I(t) - \lambda H(t)$$

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HE MODEL OF COVID-1



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R not needed for fitting the data



$$\dot{I}(t) = \beta I(t) - \mu I(t) - \nu I(t)$$

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HE MODEL OF COVID-1



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The transmission rate  $\beta$  changes over time



$$\dot{I}(t) = eta(t)I(t) - \mu I(t) - 
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HE MODEL OF COVID-1



$$egin{aligned} \dot{I}(t) &= eta(t)I(t) - \mu I(t) - 
u I(t) \ \dot{H}(t) &= 
u I(t) - \lambda H(t) \ \dot{D}(t) &= \lambda H(t) \ eta(t) &= eta_0 + a\,t + \sum_{k=1}^K h_k\,t imes extsf{1}\{t \geq au_k\} \end{aligned}$$

We will use a piecewise linear function for  $\boldsymbol{\beta}$ 

HE MODEL OF COVID-19

#### Available data:

•  $w = (w_j, j = 1, 2, ...)$  where  $w_j$  is the cumulated number of confirmed cases

Then,  $w_i - w_{i-1}$  is the number of new confirmed cases on day j

•  $d = (d_i, j = 1, 2, ...)$  where  $d_i$  is the cumulated number of deaths

Then,  $d_i - d_{i-1}$  is the number of new deaths on day j







#### The data:

The epidemiological model:

• cumulated number of *confirmed* cases  $(w_i)$ 

• cumulated number of deaths  $(d_i)$ 

 $\dot{I}(t) = eta(t)I(t) - \mu I(t) - 
u I(t)$  $\dot{H}(t) = 
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We assume that only a fraction  $\alpha$  of the infected people are *confirmed*,

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u I(t)$  $\dot{W}_c(t) = lphaeta(t)I(t)$  $\dot{H}(t) = 
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#### The data:

The epidemiological model:

- cumulated number of *confirmed* cases  $(w_j)$  $w_j$  predicted by  $W_c(t_j)$
- cumulated number of deaths  $(d_j)$  $d_j$  predicted by  $D(t_j)$

 $ar{I}(t) = eta(t)I(t) - \mu I(t) - 
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#### A first statistical model for the daily counts:

$$w_j - w_{j-1} = W(t_j) - W(t_{j-1}) + e_j \quad ; \quad e_j \sim \mathcal{N}(0, \sigma_e^2)$$

$$d_j - d_{j-1} = D(t_j) - D(t_{j-1}) + u_j \quad ; \quad u_j \sim \mathcal{N}(0, \sigma_u^2)$$

#### Parameters of the model:

 $heta = (lpha, eta_0, a, h_1, \dots, h_K, au_1, \dots, au_K, \mu, 
u, \lambda, I_0, H_0, D_0, \sigma_e^2, \sigma_u^2)$ 

 $egin{aligned} \dot{I}(t) &= eta(t)I(t) - \mu I(t) - 
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θ obtained by Maximum Likelihood (ML) Estimation*K* obtained by minimizing the Bayesian Information Criteria (BIC)

# Fitting the Italian data



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The residuals (daily numbers)



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The residuals errors exhibit a weekly periodic component: the observation model should include this periodic component.

#### The residuals (daily numbers)



#### Observations vs predictions (daily numbers)



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#### Observations vs predictions (daily numbers)



The magnitude of the errors increase with the prediction: the observation model should include a proportional error model

### The observation model

A second statistical model for the daily counts:
$$I(t) = \beta(t)I(t) - \mu I(t) - \nu I(t)$$
 $w_j - w_{j-1} = (W(t_j) - W(t_{j-1})) \left(1 + A\cos(\frac{2\pi}{7}t_j + \phi)\right) (1 + e_j)$  $\dot{W}_c(t) = \alpha\beta(t)I(t)$  $e_j \sim \mathcal{N}(0, \sigma_e^2)$  $\dot{H}(t) = \nu I(t) - \lambda H(t)$  $d_j - d_{j-1} = (D(t_j) - D(t_{j-1})) \left(1 + B\cos(\frac{2\pi}{7}t_j + \phi)\right) (1 + u_j)$  $\dot{D}(t) = \lambda H(t)$  $u_j \sim \mathcal{N}(0, \sigma_u^2)$  $\beta(t) = \beta_0 + at + \sum_{k=1}^K h_k t \times \mathrm{II}\{t \ge \tau_k\}$ 



Cumulated numbers

Daily numbers

Transmission rate





Some fits with the periodic component



Some fits without the periodic component

### About the basic reproduction number

 $\partial(\mathbf{n})$ 

$$\dot{I}(t) = \beta(t)I(t) - \mu I(t) - \nu I(t) \qquad \qquad R_0 = \frac{\beta(t)}{\mu + \nu}$$

- Not so easy to understand (at least for me)
- Seems to depend on the model (and not only on the parameter values)

The difference  $\beta(t) - \mu + \nu$ 

- (maybe) more informative than the ratio  $~~eta(t)/(\mu+
  u)$
- easy to interpret, as related to the "half-life"

$$t_2 = \log(2)/(eta - \mu + 
u)$$
  
 $t_{1/2} = -\log(2)/(eta - \mu + 
u)$ 





t2	2.9	4.7	2.6	4.4	6.9
t1/2	16.1	15.7	31.4	44.1	-

	Increase		Peak of daily deaths		Decrease	
Country	t4 ( ↑)	t2 (↑)	Date	n	t1/2 (↓)	t1/4 (↓)
Denmark	12	8	4/3/2020	16	25	50
Portugal	19	15	4/11/2020	32	24	41
Switzerland	16	11	4/5/2020	58	19	29
Netherlands	13	10	4/4/2020	155	28	46
Germany	19	14	4/13/2020	226	22	37
Belgium	21	15	4/15/2020	268	17	27
France	15	11	4/5/2020	532	20	34
Italy	15	10	3/27/2020	835	25	47
Spain	16	12	4/3/2020	839	17	33
United Kingdom	19	13	4/13/2020	927	27	50

Maximum daily number of deaths predicted by the model. For each country, t4 ( $\uparrow$ ) and t2 ( $\uparrow$ ) are, respectively, the number of days it took to multiply the number of deaths by 4 and 2 ; t1/2 ( $\downarrow$ ) and t1/4 ( $\downarrow$ ) are, respectively, the number of days it took to divide the number of deaths by 2 and 4.

This tool can be useful for detecting unexpected changes in the dynamics of the epidemics.

Portuguese data:



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... or to consider as expected what may seem unexpected

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♠ > Actualité > Fiches > Guide Vie quotidienne > Coronavirus

### Coronavirus dans le monde : hausse inquiétante des décès aux USA, les chiffres

Twitter



Partager sur Facebook



CORONAVIRUS. Le nombre de contaminations et de morts liés au Covid-19 semble repartir à la hausse aux Etats-Unis, selon le dernier bilan en date. De nombreux autres pays craignent ou constatent une résurgence du nombre de cas. Le

 $\boxtimes$ 

Email

point sur la pandémie dans le monde.



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Notable rebound in Germany of new cases and deaths from coronavirus



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Notable rebound in Germany of new cases and deaths from coronavirus



### 1) The transmission rate remains the same



### 2) The transmission rate is multiplied by 1.5



### 3) The transmission rate is multiplied by 2



### 4) The lockdown ends 2 weeks later (May 25)



### Possible scenarios before/after the lockdown

#### 5) The lockdown starts one week before (March 10)



### **About the data**

### Some French data...





### **About the data**

### Ireland:





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Bayesian approach should be used for introducing prior information (I think that  $\beta$  should not be far from 3... probably between 2.5 and 3.5)

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Thank you !